

Ludwig-Maximilians-Universität München
Lehrstuhl für Datenbanksysteme und Data Mining
Prof. Dr. Thomas Seidl

Knowledge Discovery and Data Mining 1

(Data Mining Algorithms 1)

Winter Semester 2022/23

Introduction



Agenda

1. Introduction

1.1 Organization

1.2 Motivation

1.3 Knowledge Discovery Process

2. Preliminaries: Data

3. Supervised Learning

4. Unsupervised Learning

5. Outlier Detection

6. Further Topics

4. Unsupervised Learning

5. Outlier Detection

6. Further Topics

Material, Tutorials & Exam

Material (Slides, Exercises, etc.)

Available via uni2work:

<https://uni2work.ifi.lmu.de/course/W22/IfI/KDD1>

Tutorial

- ▶ New exercise sheets available weekly
- ▶ Prepare at home
- ▶ Presentation and discussion one week after

Exam

- ▶ Written exam at the end of semester
- ▶ All material discussed in the lecture and tutorials
- ▶ Registration via [uni2work](#)

People

Lecturer

- ▶ Prof. Dr. Thomas Seidl

Assistants

- ▶ Philipp Jahn
- ▶ Simon Rauch
- ▶ Janina Sontheim

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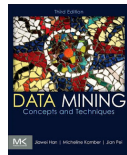
5. Outlier Detection

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Textbook / Acknowledgements

The slides used in this course are modified versions of the copyrighted original slides provided by the authors of the adopted textbooks:

- ▶ © Jiawei Han, Micheline Kamber, Jian Pei: *Data Mining – Concepts and Techniques*, 3rd ed., Morgan Kaufmann Publishers, 2011.
<http://www.cs.uiuc.edu/~hanj/bk3>
- ▶ © Martin Ester and Jörg Sander: *Knowledge Discovery in Databases – Techniken und Anwendungen* Springer Verlag, 2000 (in German).



Content of the Course

- ▶ Introduction
- ▶ Preliminaries – What is data, how to represent data, how to present data
- ▶ Classification – Supervised learning
- ▶ Clustering – Unsupervised learning
- ▶ Frequent Pattern Mining – Itemsets, sequences, processes
- ▶ Further topics – Outlook

Motivation

- ▶ Data Mining = extraction of patterns from data
- ▶ Patterns
 - ▶ Regularities – examples: frequent itemsets, clusters
 - ▶ Irregularities – examples: outliers
- ▶ Not all patterns are useful
 - ▶ *"all mothers in our database are female"* \rightsquigarrow trivial/known
 - ▶ *"bread, butter is frequent"* given *"bread, butter, salt is frequent"* \rightsquigarrow redundant
- ▶ Aggregation of data may help: Basic statistics

What is Data Mining?

Knowledge Discovery in Databases (Data Mining)

Extraction of interesting (*non-trivial, implicit, previously unknown and potentially useful*) information or patterns from data in *large databases*

Roots of Data Mining

- ▶ Statistics
- ▶ Machine Learning
- ▶ Database Systems
- ▶ Information Visualization

Data Mining and Machine Learning

Descriptive Learning

- ▶ Better understanding – data mining
- ▶ examples: pattern recognition, clustering, outlier detection

Predictive Learning

- ▶ Better forecasts – regression
- ▶ examples: traffic prediction, labeling, fraud detection

Prescriptive Learning

- ▶ Better actions – artificial intelligence
- ▶ examples: predictive maintenance, autonomous driving, medical therapies

Data Mining: Motivation

"Necessity is the mother of invention"

Data Explosion Problem

Tremendous amounts of data caused by

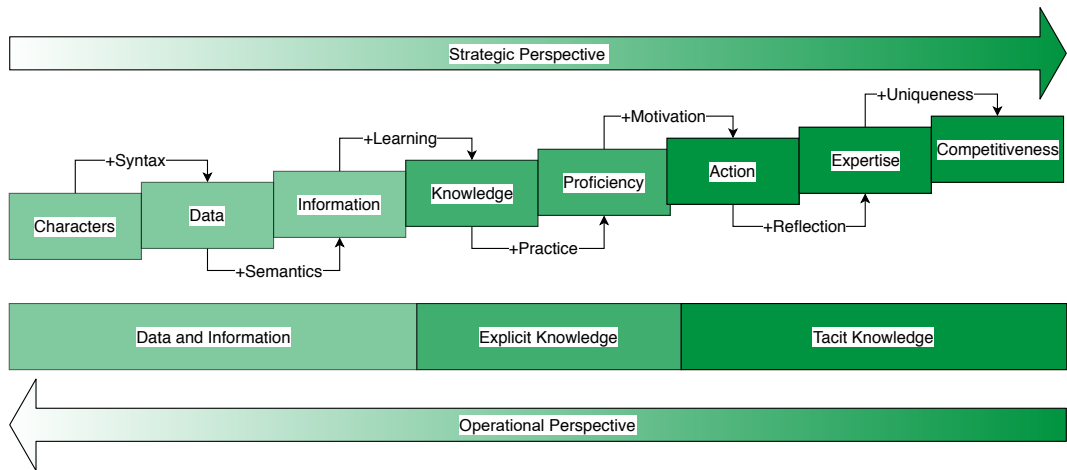
- ▶ Automated data collection
- ▶ Mature database technology

"We are drowning in data, but starving for knowledge!"

Solution

- ▶ Data Warehousing and on-line analytical processing (OLAP)
- ▶ Data Mining: Extraction of interesting knowledge (rules, regularities, patterns, constraints) from data in large databases

Data Mining: Motivation



Stairs of Knowledge (K. North) ¹

¹Stairs of Knowledge: North, K.: Wissensorientierte Unternehmensführung - Wertschöpfung durch Wissen. Gabler, Wiesbaden 1998.

Data Mining: Potential Applications

- ▶ Database analysis and decision support
 - ▶ *Market analysis and management:*
target marketing, customer relation management, market basket analysis, cross selling, market segmentation
 - ▶ *Risk analysis and management:*
Forecasting, customer retention ("Kundenbindung"), improved underwriting, quality control, competitive analysis
 - ▶ *Fraud detection and management*
- ▶ Other Applications:
 - ▶ Text mining (news group, email, documents) and Web analysis.
 - ▶ Intelligent query answering

References: Where to find scientific publications

	Conference	Journal
Data Mining and KDD	KDD, PKDD, SDM, PAKDD, ICDM, ...	Data Mining and Knowledge Discovery, ...
Database Field	ACM-SIGMOD, ACM-PODS, VLDB, ICDE, EDBT, CIKM, ...	ACM-TODS, J. ACM, IEEE-TKDE, JIIS, VLDBJ, ...
AI and Machine Learning	Machine learning, AAAI, IJCAI, ICLR, ...	Machine Learning, Artificial Intelligence, ...
Statistics	Joint Stat. Meeting, ...	Annals of Statistics, ...
Visualization	CHI (Comp. Human Interaction), ...	IEEE Trans. Visualization and Computer Graphics, ...

Useful bibliography: [DBLP.org](https://dblp.org)

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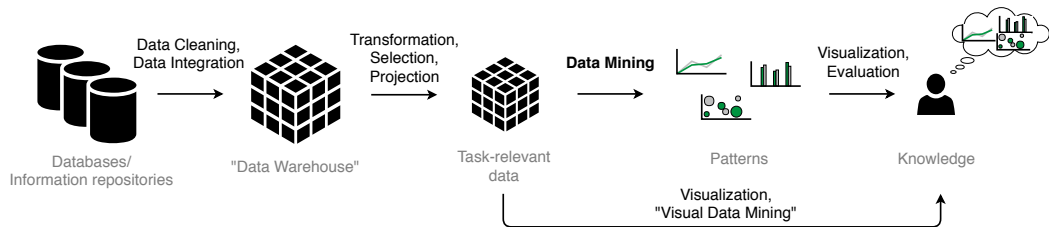
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The Knowledge Discovery Process

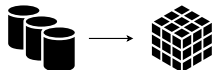
► The KDD-Process (Knowledge Discovery in Databases)



► Data Mining:

- Frequent Pattern Mining
- Clustering
- Classification
- Regression
- Process Mining
- ...

KDD Process: Data Cleaning & Integration



- ▶ ... may take 60% of effort
- ▶ Integration of data from different sources
 - ▶ Mapping of attribute names, e.g. $C_Nr \rightarrow O_Id$
 - ▶ Joining different tables, e.g. $Table1 = [C_Nr, Info1]$ and $Table2 = [O_Id, Info2]$
 $\leadsto JoinedTable = [O_Id, Info1, Info2]$
- ▶ Elimination of inconsistencies
- ▶ Elimination of noise
- ▶ Computation of missing values (if necessary and possible): Possible strategies e.g. default value, average value, or application specific computations

KDD Process: Focusing on Task-Relevant Data



Task

- ▶ Find useful features, dimensionality/variable reduction, invariant representation
- ▶ Creating a target data set

Selections

Select the relevant tuples/rows from the database tables, e.g., sales data for the last year

KDD Process: Focusing on Task-Relevant Data

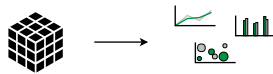
Projections

Select the relevant attributes/columns from the database tables, e.g., (id, name, date, location, amount) \rightsquigarrow (id, date, amount)

Transformations, e.g.:

- ▶ Discretization of numerical attributes, e.g.,
amount: [0, 100] \rightsquigarrow d_amount: {low, medium, high}
- ▶ Computation of derived tuples/rows and derived attributes:
 - ▶ aggregation of sets of tuples, e.g., total amount per months
 - ▶ new attributes, e.g., diff = sales current month - sales previous month

KDD Process: Basic Data Mining Tasks



Goal

Find patterns of interest

Tasks

- ▶ Identify task: Are there labels (in the training data)?
 - ▶ *Many* \rightsquigarrow Supervised learning (focus on given concepts)
 - ▶ *Some few* \rightsquigarrow Semi-supervised learning (focus on few hidden concepts)
 - ▶ *None* \rightsquigarrow Unsupervised learning (many hidden concepts)
- ▶ Choose fitting mining algorithm(s)

Basic Mining Tasks: Frequent Itemset Mining

Setting

Given a database of transactions,
e.g.

Transaction ID	Items Bought
2000	A,B,C
1000	A,C
4000	A,D
5000	B,E,F

Motivation

Frequently co-occurring items in the set of transactions indicate correlations or causalities

Examples

- ▶ $\text{buys}(x, \text{"diapers"}) \Rightarrow \text{buys}(x, \text{"beers"})$ [supp: 0.5%, conf: 60%]
- ▶ $\text{major}(x, \text{"CS"}) \wedge \text{takes}(x, \text{"DB"}) \Rightarrow \text{grade}(x, \text{"A"})$ [supp: 1.0%, conf: 75%]

Basic Mining Tasks: Frequent Itemset Mining

Applications

- ▶ Market-basket analysis
- ▶ Cross-marketing
- ▶ Catalogue design
- ▶ Also used as a basis for clustering, classification
- ▶ Association rule mining: Determine correlations between different itemsets

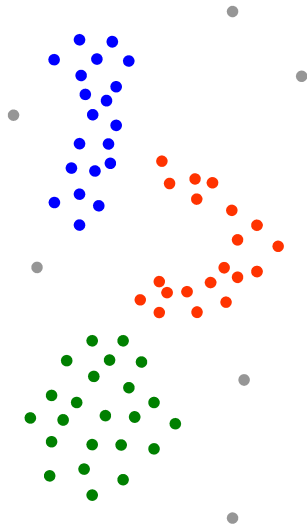
Basic Mining Tasks: Clustering

Setting

- ▶ Database of objects O
- ▶ Unknown class labels
- ▶ Similarity model for objects, often as (dis)similarity function $sim : O \times O \rightarrow \mathbb{R}$

Task

Group objects into clusters while maximizing intra-cluster similarity (cohesion) and minimizing inter-cluster similarity (separation)



Basic Mining Tasks: Clustering

Applications

- ▶ Customer profiling/segmentation
- ▶ Document or image collections
- ▶ Web access patterns
- ▶ ...

Basic Mining Tasks: Classification

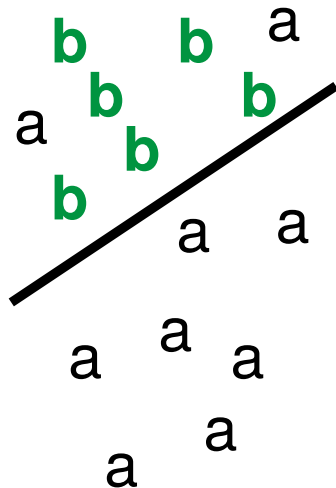
Setting

Class labels are known for a small set of "training data"

Task

Find models/functions/rules (based on attribute values of the training examples) that

- ▶ describe and distinguish classes
- ▶ predict class membership for "new" objects



Basic Mining Tasks: Classification

Applications

- ▶ Classify disease type for tissue samples from gene expression values
- ▶ Automatic assignment of categories to large sets of newly observed celestial objects
- ▶ Predict unknown or missing values (cf. KDD data cleaning & integration)
- ▶ ...

Basic Mining Tasks: Regression

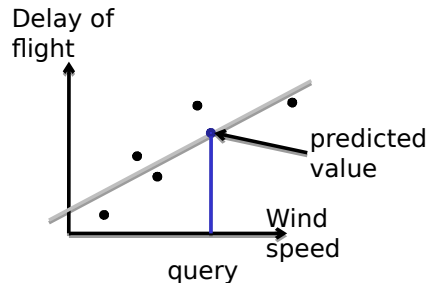
Setting

Numerical output values are known for a small set of "training data"

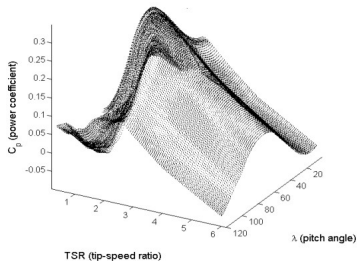
Task

Find models/functions/rules (based on attribute values of the training examples) that

- ▶ describe the numerical output values of the training data
- ▶ predict the numerical value for "new" objects



Basic Mining Tasks: Regression

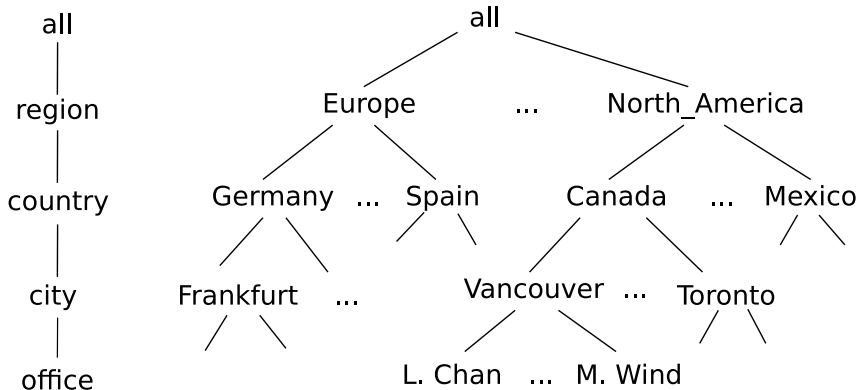


Applications

- ▶ Build a model of the housing values, which can be used to predict the price for a house in a certain area
- ▶ Build a model of an engineering process as a basis to control a technical system
- ▶ ...

Basic Mining Tasks: Generalization Levels

- ▶ Generalize, summarize, and contrast data characteristics
- ▶ Based on attribute aggregation along concept hierarchies
 - ▶ Data cube approach (OLAP)
 - ▶ Attribute-oriented induction approach



Basic Mining Tasks: Other Methods

Outlier Detection

Find objects that do not comply with the general behaviour of the data (fraud detection, rare events analysis)

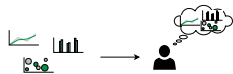
Trends and Evolution Analysis

Sequential patterns (find re-occurring sequences of events)

Methods for special data types, and applications

- ▶ Process Mining
- ▶ Spatial Data Mining
- ▶ Graphs
- ▶ ...

KDD Process: Evaluation and Visualization



- ▶ Pattern evaluation and knowledge presentation: Visualization, transformation, removing redundant patterns, etc.
- ▶ Different stages of visualization:
 - ▶ visualization of *data*
 - ▶ visualization of data mining *results*
 - ▶ visualization of data mining *processes*
 - ▶ *interactive* visual data mining
- ▶ Different types of 2D/3D plots, charts and diagrams are used, e.g. box-plots, trees, scatterplots, parallel coordinates
- ▶ Supports insights, usage, and trust in discovered knowledge

Summary

- ▶ Data mining = Discovering interesting patterns from large amounts of data
- ▶ A natural evolution of database technology, machine learning, statistics, visualization, in great demand, with wide applications
- ▶ A KDD process includes data cleaning, data integration, data selection, transformation, data mining, pattern evaluation, and knowledge presentation
- ▶ Data mining functionalities: characterization, discrimination, association, classification, clustering, outlier and trend analysis, etc.

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Knowledge Discovery and Data Mining 1

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Preliminaries: Data



Preliminaries: Data

- ▶ What is data?
 - Representation of real (or artificial) objects, situations, processes, ...
 - Measured by physical sensors → temperature, humidity, car traffic, speed, color, ...
 - Recorded from digital systems → bank transfers, web browsing, ...
 - Generated by simulations → weather forecast, digital mockups, ...
 - Stored and provided by computers → e.g., on local disk or on remote server
- ▶ How to represent data?
 - Numerical and categorical data types
 - Similarity models → allow for pattern mining
 - Data reduction → to increase efficiency
- ▶ How to present data?
 - Visualization
 - Privacy aspects

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1. Introduction

2. Preliminaries: Data

2.1 Data Representation

2.2 Visualization

2.3 Data Reduction

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6. Further Topics

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Data Types – Algebraic View

Ingredients of data types

- ▶ Types have identifiers: `int`, `long`, `float`, `double`, `boolean`, `char`, ...
- ▶ Types have domains \mathcal{D} : $\{1, 2, \dots\}$, $\{true, false\}$, $\{'hello', 'hi', 'howdy', \dots\}$
- ▶ Types have operations: `+`, `-`, `mod`, `div`, `and`, `or`, `not`, `concat`, ...

E.g., operations for comparison, as needed for data mining

- ▶ Equality tests $=, \neq: \mathcal{D} \times \mathcal{D} \rightarrow \{true, false\}$
- ▶ Distance functions $d: \mathcal{D} \times \mathcal{D} \rightarrow \mathbb{R}_0^+$
- ▶ Examples: Euclidean distance, maximum distance, difference value

Data Handling is Expensive – Implementation View

Data need storage space

- ▶ Single values need 1 Byte = 8 Bit, 4 Byte = 32 Bit, 8 Byte = 64 Bit
- ▶ Big data sets allocate Kilobytes 10^3 , Megabytes 10^6 , Gigabytes 10^9 , Terabytes 10^{12} , Petabytes 10^{15} , Exabytes 10^{18} , Zettabytes 10^{21} , etc
- ▶ Data compression helps (partially)

Operations need calculation time

- ▶ Calculating the Euclidean distance of two objects from \mathbb{R}^d needs $O(d)$ time
- ▶ Mean $\frac{1}{n} \sum_{i=1}^n x_i$ of n objects from \mathbb{R}^d needs $O(nd)$ time
- ▶ Covariance matrix of n objects $x_i \in \mathbb{R}^d$ needs $O(nd^2)$ time

Overview of Data Types

Simple, basic data types

Numerical data (numbers) or categorical data (symbols)

Composed data types

Vectors, sequences, sets, relations

Complex data types

- ▶ Multimedia data: images, videos, audio, text, documents, web pages, etc.
- ▶ Spatial data: shapes, geography, trajectories, etc.
- ▶ Structures: graphs, networks, trees, etc.

Numeric Data

Simple numeric data

- ▶ Numbers: natural, integer, rational, real numbers
- ▶ Domain examples: age, income, shoe size, height, weight
- ▶ (Dis-)similarity: difference value $d(x, y) = |x - y|$
- ▶ Example: 3 is more similar to 30 than 30 is to 3,000

Composed numeric data

- ▶ Vectors $x \in \mathbb{R}^d = \mathbb{R} \times \mathbb{R} \times \dots \times \mathbb{R}$ (d times)
- ▶ Examples: geolocation $(lat, lon) \in \mathbb{R}^2$, feature vector $x = (x_1, x_2, \dots, x_d) \in \mathbb{R}^d$
- ▶ Comparison by Euclidean distance, Manhattan dist., Earth Movers' dist., etc.

Examples: Comparisons of vectors by L_p -distance functions

Given two vectors $o, q \in \mathbb{R}^n$

Distances based on p -norms:

$$d_p(o, q) = \|o - q\|_p = \sqrt[p]{\sum_{i=1}^n |o_i - q_i|^p}$$

Euclidean distance (aerial, beeline)

$$d_2(o, q) = \|o - q\|_2 = \sqrt{\sum_{i=1}^n (o_i - q_i)^2}$$

Manhattan distance (city blocks)

$$d_1(o, q) = \|o - q\|_1 = \sum_{i=1}^n |o_i - q_i|$$

Maximum distance, $p \rightarrow \infty$

$$d_\infty(o, q) = \max\{|o_i - q_i|, i = 1..n\}$$

Weighted p -distances

$$d_{p,w}(o, q) = \sqrt[p]{\sum_{i=1}^n w_i \cdot |o_i - q_i|^p}$$

To illustrate, draw "circles" around c : $\{p \in \mathbb{R}^n, d(p, c) = \varepsilon\}$

Generalization: Metric Data

Metric Space

Metric space (O, d) consists of object set O and *metric distance* function $d : O \times O \rightarrow \mathbb{R}_0^+$ which fulfills:

$$\text{Symmetry: } \forall p, q \in O : d(p, q) = d(q, p)$$

$$\text{Identity of Indiscernibles: } \forall p, q \in O : d(p, q) = 0 \iff p = q$$

$$\text{Triangle Inequality: } \forall p, q, o \in O : d(p, q) \leq d(p, o) + d(o, q)$$

Example: Points in 2D space or in \mathbb{R}^n with Euclidean distance

Counterexamples: do we really want to have metrics in every application?

- ▶ non-symmetric: one-way roads on the way from p to q
- ▶ non-definite: indiscernible equivalent objects are not necessarily identical
- ▶ triangles: sometimes detours maybe preferred

Categorical data

- ▶ Symbols, "just identifiers"
- ▶ Examples:
 - ▶ subjects = { physics, biology, math, music, literature, ... }
 - ▶ occupation = { butcher, hairdresser, physicist, physician, ... }
- ▶ Similarity measure: How to compare values?

Example: Trivial metric

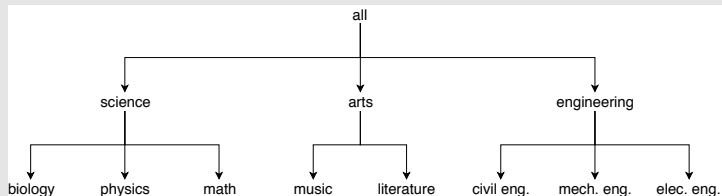
$$d(p, q) = \begin{cases} 0 & \text{if } p = q \\ 1 & \text{else} \end{cases}$$

Categorical data (cont'd)

Explicit similarity matrix, $O \times O \rightarrow \mathbb{R}_0^+$

	car	bike	trolley
car	1	0.3	0.1
bike	0.3	1	0.2
trolley	0.1	0.2	1

Path length in generalization hierarchy



Simple Data Types: Ordinal

Characteristic

There is a (total) order \leq on the set of possible data values O :

Transitivity: $\forall p, q, o \in O : p \leq q \wedge q \leq o \implies p \leq o$

Antisymmetry: $\forall p, q \in O : p \leq q \wedge q \leq p \implies p = q$

Totality: $\forall p, q \in O : p \leq q \vee q \leq p$

Examples

- ▶ Words & lexicographic ordering: $high \leq highschool \leq highscore$
- ▶ (Vague) sizes: $tiny \leq small \leq medium \leq big \leq huge$
- ▶ Frequencies, e.g.: $never \leq seldom \leq rarely \leq occasionally \leq sometimes \leq often \leq frequently \leq regularly \leq usually \leq always$
- ▶ Numbers (finite or infinite sets): $0 \leq 1 \leq 2 \leq \dots$, or $1.78 \leq 2.35 \leq 3.14 \leq \dots$

Composed Data Types: Sequences, Vectors

Characteristic

- ▶ Given a domain D , a sequence s of length n is a mapping $I_n \rightarrow D$ of the index set $I_n = \{1, \dots, n\}$ into D . Let us write $s \in D^n$ for short.
- ▶ The sequence s concatenates n values from D ; the order does matter

Examples

- ▶ Distances based on p -norms:
$$d_p(o, q) = \sqrt[p]{\sum_{i=1}^n |o_i - q_i|^p}$$
- ▶ Generalization, with ground distances d_i :
$$d_p(o, q) = \sqrt[p]{\sum_{i=1}^n d_i(o_i, q_i)^p}$$
- ▶ Note: d_p is metric iff all ground distances $d_i : D_i \times D_i \rightarrow \mathbb{R}_0^+$ are metric

Composed Data Types: Sets

Characteristic

Unordered collection of individual values

Examples

► $\text{skills} = \{\text{Java}, \text{C}, \text{Python}\}$, $\text{hobbies} = \{\text{skiing}, \text{diving}, \text{hiking}\}$

Comparison

► Symmetric Set Difference:

$$\begin{aligned} R \Delta S &= (R - S) \cup (S - R) \\ &= (R \cup S) - (R \cap S) \end{aligned}$$

► Jaccard Distance: $d(R, S) = \frac{|R \Delta S|}{|R \cup S|}$



$R \Delta S$



$R \cup S$

Composed Data Types: Sets

Bitvector Representation

- ▶ Given an ordered base set $B = (b_1, \dots, b_n)$, for any set S create a binary vector $r \in \{0, 1\}^n$ with $r_i = 1 \iff b_i \in S$.
- ▶ Hamming distance: Sum of different entries (equals cardinality of symmetric set difference)

Example

- ▶ Base: $B = (\text{Math}, \text{Physics}, \text{Chemistry}, \text{Biology}, \text{Music}, \text{Arts}, \text{English})$
- ▶ $S = \{\text{Math}, \text{Music}, \text{English}\} = (1, 0, 0, 0, 1, 0, 1)$
- ▶ $R = \{\text{Math}, \text{Physics}, \text{Arts}, \text{English}\} = (1, 1, 0, 0, 0, 1, 1)$
- ▶ $\text{Hamming}(R, S) = 3$

Complex Data Types

Examples for components of complex data

- ▶ Structure: graphs, networks, trees
- ▶ Geometry: shapes, contours, routes, trajectories
- ▶ Multimedia: images, audio, text, etc.

Similarity models: Approaches

- ▶ Direct measures – highly data type dependent
- ▶ Feature extraction / feature engineering – explicit vector space embedding with hand-crafted features
- ▶ Kernel trick – implicit vector space embedding
- ▶ Feature learning – (explicit) vector space embedding learned by deep learning methods, e.g. neural networks

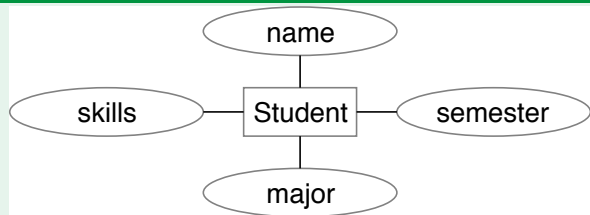
Complex Data Types

Examples for similarity models

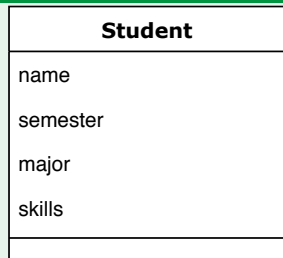
	Direct	Feature extraction	Kernel-based	Feature learning
Graphs	Structural Alignment	Degree Histograms	Label Sequence Kernel	Node embeddings, Spectral Neural Networks
Geometry	Hausdorff Distance	Shape Histograms	Spatial Pyramid Kernel	Convolutional Neural Networks (CNN)
Sequences	Edit Distance	Symbol Histograms	Cosine Distance	Recurrent neural network (RNN)

Objects and Attributes (Conceptual Modeling)

Entity-Relationship Diagram (ER)



UML Class Diagram

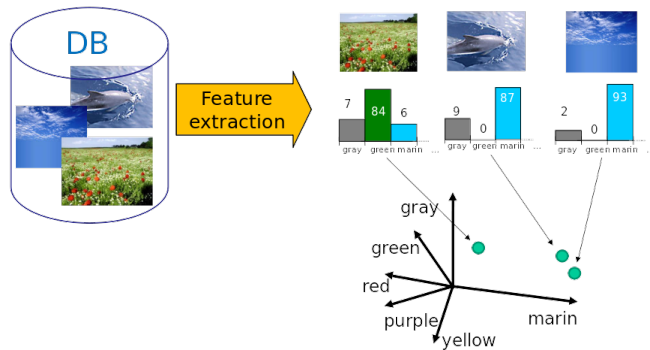


Data Tables (Relational Model)

name	sem	major	skills
Ann	3	CS	Java, C, R
Bob	1	CS	Java, PHP
Charly	4	History	Piano
Debra	2	Arts	Painting

Feature Extraction

- Objects from database DB are mapped to feature vectors



- Feature vector space
 - Points represent objects
 - Distance corresponds to (dis-)similarity

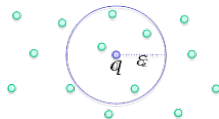
Similarity Queries

- ▶ Similarity queries are basic operations in (multimedia) databases
- ▶ Given: universe O , database $DB \subseteq O$, distance function d and query object $q \in O$

Range query

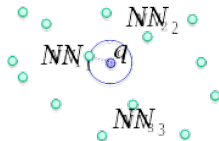
Range query for range parameter $\varepsilon \in \mathbb{R}_0^+$:

$$range(DB, q, d, \varepsilon) = \{o \in DB \mid d(o, q) \leq \varepsilon\}$$



Nearest neighbor query

$$NN(DB, q, d) = \{o \in DB \mid \forall o' \in DB : d(o, q) \leq d(o', q)\}$$



Similarity Queries

k -nearest neighbor query

k -nearest neighbor query for parameter $k \in \mathbb{N}$:

$$NN(DB, q, d, k) \subseteq DB \text{ with } |NN(DB, q, d, k)| = k \text{ and}$$

$$\forall o \in NN(DB, q, d, k), o' \in DB - NN(DB, q, d, k) : d(o, q) \leq d(o', q)$$

Ranking query

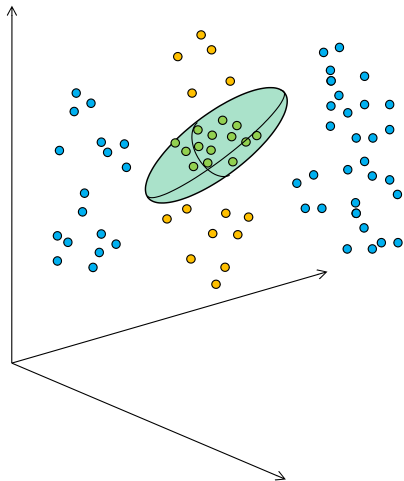
Ranking query (partial sorting query): "get next" functionality for picking database objects in an increasing order w.r.t. their distance to q :

$$\forall i \leq j : d(q, \text{rank}_{DB, q, d}(i)) \leq d(q, \text{rank}_{DB, q, d}(j))$$

Similarity Search

- ▶ Example: Range query $range(DB, q, d, \varepsilon) = \{o \in DB \mid d(o, q) \leq \varepsilon\}$
- ▶ Naive search by sequential scan
 - ▶ Fetch database objects from secondary storage (e.g. disk): $O(n)time$
 - ▶ Check distances individually: $O(n)time$
- ▶ Fast search by applying database techniques
 - ▶ Filter-refine architecture
 - ▶ Filter: Boil database DB down to (small) candidate set $C \subseteq DB$
 - ▶ Refine: Apply exact distance calculation to candidates from C only
 - ▶ Indexing structures
 - ▶ Avoid sequential scans by (hierarchical or other) indexing techniques
 - ▶ Data access in time $O(n)$, $O(\log n)$, or even $O(1)$

Filter-Refine Architecture

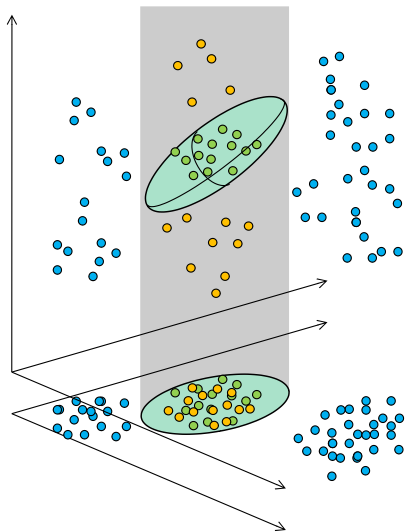


- ▶ Principle of multi-step search:
 1. Fast filter step produces candidate set $C \subset DB$ (by approximate distance function d')
 2. Exact distance function d is calculated on candidate set C only.
- ▶ Example: Dimensionality reduction^a
- ▶ ICES criteria for filter quality^b
 - I ndexable – Index enabled
 - C omplete – No false dismissals
 - E fficient – Fast individual calculation
 - S elective – Small candidate set

^aGEMINI: Faloutsos 1996; KNOP: Seidl & Kriegel 1998

^bAssent, Wenning, Seidl: ICDE 2006

Filter-Refine Architecture



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^bAssent, Wenning, Seidl: ICDE 2006

Indexing: Example

- ▶ Example: Phone book
- ▶ Indexed using alphabetical order of participants
- ▶ Instead of sequential search:
 - ▶ Estimate region of query object (interlocutor)
 - ▶ Check for correct branch
 - ▶ Use next identifier of query object
 - ▶ Repeat until query is finished

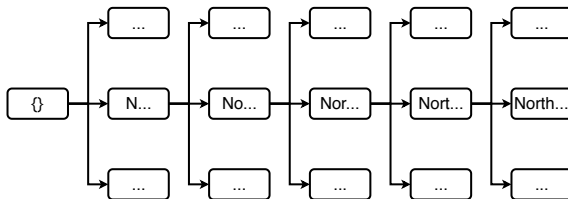
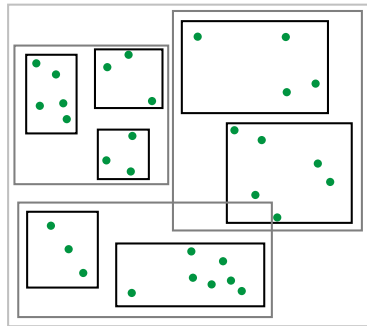
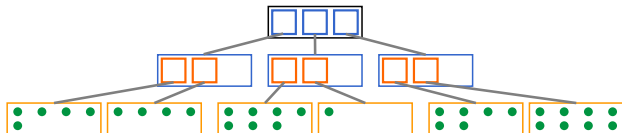


Image source: hierher/flickr, Licence: CC BY 2.0

Indexing: Principle

- Organize data in a way that allows for fast access to relevant objects, e.g. by heavy pruning.



- R-Tree as an example for spatial index structure:
 - Hierarchy of minimum bounding rectangles
 - Disregard subtrees which are not relevant for the current query region

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2.2 Visualization

2.3 Data Reduction

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5. Outlier Detection

6. Further Topics

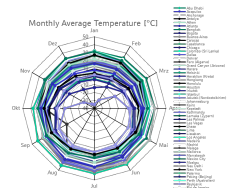
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Data Visualization

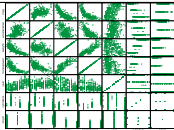
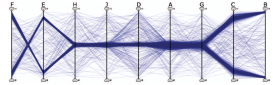
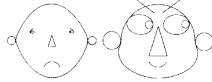

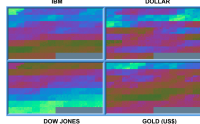
- ▶ Patterns in large data sets are hardly perceived from tabular numerical representations
- ▶ Data visualization transforms data in visually perceivable representations ("a picture is worth a thousand words")
- ▶ Combine capabilities:
 - ▶ Computers are good in number crunching (and data visualization by means of computer graphics)
 - ▶ Humans are good in visual pattern recognition



Monthly average temperature [°C]

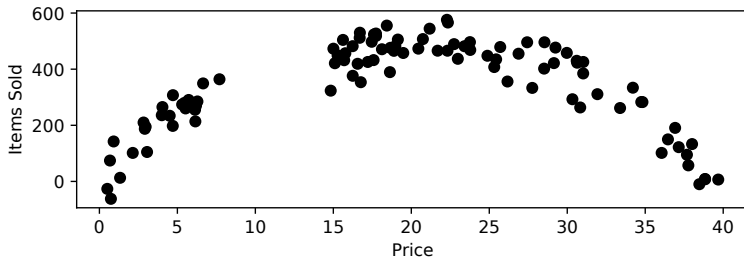
Städte Ø	Jan	Feb	Mrz	Apr	Mai	Jun	Jul	Aug	Sep	Okt	Nov	Dez
Abu Dhabi	25	27	31	36	40	41	42	43	42	37	31	27
Acapulco	32	31	32	32	33	33	33	33	33	33	32	32
Anchorage	-4	-2	0	6	13	17	18	17	13	5	-3	-5
Antalya	15	16	19	22	27	32	35	36	32	27	21	17
Athen	13	14	17	20	26	30	34	34	29	24	18	14
Atlanta	11	13	18	23	26	30	31	31	28	23	17	12
Bangkok	32	33	35	36	35	34	33	33	33	32	32	32
Bogota	20	19	19	19	19	18	18	18	18	19	19	20
Buenos Aires	30	28	26	23	19	16	15	17	19	21	26	29
Caracas	30	28	30	30	31	32	32	32	33	32	31	30
Casablanca	18	18	20	21	22	25	26	27	26	24	21	19
Chicago	0	1	9	16	21	26	29	28	24	17	9	2
Colombo (Sri Lanka)	31	31	32	32	32	31	31	31	31	31	31	31
Dallas	13	16	21	25	29	33	36	36	32	26	19	14
Denver	7	8	14	14	21	28	32	30	25	18	12	6
Faro (Algarve)	16	16	19	21	23	27	29	29	26	23	19	17
Grand Canyon (Arizona)	6	8	13	15	21	27	29	27	25	18	12	6
Harare	27	26	27	26	24	21	22	24	28	29	28	27
Helsinki	-3	-3	2	9	15	20	23	21	17	9	3	0
Heraklion (Kreta)	15	16	18	20	24	27	30	30	27	24	20	17
Hongkong	19	20	23	26	30	32	33	33	32	30	25	21
Honolulu	26	26	27	27	28	30	30	31	30	30	28	27
Houston	16	19	23	27	30	33	34	35	32	28	21	17
Irkutsk	-14	-9	1	9	16	23	24	21	16	7	-4	-13
Istanbul	9	9	13	17	23	27	30	30	26	20	15	11
Jakutsk (Nordostsibirien)	-35	-28	-10	3	14	23	26	21	11	-3	-25	-34
Johannesburg	25	25	24	22	20	17	17	20	24	25	25	25
Kairo	19	20	24	27	32	35	35	35	34	30	25	20
Kapstadt	27	27	26	24	21	18	18	18	19	22	24	26
Kathmandu	18	21	25	28	28	29	28	28	28	26	23	20
Larnaka (Zypern)	17	18	20	23	26	31	33	34	31	28	23	19
Las Palmas	21	20	22	23	24	25	27	28	28	27	24	22
Las Vegas	15	16	23	26	31	38	40	39	35	27	20	14
Lhasa	9	10	13	17	21	24	23	22	21	17	13	10
Lima	26	26	27	24	21	20	19	18	19	20	22	24
Lissabon	14	15	18	20	23	27	28	29	27	22	17	15

Data Visualization Techniques

Type	Idea	Examples
Geometric	Visualization of geometric transformations and projections of the data	 <p>Scatterplots</p>  <p>Parallel Coordinates</p>
Icon-Based	Visualization of data as icons	<p>Minimum Values of Data Range Maximum Values of Data Range</p>  <p>Chernoff Faces</p>  <p>Stick Figures</p>
Pixel-oriented	Visualize each attribute value of each data object by one coloured pixel	 <p>Recursive Patterns</p>
Other		Hierarchical Techniques, Graph-based Techniques, Hybrid-Techniques, ...

Slide credit: Keim, Visual Techniques for Exploring Databases, Tutorial Slides, KDD 1997.

2D Scatterplot



Characteristic

- ▶ Designed for two-dimensional data; two axes span the drawing area
- ▶ 2D objects are depicted as points in the diagram
- ▶ Orthogonal projections of points to axes indicate coordinate values
- ▶ Provides a first look at bivariate data to see clusters of points, outliers, etc.

Scatterplot Matrix

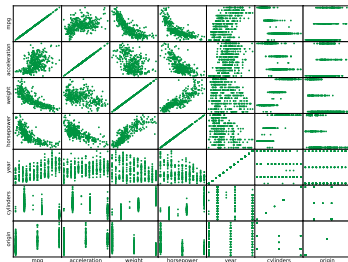
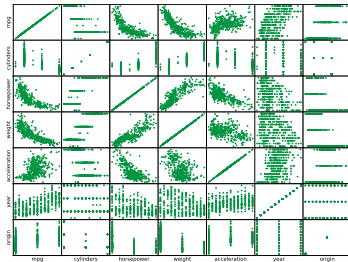
Characteristic

Matrix of scatterplots for pairs of dimensions

Ordering

Ordering of dimensions is important:

- ▶ Reordering improves understanding of structures and reduces clutter
- ▶ Interestingness of orderings can be evaluated with quality metrics (e.g. Peng et al.)



Clutter Reduction in Multi-Dimensional Data Visualization Using Dimension Reordering, IEEE Symp. on Inf. Vis., 2004.

Scatterplot Limitations

Limitations

- ▶ Scatterplots work well for two dimensions only
- ▶ Scatterplot matrices depict pairwise correlations only
- ▶ In perspective illustrations of three or more dimensions, projections get ambiguous

Polygonal Plots

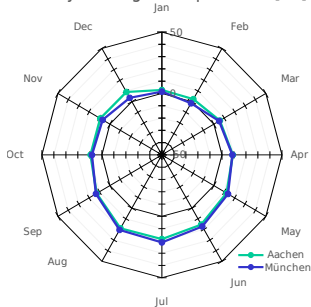
- ▶ Depict objects by curves rather than by points
- ▶ Coordinates are not indicated by orthogonal projections but by explicit intersections of polygons with axes
- ▶ Example Spiderweb – axes remain connected at origin
- ▶ Example Parallel Coordinates – axes are aligned in parallel

Spiderweb Model

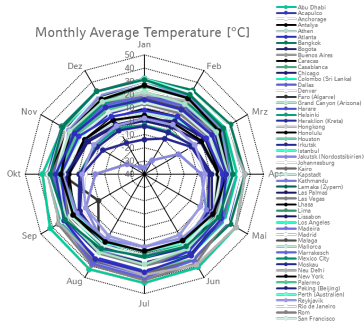
Characteristics

- ▶ Illustrate any single object by a polygonal line
- ▶ Contract origins of all axes to a global origin point
- ▶ Works well for few objects only

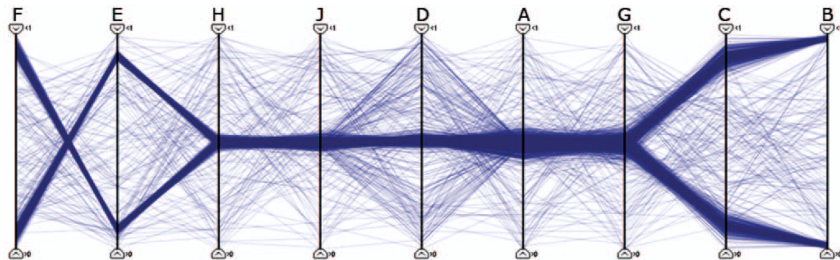
Monthly Average Temperature [°C]



Monthly Average Temperature [°C]



Parallel Coordinates



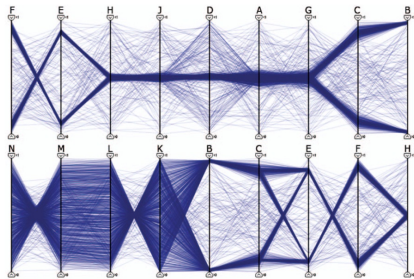
Characteristics

- ▶ d -dimensional data space is visualised by d parallel axes
- ▶ Each axis is scaled to min-max range
- ▶ Object = polygonal line intersecting axis at value in this dimension

Parallel Coordinates (cont'd)

Ordering

- ▶ Again, the ordering and orientation of the dimensions is important to reveal correlations
- ▶ The farther the attributes the harder their correlations are perceived; coloring helps



- ▶ Visualize clusters
- ▶ Visualize correlations between dimensions

Bertini et al., Quality Metrics in High-Dimensional Data Visualization: An Overview and Systematization, Trans. on Vis. and Comp. Graph., 2011.

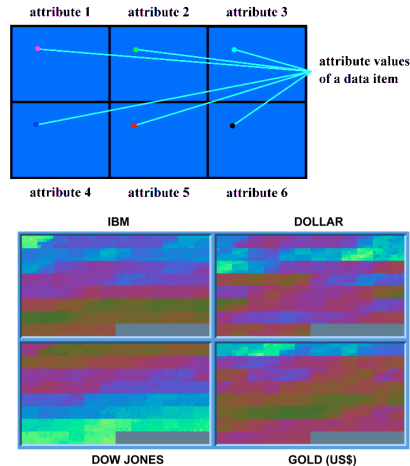
Pixel-Oriented Techniques

Characteristics

- ▶ Each data value is mapped onto a colored pixel
- ▶ Each dimension is shown in a separate window

How to arrange the pixel ordering?

One strategy: Recursive Patterns iterated line and column-based arrangements



Figures from Keim, Visual Techniques for Exploring Databases, Tutorial Slides, KDD 1997.

Chernoff Faces

Characteristics

Map d -dimensional space to facial expression, e.g. length of nose = dim 6; curvature of mouth = dim 8

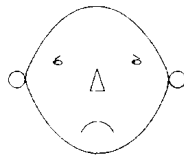
Advantage

Humans can evaluate similarity between faces much more intuitively than between high-dimensional vectors

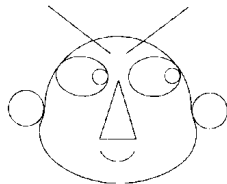
Disadvantages

- ▶ Without dimensionality reduction only applicable to data spaces with up to 18 dimensions
- ▶ Which dimension represents what part?

Minimum Values
of Data Range



Maximum Values
of Data Range



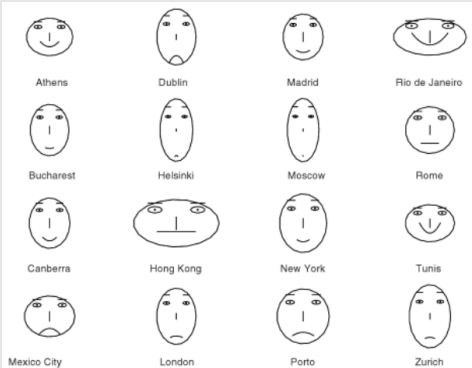
Figures taken from Mazza, Introduction to Information Visualization, Springer, 2009.

Chernoff Faces

Example: Weather Data

City	Precip. average	Temp. average	Temp. max average	Temp. min average	Record max	Record min
Athens	37	17	21	13	42	-3
Bucharest	58	11	16	5	49	-23
Canberra	62	12	19	6	42	-10
Dublin	74	10	12	6	28	-7
Helsinki	63	5	8	1	31	-36
Hong Kong	218	23	25	21	37	2
London	75	10	13	5	35	-13
Madrid	45	13	20	7	40	-10
Mexico City	63	17	23	11	32	-3
Moscow	59	4	8	1	35	-42
New York	118	12	17	8	40	-18
Porto	126	14	18	10	34	-2
Rio de Janeiro	109	25	30	20	43	7
Rome	80	15	20	11	37	-7
Tunis	44	18	23	13	46	-1
Zurich	107	9	12	6	35	-20

Table 4.1 Annual climatic values in Celsius of some world cities. Values from <http://www.weatherbase.com>.



Figures from Riccardo Mazza, Introduction to Information Visualization, Springer, 2009.

Chernoff Faces

Example: Finance Data

FIGURE 3
Facial Representation of Financial Performance (1 to 5 Years Prior to Failure)

Date Dimensions	FEDERAL				
	Year to Failure				
	5	4	3	2	1
1. Return on Assets	0.10	0.11	0.06	0.03	-0.16
2. Debt Service	3.66	3.79	1.55	0.78	-14.11
3. Cash Flows	1.53	1.48	1.39	1.35	0.94
4. Capitalization	0.22	0.20	0.18	0.16	-0.02
5. Current Ratio	71.40	89.10	97.85	96.80	58.21
6. Cash Turnover	24.03	25.92	25.62	27.40	71.26
7. Receivables Turnover	5.25	4.46	4.26	4.36	9.56
8. Inventory Turnover	5.38	4.77	4.57	4.44	5.34
9. Sales per Dollar Working Capital	6.74	6.33	7.02	7.61	-45.77
10. Retained Earning/ Total Assets	0.32	0.30	0.01	-0.01	-0.26
11. Total Assets	0.94	.76	0.39	0.45	0.43



Figure from Huff et al., Facial Representation of Multivariate Data, Journal of Marketing, Vol. 45, 1981, pp. 53-59.

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6. Further Topics

Data Reduction

Why data reduction?

- ▶ Better perception of patterns
 - ▶ Raw (tabular) data is hard to understand
 - ▶ Visualization is limited to (hundreds of) thousands of objects
 - ▶ Reduction of data may help to identify patterns
- ▶ Computational complexity
 - ▶ Big data sets cause prohibitively long runtime for data mining algorithms
 - ▶ Reduced data sets are useful the more the algorithms produce (almost) the same analytical results

How to approach data reduction?

- ▶ Data aggregation (basic statistics)
- ▶ Data generalization (abstraction to higher levels)

Data Reduction Strategies: Three Directions

ID	A1	A2	A3
1	54	56	75
2	87	12	65
3	34	63	76
4	86	23	4

Numerosity Reduction
Reduce number of objects

Dimensionality Reduction
Reduce number of attributes

Quantization, Discretization
Reduce number of values per domain

ID	A1	A3
1	L	75
3	XS	76
4	XL	4

Numerosity reduction

Reduce number of objects

- ▶ Sampling (loss of data)
- ▶ Aggregation (model parameters, e.g., center and spread)

Data Reduction Strategies (cont'd)

Dimensionality reduction

Reduce number of attributes

- ▶ Linear methods: feature sub-selection, Principal Components Analysis, Random projections, Fourier transform, Wavelet transform, etc
- ▶ Non-linear methods: Multidimensional scaling (force model), Neural embedding

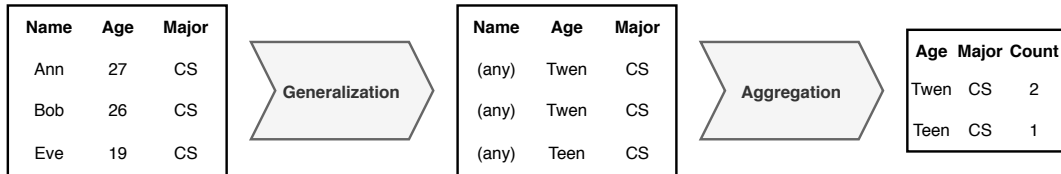
Quantization, discretization

Reduce number of values per domain

- ▶ Binning (various types of histograms)
- ▶ Generalization along hierarchies (OLAP, attribute-oriented induction)

Data Aggregation

- ▶ Aggregation is numerosity reduction (= less tuples)
- ▶ Generalization yields duplicates → add counting attribute and merge duplicate tuples



Basic Aggregates

- ▶ Central tendency: Where is the data located? Where is it centered?
 - ▶ Examples: mean, median, mode, etc. (see below)
- ▶ Variation, spread: How much do the data deviate from the center?
 - ▶ Examples: variance / standard deviation, min-max-range, ...

Examples

- ▶ Age of students is around 20
- ▶ Shoe size is centered around 40
- ▶ Recent dates are around 2020
- ▶ Average income is in the thousands

Distributive Aggregate Measures

Distributive Measures

The value of a *distributive measure* d on D can be calculated by combining the results of distributed calculations on partitions $D_i \subset D, D = D_1 \cup D_2 \cup \dots D_n$

Examples

- ▶ $count(D_1 \cup D_2) = count(D_1) + count(D_2)$
- ▶ $sum(D_1 \cup D_2) = sum(D_1) + sum(D_2)$
- ▶ $min(D_1 \cup D_2) = min(min(D_1), min(D_2))$
- ▶ $max(D_1 \cup D_2) = max(max(D_1), max(D_2))$

Algebraic Aggregate Measures

Algebraic Measures

An *algebraic measure* on D can be computed by an algebraic function with M arguments (M being a bounded integer), each of which is obtained by applying a distributive aggregate function to the partitions $D_i \subset D, D = D_1 \cup D_2 \cup \dots D_n$

Examples

- ▶ $avg(D_1 \cup D_2) = \frac{sum(D_1 \cup D_2)}{count(D_1 \cup D_2)} = \frac{sum(D_1) + sum(D_2)}{count(D_1) + count(D_2)}$
- ▶ Note: *avg* is not distributive, $avg(D_1 \cup D_2) \neq avg(avg(D_1), avg(D_2))$
- ▶ *standard_deviation*($D_1 \cup D_2$)

Holistic Aggregate Measures

Holistic Measures

There is no constant bound on the storage size that is needed to calculate and represent sub-aggregates.

Examples

- ▶ *median*: value in the middle of a sorted series of values (=50% quantile)

$$\text{median}(D_1 \cup D_2) \neq \text{simple_function}(\text{median}(D_1), \text{median}(D_2))$$

- ▶ *mode*: value that appears most often in a set of values
- ▶ *rank*: k -smallest / k -largest value (cf. quantiles, percentiles)

Measuring the Central Tendency

Mean – (weighted) arithmetic mean

Well-known measure for central tendency ("average").

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i \quad \bar{x}_w = \frac{\sum_{i=1}^n w_i x_i}{\sum_{i=1}^n w_i}$$

Mid-range

Average of the largest and the smallest values in a data set:

$$(max + min)/2$$

- ▶ Both are algebraic measures
- ▶ Applicable to numerical data only (sum, scalar multiplication)

What about categorical data?

Measuring the Central Tendency (cont'd)

Median

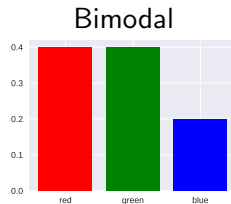
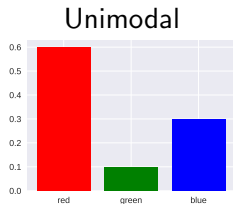
- ▶ Middle value of sorted values (if their count is odd)
- ▶ For even number of values: average of the middle two values (numeric case), or one of the two middle values (non-numeric case)
- ▶ Applicable to ordinal data only, as a (total) order is required
- ▶ Median is a holistic measure

Examples

- ▶ never, never, never, rarely, rarely, often, usually, usually, always
- ▶ tiny, small, big, big, big, big, big, big, huge, huge
- ▶ tiny, tiny, small, medium, big, big, large, huge

What if there is no ordering?

Measuring the Central Tendency



Mode

- ▶ Value that occurs most frequently in the data
- ▶ Example: *blue*, red, *blue*, yellow, green, *blue*, red
- ▶ Unimodal, bimodal, trimodal, ...: There are 1, 2, 3, ... modes in the data (multi-modal in general), cf. mixture models
- ▶ There is no mode if each data value occurs only once
- ▶ Well suited for categorical (i.e., non-numerical) data

Measuring the Dispersion of Data

Variance

- ▶ The variance measures the spread around the mean of numerical data:

$$\sigma^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2 = \frac{1}{n-1} \left[\sum_{i=1}^n x_i^2 - \frac{1}{n} \left(\sum_{i=1}^n x_i \right)^2 \right]$$

- ▶ The single pass calculation (sum of squares and square of sum in parallel) is faster than the two-pass method but numerically less robust in case of big numbers.
- ▶ Variance is zero if and only if all the values are equal
- ▶ Standard deviation is equal to the square root of the variance
- ▶ Both the standard deviation and the variance are algebraic measures

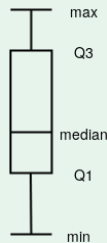
Boxplot Analysis

Boxplots comprise a five-number summary of a dataset

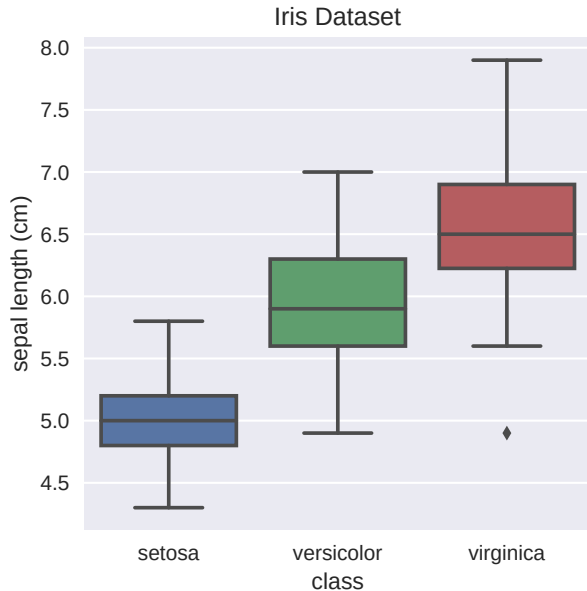
- ▶ Minimum, first quartile, median, third quartile, maximum
- ▶ These are the 0%, 25%, 50%, 75%, 100% quantiles of the data
- ▶ Also called "25-percentile", etc.

Boxplot illustration

- ▶ The box ranges from the first to the third quartile
- ▶ Height: inter-quartile range ($IQR = Q3 - Q1$)
- ▶ The median is marked by a line within the box
- ▶ Whiskers at minimum and maximum value
- ▶ Outliers: usually values more than $1.5 \cdot IQR$ below $Q1$ or above $Q3$

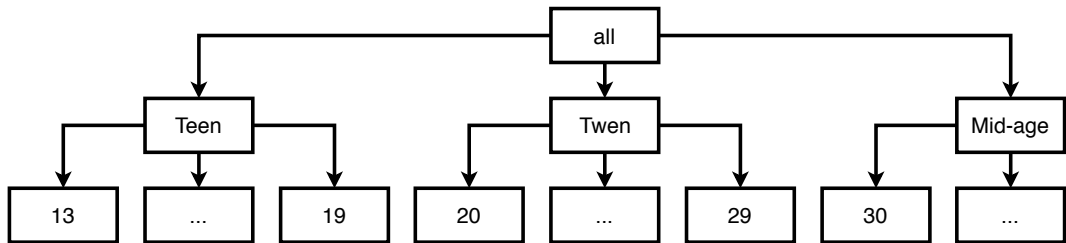


Boxplot Example



Data Generalization

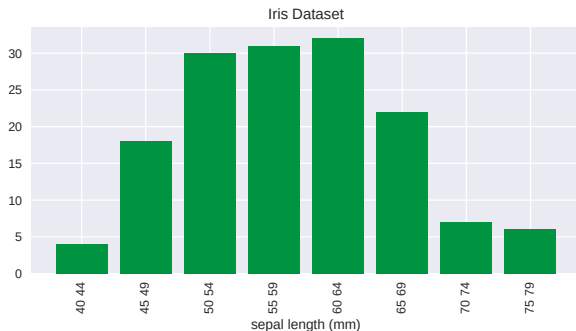
- ▶ Quantization may use generalization
 - ▶ E.g., group age (7 bits \rightarrow 128 values) to age_range (4 bits \rightarrow 16 values only)
- ▶ Dimensionality reduction is a borderline case of quantization
 - ▶ Dropping age corresponds to reduction zero bits
 - ▶ Corresponds to generalization of age to "all" = "any age" = no information



Data Generalization

- ▶ How to group the values of an attribute into partitions?
- ▶ Overall data (no partitioning, i.e., single partition)
 - ▶ Overall mean, overall variance: too coarse (overgeneralization)
- ▶ Different techniques to form groups for aggregation
 - ▶ Binning – histograms, based on value ranges
 - ▶ Generalization – abstraction based on generalization hierarchies
 - ▶ Clustering (see later) – based on object similarity

Binning Techniques: Histograms



- ▶ Histograms use binning to approximate data distributions
- ▶ Divide data into bins and store a representative (sum, average, median) for each bin

Equi-width Histograms

- ▶ Divide the range into N intervals of equal size (uniform grid)
- ▶ If A and B are the lowest and highest values of the attribute, the width of intervals will be $(B - A)/N$

Benefits

- ▶ Most straightforward
- ▶ Easy to understand

Limitations

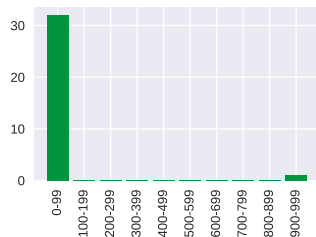
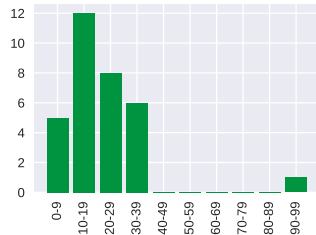
- ▶ Outliers may dominate presentation
- ▶ Skewed data is not handled well

Equi-width Histograms

Example

► Sorted data, 10 bins: 5, 7, 8, 8, 9, 11, 13, 13, 14, 14, 14, 15, 17, 17, 17, 18, 19, 23, 24, 25, 26, 26, 26, 27, 28, 32, 34, 36, 37, 38, 39, 97

► Insert 999



Equi-height Histograms

Divide the range into N intervals, each containing approx. the same number of samples (*quantile-based approach*)

Benefits

- ▶ Good data scaling
- ▶ Less prone to outliers

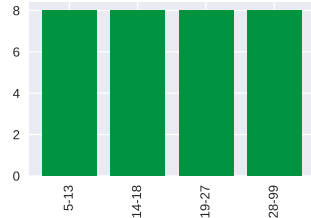
Limitations

- ▶ Key information in bin boundaries (somehow subtle)
- ▶ If any value occurs often, the equal frequency criterion might not be met (intervals have to be disjoint!)

Equi-height Histograms

Example

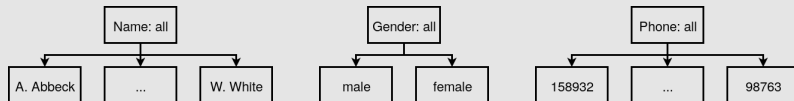
- ▶ Same data, 4 bins: 5, 7, 8, 8, 9, 11, 13, 13, 14, 14, 14, 15, 17, 17, 17, 18, 19, 23, 24, 25, 26, 26, 26, 27, 28, 32, 34, 36, 37, 38, 39, 97



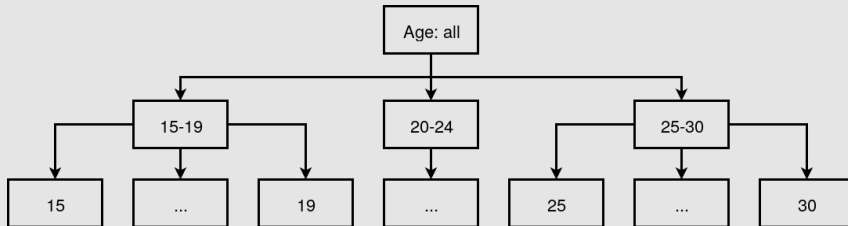
- ▶ Median = 50%-quantile
 - ▶ More robust against outliers (cf. value 999 from above)
 - ▶ Four bin example is strongly related to boxplot

Concept Hierarchies: Examples

Flat groups (i.e., no serious hierarchies)

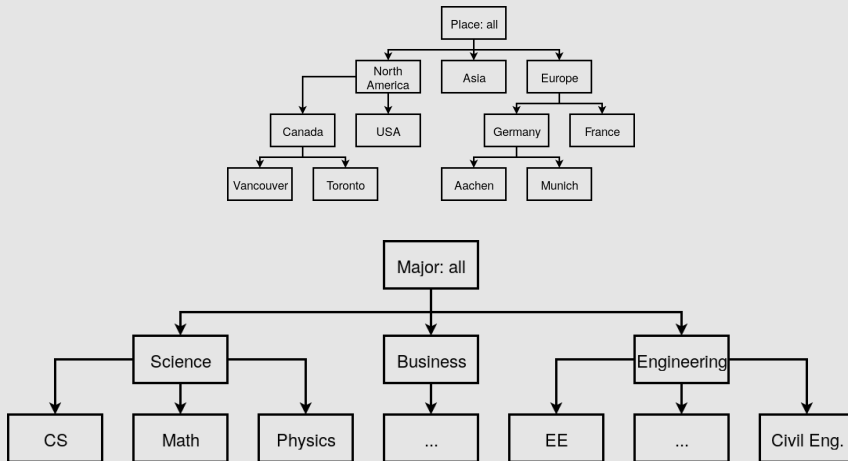


Hierarchies by subgrouping



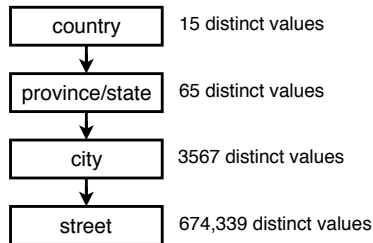
Concept Hierarchies: Examples

Hierarchies from schema information



Concept Hierarchy for Categorical Data

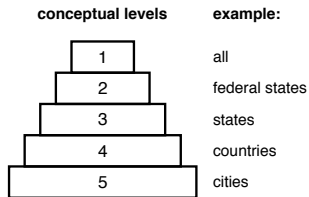
- ▶ Concept hierarchies can be specified by (expert) users
- ▶ Heuristically generate a hierarchy for a set of (related) attributes
 - ▶ based on the number of distinct values per attribute in the attribute set
 - ▶ The attribute with the most distinct values is placed at the lowest level of the hierarchy
- ▶ Fails for counter examples: 20 distinct years, 12 months, 7 days_of_week, but not "year < month < days_of_week" with the latter on top



Summarization-based Aggregation

Data Generalization

A process which abstracts a large set of task-relevant data in a database from low conceptual levels to higher ones.



- ▶ Approaches:
 - ▶ Data-cube approach (OLAP / Roll-up) – manual
 - ▶ Attribute-oriented induction (AOI) – automated

Basic OLAP (One Line Analytical Processing) Operations

Roll up

Summarize data by climbing up hierarchy or by dimension reduction.

Drill down

Reverse of roll-up. From higher level summary to lower level summary or detailed data, or introducing new dimensions.

Slice and dice

Selection on one (slice) or more (dice) dimensions.

Pivot (rotate)

Reorient the cube, visualization, 3D to series of 2D planes.

Example: Roll up / Drill down

Query

```
SELECT country , quarter , some_agg_fnc (...)
FROM business
GROUP BY country , quarter
```

Roll-Up

```
SELECT continent , quarter , some_agg_fnc (...)
FROM business
GROUP BY continent , quarter
```

```
SELECT country , some_agg_fnc (...)
FROM business
GROUP BY country
```

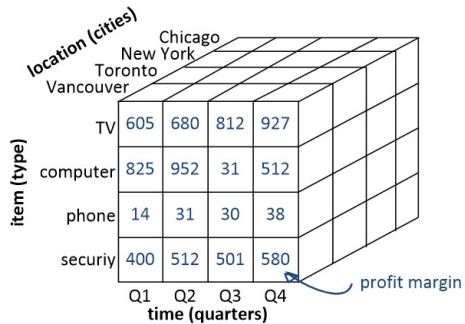
Drill-Down

```
SELECT city , quarter , some_agg_fnc (...)
FROM business
GROUP BY city , quarter
```

```
SELECT country , quarter , product , some_agg_fnc (...)
FROM business
GROUP BY country , quarter , product
```

Example: Roll up and Drill-Down in a Data Cube

Data Cube: Sales



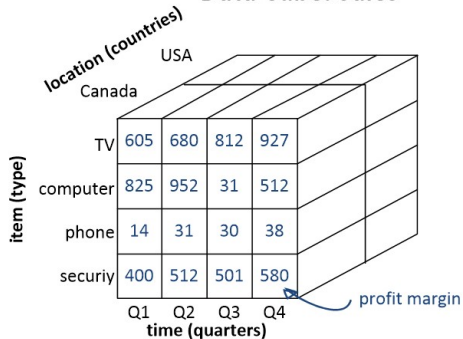
Roll Up



Drill-Down



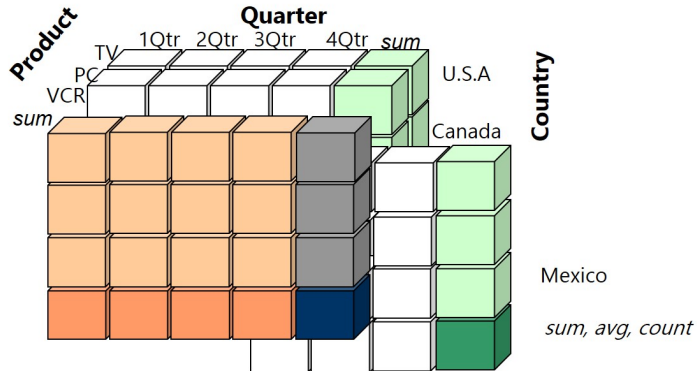
Data Cube: Sales



Example: Slice Operation

```
SELECT income
FROM   time t, product p, country c
WHERE  p.name = 'VCR'
```

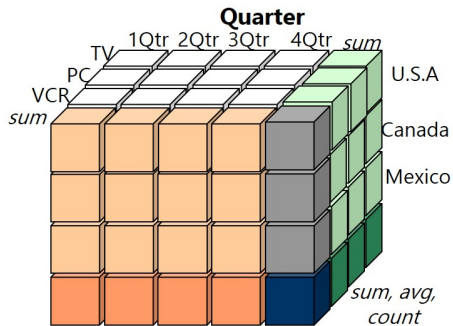
VCR dimension is chosen



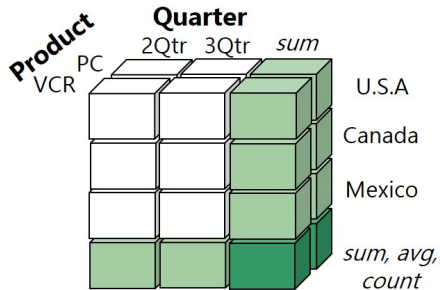
Example: Dice Operation

```
SELECT income
FROM   time t, product p, country c
WHERE  p.name = 'VCR' OR p.name = 'PC' AND t.quarter BETWEEN 2 AND 3
```

sub-data cube over PC, VCR and quarters 2 and 3 is extracted



Dice
⇒



Example: Pivot (rotate)

year	17			18			19		
product	TV	PC	VCR	TV	PC	VCR	TV	PC	VCR
	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮

↓ Pivot (rotate) ↓

product	TV			PC			VCR		
year	17	18	19	17	18	19	17	18	19
	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮

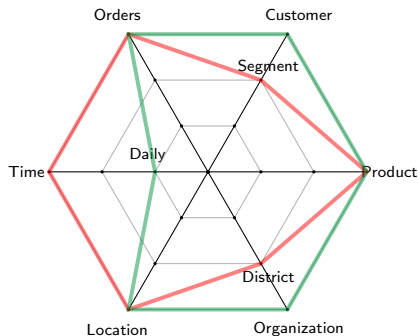
Further OLAP Operations

Other operations

- ▶ *Drill across*: involving (across) more than one fact table
- ▶ *Drill through*: through the bottom level of the cube to its back-end relational tables (using SQL)

Specifying Generalizations by Star-Nets

- ▶ Each circle is called a *footprint*
- ▶ Footprints represent the granularities available for OLAP operations



Discussion of OLAP-based Generalization

- ▶ Strength
 - ▶ Efficient implementation of data generalization
 - ▶ Computation of various kinds of measures, e.g., count, sum, average, max
 - ▶ Generalization (and specialization) can be performed on a data cube by roll-up (and drill-down)
- ▶ Limitations
 - ▶ Handles only dimensions of simple non-numeric data and measures of simple aggregated numeric values
 - ▶ Lack of intelligent analysis, does not suggest which dimensions should be used and what levels the generalization should aim at

Attribute-Oriented Induction (AOI)

- ▶ More automated approach than OLAP
- ▶ Apply aggregation by merging identical, generalized tuples and accumulating their respective counts.
- ▶ Builds on *data focusing*: task-relevant data, including dimensions, resulting in the *initial relation*
- ▶ Generates a *generalization plan*: decide for either *attribute removal* or *attribute generalization*

Attribute-Oriented Induction (AOI)

Three choices for each attribute: keep it, remove it, or generalize it

Attribute Removal

Remove attribute A in the following cases:

- ▶ There is a large set of distinct values for A but there is no generalization operator (concept hierarchy) on A , or
- ▶ A 's higher level concepts are expressed in terms of other attributes (e.g. *street* is covered by *city*, *state*, *country*).

Attribute Generalization

If there is a large set of distinct values for A , and there exists a set of generalization operators (i.e., a concept hierarchy) on A , then select an operator and generalize A .

Attribute Oriented Induction: Example

Name	Gender	Major	Birth place	Birth data	Residence	Phone	GPA
Jim Woodman	M	CS	Vancouver, BC, Canada	8-12-81	3511 Main St., Richmond	687-4598	3.67
Scott Lachance	M	CS	Montreal, Que, Canada	28-7-80	345 1st Ave., Richmond	253-9106	3.70
Laura Lee	F	Physics	Seattle, WA, USA	25-8-75	125 Austin Ave., Burnaby	420-5232	3.83
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮

- ▶ Name: large number of distinct values, no hierarchy – **removed**
- ▶ Gender: only two distinct values – **retained**
- ▶ Major: many values, hierarchy exists – **generalized to Sci., Eng., Biz.**
- ▶ Birth_place: many values, hierarchy – **generalized, e.g., to country**
- ▶ Birth_date: many values – **generalized to age (or age_range)**
- ▶ Residence: many streets and numbers – **generalized to city**
- ▶ Phone number: many values, no hierarchy – **removed**
- ▶ Grade_point_avg (GPA): hierarchy exists – **generalized to good, ...**
- ▶ Count: **additional attribute to aggregate base tuples**

Attribute Oriented Induction: Example

► Initial Relation:

Name	Gender	Major	Birth place	Birth data	Residence	Phone	GPA
Jim Woodman	M	CS	Vancouver, BC, Canada	8-12-81	3511 Main St., Richmond	687-4598	3.67
Scott Lachance	M	CS	Montreal, Que, Canada	28-7-80	345 1st Ave., Richmond	253-9106	3.70
Laura Lee	F	Physics	Seattle, WA, USA	25-8-75	125 Austin Ave., Burnaby	420-5232	3.83
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮

► Prime Generalized Relation:

Gender	Major	Birth region	Age Range	Residence	GPA	Count
M	Science	Canada	20-25	Richmond	Very good	16
F	Science	Foreign	25-30	Burnaby	Excellent	22
⋮	⋮	⋮	⋮	⋮	⋮	⋮

► Crosstab for generalized relation:

	Canada	Foreign	Total
M	16	14	30
F	10	22	32
Total	26	36	62

Attribute Generalization Control

- ▶ Two common approaches
 - ▶ *Attribute-threshold control*: default or user-specified, typically 2-8 values
 - ▶ *Generalized relation threshold control*: control the size of the final relation/rule, e.g., 10-30 tuples
- ▶ Tradeoff: how many distinct values for an attribute?
 - ▶ *Overgeneralization*: values are too high-level
 - ▶ *Undergeneralization*: level not sufficiently high
 - ▶ Both yield tuples of poor usefulness

Strategies for Next Attribute Selection

- ▶ Aiming at *minimal degree of generalization*
 - ▶ Choose attribute that reduces the number of tuples the most
 - ▶ Useful heuristic: choose attribute with highest number of distinct values.
- ▶ Aiming at *similar degree of generalization* for all attributes
 - ▶ Choose the attribute currently having the least degree of generalization
- ▶ *User-controlled*
 - ▶ Domain experts may specify appropriate priorities for the selection of attributes