

Lecture Notes for  
**Managing and Mining Multiplayer Online Games**  
Summer semester 2018

## Chapter 7: Spatial Analytics

Lecture Notes © 2012 Matthias Schubert

[http://www.dbs.ifi.lmu.de/cms/VO\\_Managing\\_Massive\\_Multiplayer\\_Online\\_Games](http://www.dbs.ifi.lmu.de/cms/VO_Managing_Massive_Multiplayer_Online_Games)

# Chapter Overview

---

- spatial data mining in games
- visual analytics and heat maps
- spatial outliers
- trajectories: representation and similarity
- pattern search on trajectory data

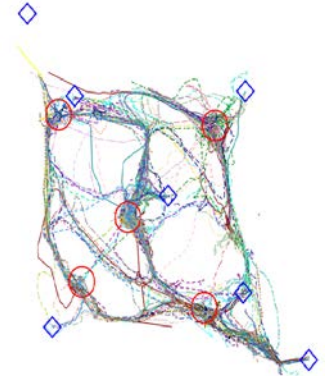
# Spatial Data Mining and Games

- many games take place in a virtual 2D-/3D-World
- movement and position is often an important part of game play
- game world design is relevant for balancing
- analysis of spatial and spatial-temporal information is referred to as *Spatial Data Mining*



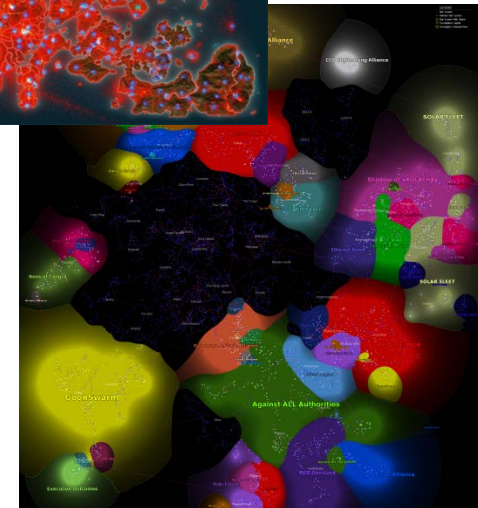
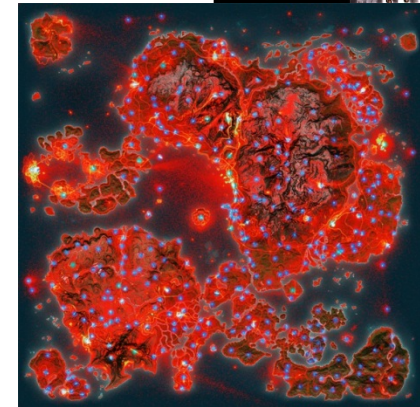
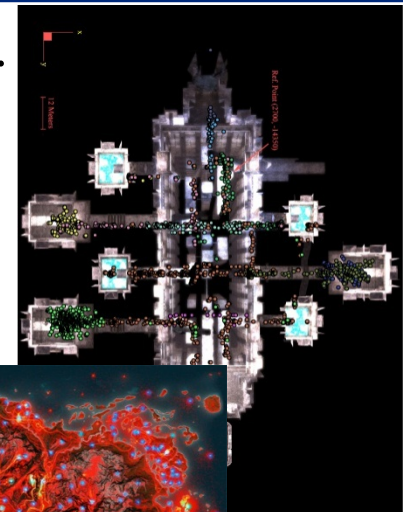
# Tasks of Spatial Game Analytics

- find exploitation spots
  - extract game moves and movement strategies
  - encounter detection (open PVP)
  - sub team recognition
  - dynamic adjustment of respawn times
  - detect bot and multiboxers
  - detect movement and teleportation hacks
- ⇒ find specific places  
(heat-maps, spatial outliers)
- ⇒ find movement patterns (trajectory mining)



# Spatial Data and Visualization

- spatial data consists of object descriptions and positions.  
(Example: Marine, 43,56)
  - to find special places, object descriptions are aggregated w.r.t. positions  
(e.g. number of kills at a position, monster's spawn frequency at a place)
  - spatial continuity: usually one assumes adjacent positions to behave in a similar fashion.
- ⇒ presentation of aggregated information in 2D histograms (bin counting)
- ⇒ presentation of spatial continuity with smoothing approach (kernel density estimation)



# Heat Maps

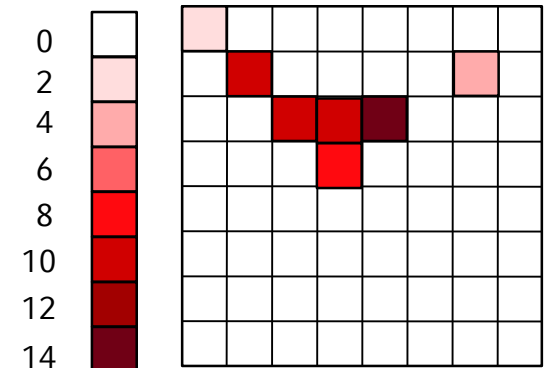
- visualizing the distribution of events on X-,Y-coordinates of a map.
- displaying the distribution as a 2D-Density distribution.
- a bin's height is encoded with it's color.

## simple algorithm: Bin Counting

1. place uni-distance Grid overlay on the map
2. for every event
  1. determine grid cell
  2. increase grid cell counter by 1
3. draw the grid and color each cell matching the number within.



3							
	10					5	
		11	11	14			
			9				

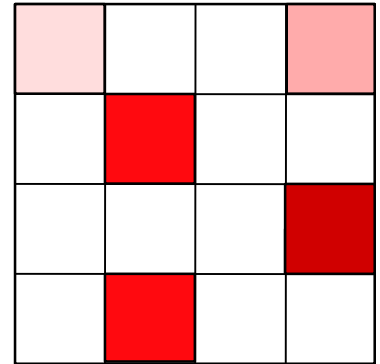
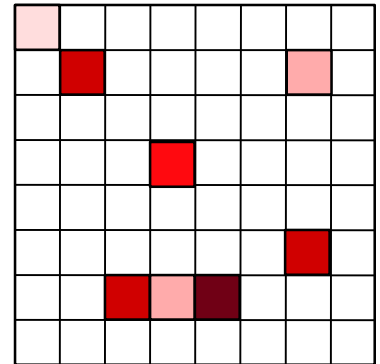


# Heat Maps

## Problems with bin counting:

- setting grid-size:
  - too small: torn view, few dense areas
  - too big: rough view, few differences
- grid position influences result
- spatial continuity may be hardly discernible

**Remedy:** smooth curves with kernel density estimation  
estimate density with the sum of kernel functions  
⇒ continuous and smoothed density function  
⇒ discretization of data only for drawing



# Kernel density estimator

- method to estimate a continuous density function from a sample set  $X$ .
- consider density  $p(t)$  as mixture model of  $|X|$  distributions, all of them distributed with kernel function  $K(t)$ :

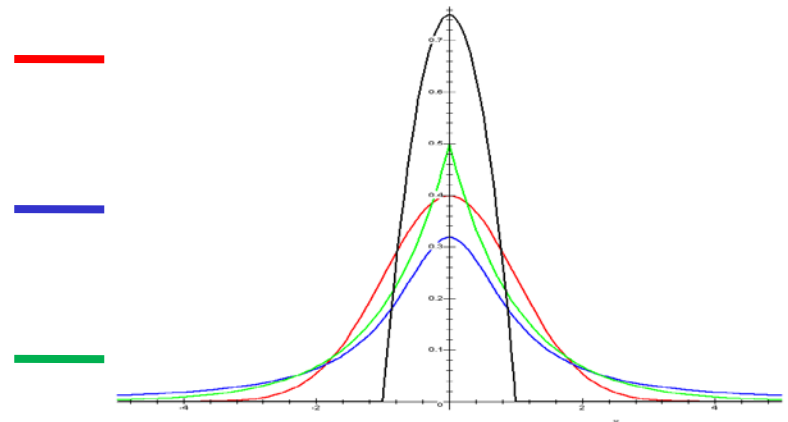
- common kernel functions:  $p(x) = \frac{1}{|X|} \sum_{t \in X} K(t - x)$

- Gauss-kernel :  $K(t) = \frac{1}{\sqrt{2\pi}} e^{\left(-\frac{1}{2}t^2\right)}$

- Cauchy-kernel:  $K(t) = \frac{1}{\pi(1+t^2)}$

- Picard-kernel :  $K(t) = \frac{1}{2} e^{(-|t|)}$

- Epanechnikow-kernel:  $K(t) = \begin{cases} \frac{3}{4}(1-t^2), & \text{falls } t \in [-1;1] \\ 0 & \text{sonst} \end{cases}$





# Heatmaps with kernel density estimators

- kernels in 2D-Space assuming independent dimensions:
- every bin corresponds to one pixel
- for every pixel  $P$ ,  $p(m)$  is calculated based on pixel center  $m$
- for efficient calculation:

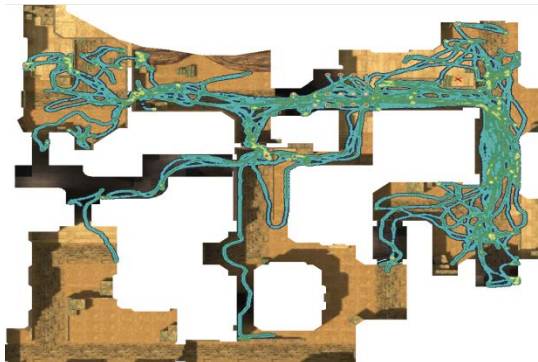
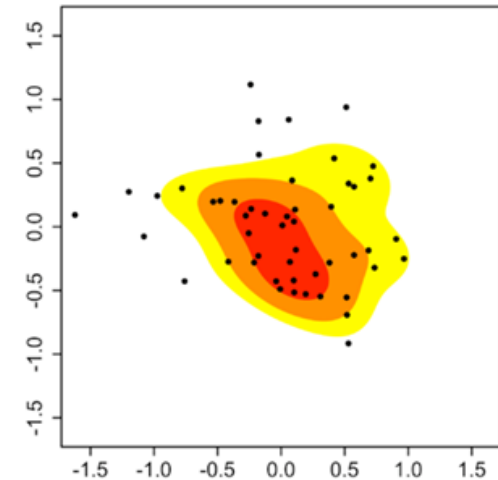
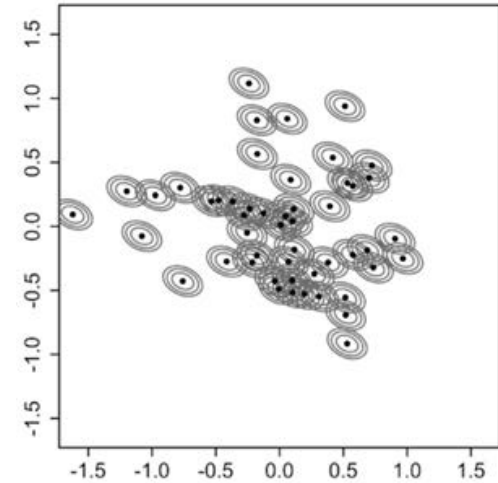
for all points  $x$ :

for all pixel  $p$ :

for both dimensions:

increase the value of  $p$   
by  $K(x-p_m)$  with  $p_m$  center of  $p$

$$p(t) = \left( \frac{1}{|X|} \sum_{x \in X} K(t_1 - x_1) \right) \cdot \left( \frac{1}{|X|} \sum_{x \in X} K(t_2 - x_2) \right)$$



# Spatial Data Mining

---

- particular data mining methods for spatial objects.
- object  $O$  consists of a spatial component  $p \in \mathbb{R}^2/\mathbb{R}^3$  and an object description  $v \in F$ . ( $F$  is an arbitrary feature space)
- special tasks in spatial data mining:
  - **Spatial Outlier Detection:** find places where the feature descriptions significantly varies from the object description of close objects.  
(Example: exploitation spots where you can not be hit.)
  - **Spatial Prediction:** prediction of areas where certain phenomena are more frequent. (Example: calculate the probability of a certain behavior occurring at a certain spot.)
  - **Spatial Clustering:** Clustering using proximity as well as similarities of the feature space to create or differentiate clusters.  
(Example: Are any actions frequently taken at certain areas of the map?)
  - **Spatial Rule Mining:** Derivation of association rules based on frequent spatial patterns. (Example: 80% of cities built within 50 km of another players settlement do not survive until the end of the game.)

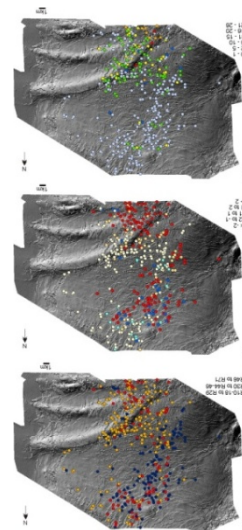
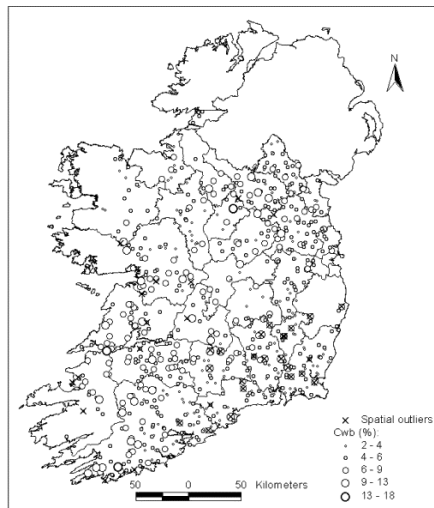
# Spatial Outlier Detection

**Given:** A set DB of spatial objects  $O = (p, v)$ .

**Searched:** Objects that are unusual for their neighborhood.

## *General procedure:*

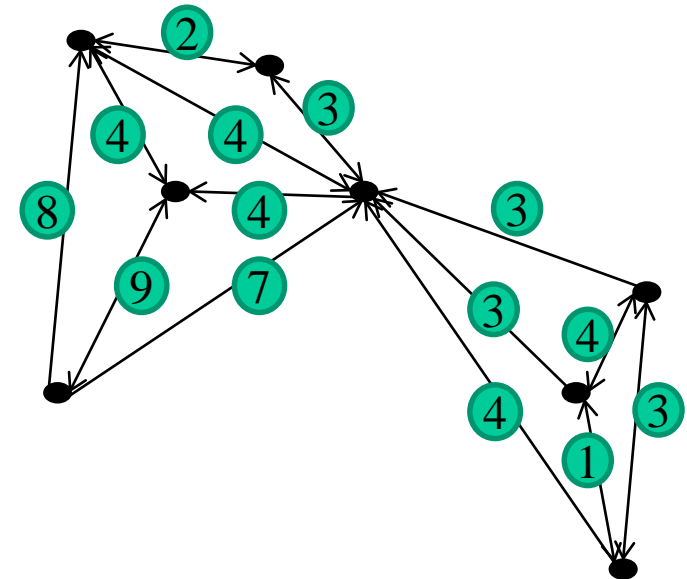
1. Determine neighborhood  $N$  for every object  $O$ .  
(e.g  $N$  consists of  $k$  closest neighbors of  $O$ ).
2. Compare the feature description of  $O.v$  with the distribution of feature descriptions in  $N$ .



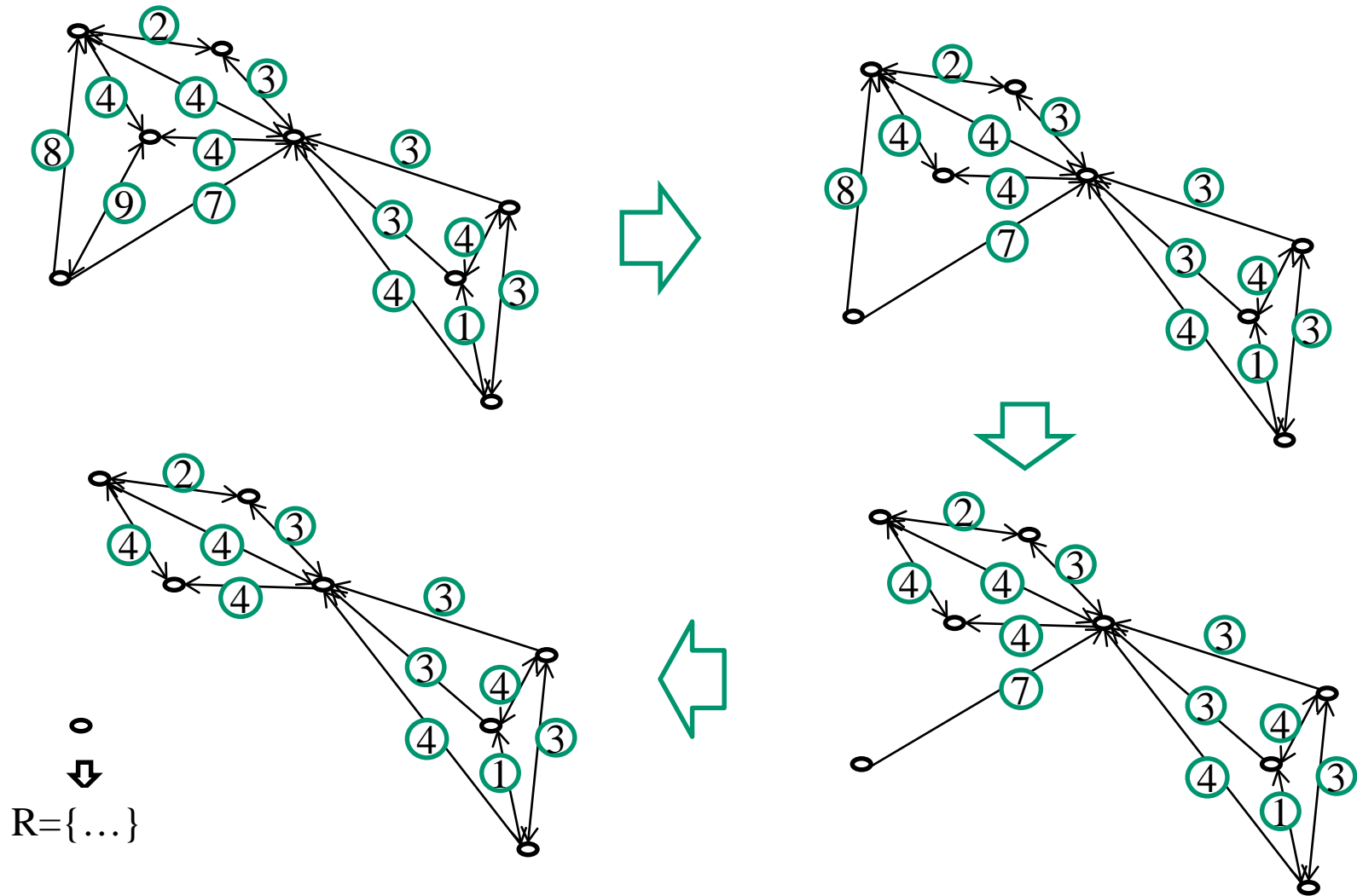
# Spatial Outlier Detection

## ***Point Outlier Detection (POD):***

1. set up a nearest neighbor graph  $G(DB, E)$  for spatial positions.  
 $E := \{(o_i, o_j) \mid o_i, o_j \in DB \wedge o_j \in NN_k(o_i)\}$   
weighting function:  
 $w(o_i, o_j) = ||o_i.v - o_j.v||$
2. sort  $E$  by  $w(o_i, o_j)$  in descending order
3. while  $|R| < m$   
( $m$  outliers not found yet)
  1. remove the edge  $(o_i, o_j)$  with max. weight  $w(o_i, o_j)$
  2. if  $o_i$  is isolated, insert  $o_i$  into the result  $R$

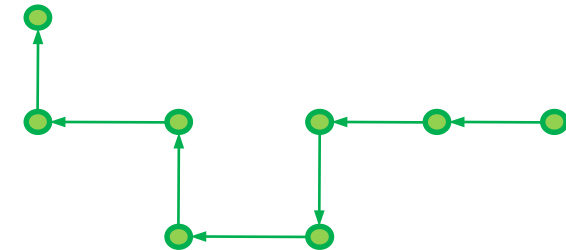


# Example POD



# Trajectories

- trajectories describe a movement through space (time series of spatial positions)
- spatial trajectory:**  $Q=(x_1, \dots, x_l) \in \mathbb{R}^2 \times \dots \times \mathbb{R}^2$  is known as spatial trajectory of length  $l$  over  $\mathbb{R}^2$ .
- spatial-temporal trajectory:** Let  $T$  be a domain to present time, then  $Q=((x_1, t_1), \dots, (x_l, t_l)) \in (\mathbb{R}^2 \times T) \times \dots \times (\mathbb{R}^2 \times T)$  is a spatial-temporal trajectory of length  $l$  over  $\mathbb{R}^2$ .
- alternatively trajectories can be described relatively to a starting position.
- movement is continuous: to get a continuous path, the movement between two positions is assumed to be linear and to be traversed with constant speed.



go , go, turn left, go, turn  
right, go, turn right, go,  
turn left, go, turn right,  
go

# Distance Measure for Trajectories

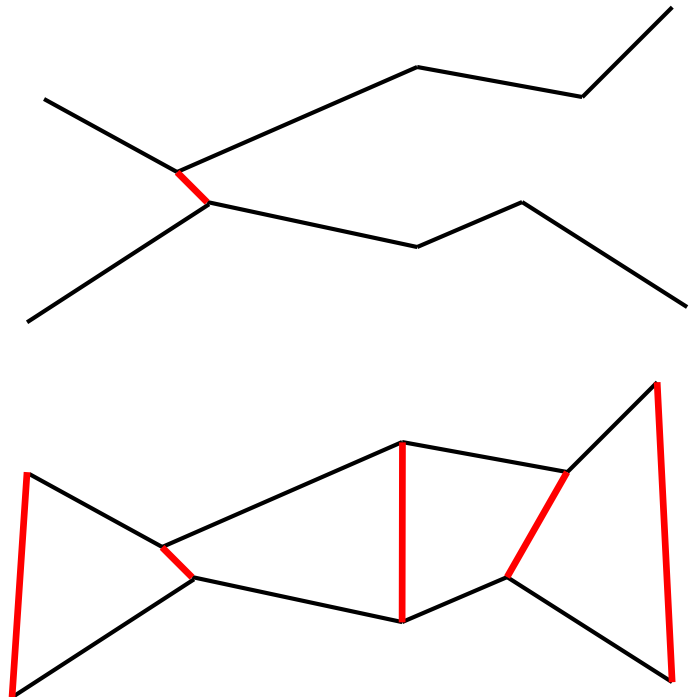
- **point to trajectory:** Given  $p \in \mathbb{R}^2$  and trajectory  $Q = ((x_1, t_1), \dots, (x_l, t_l))$ :  
$$D(p, Q) = \min_{(x, t) \in Q} d(p, x)$$
- **trajectory to trajectory:** Given  $Q = ((x_1, t_1), \dots, (x_l, t_l))$  and  $P = ((y_1, t'_1), \dots, (y_l, t'_l))$ :

*Closest Pair Distance:*

$$CPD(Q, P) = \min_{(x_i, t_i) \in Q, (y_j, t'_j) \in P} d(x_i, y_j)$$

*Sum-of-Pairs:*

$$SPD(Q, P) = \sum_{i=1}^n d(x_i, y_i)$$

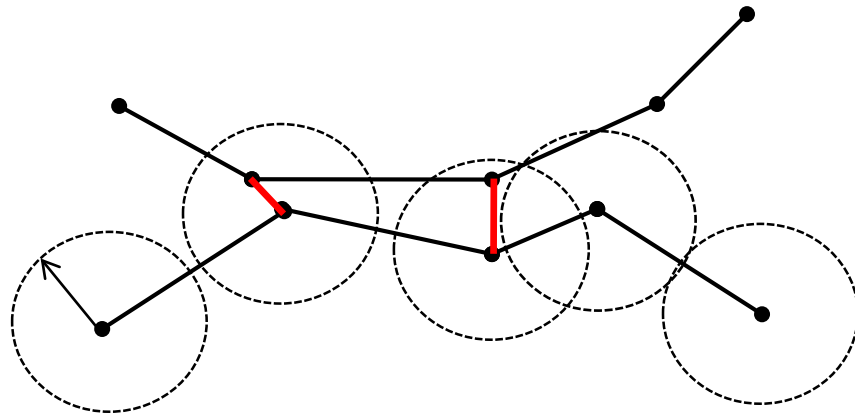


# Distance Measures for Trajectories

- for different lengths: DTW (See Chapter 8)  
but: DTW is susceptible to outliers.
- longest common sub-sequence (similarity measure!)  
LCSS (Longest Common Sub-Sequence):

$$LCSS(Q, P) = \begin{cases} 0, & \text{falls } n = 0 \vee m = 0 \\ 1 + LCSS(\text{Rest}(Q), \text{Rest}(P)), & \text{falls } d(\text{Head}(Q), \text{Head}(P)) \leq \varepsilon \wedge |n - m| < \delta \\ \max(LCSS(\text{Rest}(Q), P), LCSS(Q, \text{Rest}(P))), & \text{sonst} \end{cases}$$

- $\varepsilon$  : threshold for position matching,  $\delta$  max. shift
- calculation by recursion





# LCSS Similarity

- LCSS(P,Q) only counts the length of the longest common subsequence up to now, but is not normalized yet:

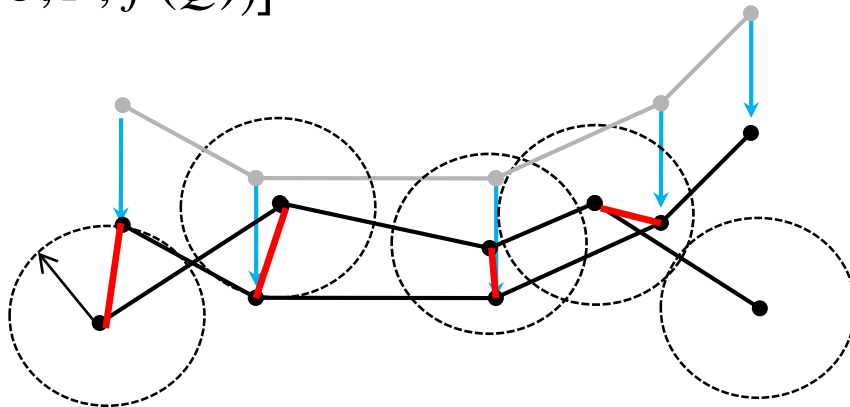
$$S1(\delta, \varepsilon, P, Q) = \frac{LCSS(P, Q)}{\min(|P|, |Q|)}$$

- similarity does not yet take the translation of trajectories into account

(translation: Shifting all positions by a fixed vector):

Let  $F$  be the set of all translations and  $f(Q)$   $F$  one translation:

$$S2(\delta, \varepsilon, P, Q) = \max_{f \in F} [S1(\delta, \varepsilon, P, f(Q))]$$



# Compressing trajectories

---

characteristics of trajectories in games:

- high resolution (ca. 20-30 points/s)
- no measuring errors for positions
- velocity gradation is usually steady and movement is often linear.

problems: resolution is often too high and redundant

- extremely high memory requirement
- comparisons become very expensive  
(e.g., all DTW based measures are square)

spproach: reduce waypoints

⇒ compression by omitting waypoints

⇒ good methods minimize approximation errors

# Douglas-Peucker Algorithm

**Given:** A trajectory  $Q=((x_1, t_1), \dots, (x_l, t_l))$  of  $l$  length.

**Searched:**  $Q'$  with  $|Q'| \ll l$  and approximation error smaller than  $\delta$ .

**Algorithm:**

$DP(Q, \delta)$

$Q' = ((x_1, t_1), (x_l, t_l))$

FOR ALL  $(x_i, t_i)$  in  $Q$

IF  $Error(x_i, Q') > \delta$  THEN

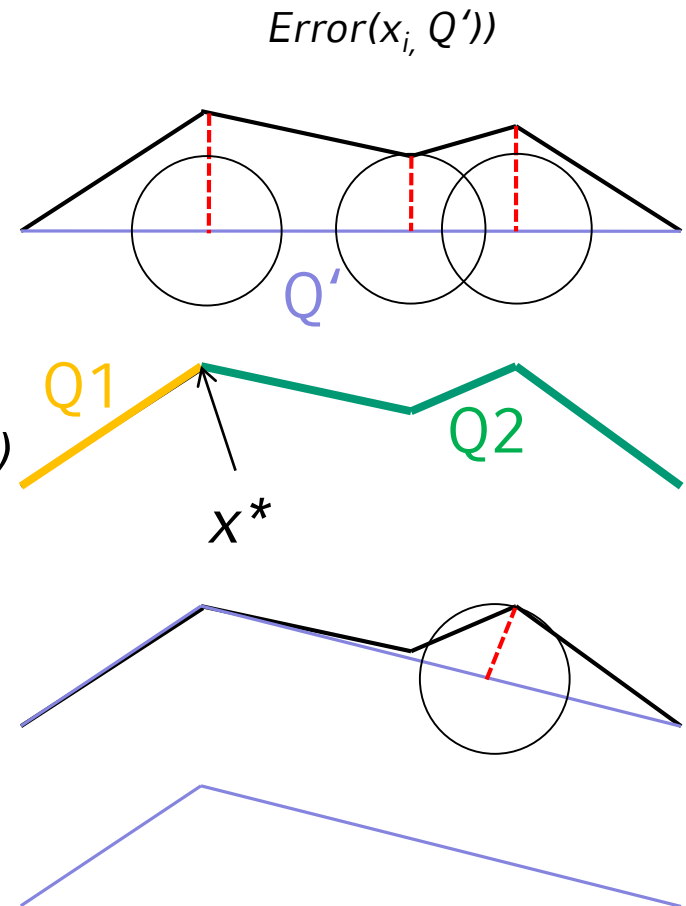
determine  $x^*$  with  $\max(Error(x_i, Q'))$

$(Q1, Q2) = split(Q, x^*)$

RETURN  $DP(Q1, \delta) \cup DP(Q2, \delta)$

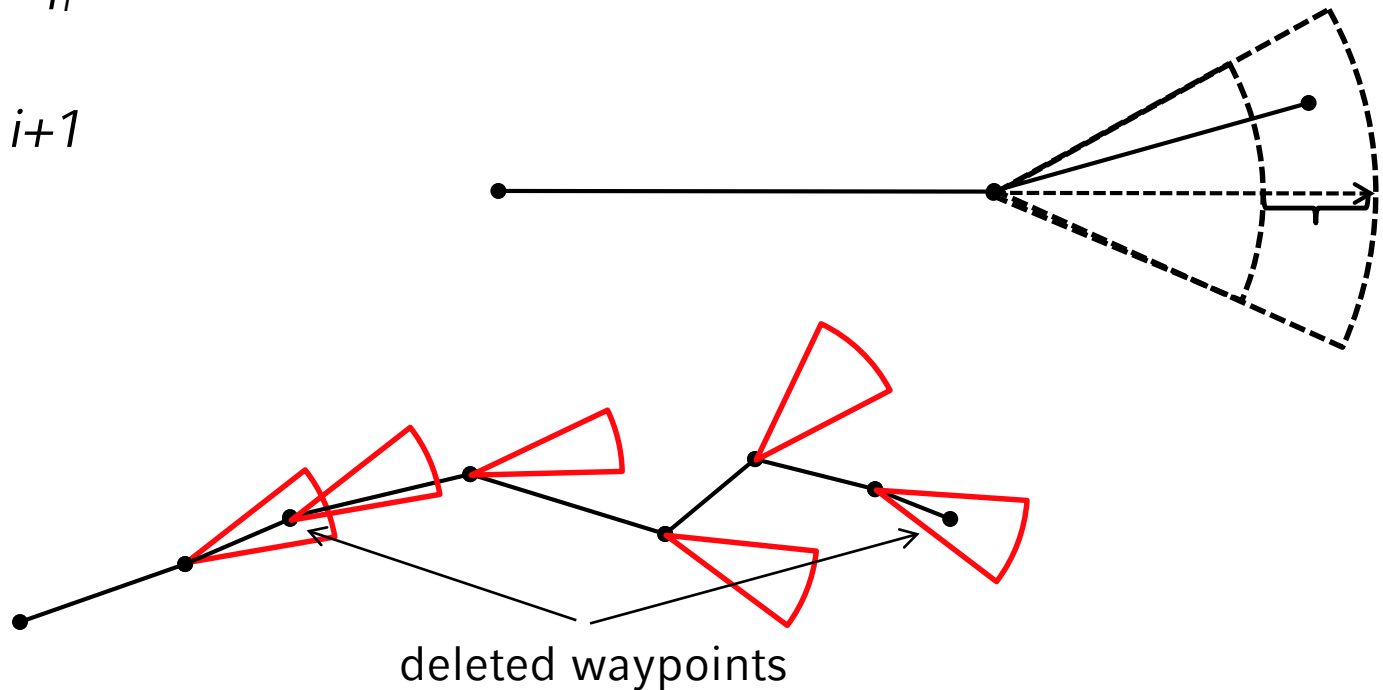
ENDFOR

RETURN  $Q'$



# Compressing with Speed and Direction

- Consider last 2 waypoints  $q_{i-2}, q_{i-1}$  and calculate movement direction  $d_i = \frac{q_{i-2} - q_{i-1}}{\|q_{i-2} - q_{i-1}\|}$  and speed  $v_i = \frac{\|q_{i-2} - q_{i-1}\|}{t_{i-2} - t_{i-1}}$
- extrapolate next waypoint  $q_{i-1} + d_i v_i (t_{i+1} - t_i)$  and test:  
 If  $|v_i(t_i - t_{i-1}) - (q_i - q_{i-1})|$  and  $\frac{\langle d_i, q_i - q_{i-1} \rangle}{\|d_i\| \cdot \|q_i - q_{i-1}\|} \leq \alpha$   
 delete  $q_i$   
 else  
 go to  $i+1$



# Pattern Search in Trajectories

---

- like other objects, trajectories can be analyzed with distance based data mining (z.B. OPTICs) and corresponding distance measures (LCSS).
- but resulting patterns consist of globally similar trajectories.
- many interesting trajectory patterns rest on a relative small part of the trajectory.
- interesting patterns usually have spatial constraints.

=> special pattern search methods for trajectories

# Continuous Flocks

**Idea:** Find objects that share a path for a certain time interval.

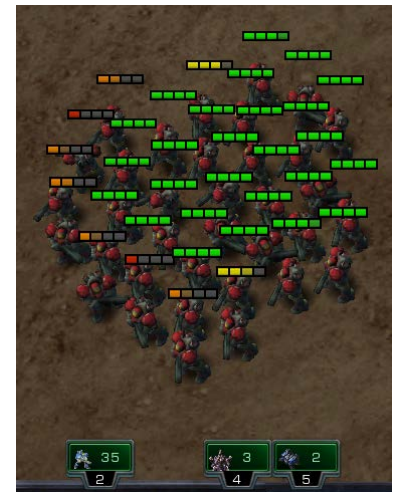
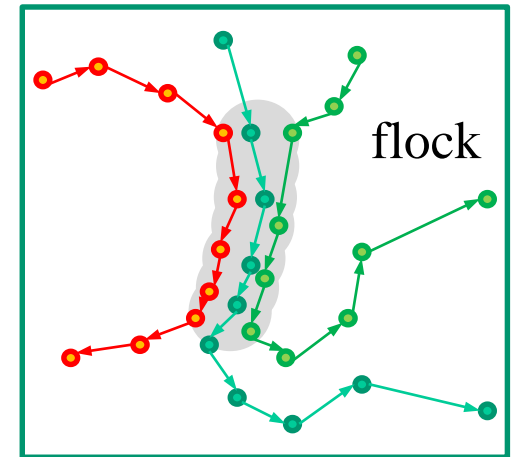
**Example:** subteams in games, convoys,...

**Definition:** Continuous  $(m,k,r)$ -Flock

Let  $DB$  be a set of trajectories of length  $l$ , a Flock within the time interval  $l=[t_i, t_j]$  where  $j-i+1 \geq k$  consists of at least  $m$  objects, so that a disc with radius  $r$ , enclosing all  $m$  objects, exists in  $l$ .

**Remark:** Calculating the flock with the longest duration and the flock with the largest subset are NP-hard problems.

=> solutions are complex or only approximate



# Flocks with discreet Time

---

**Definition:** *discreet*  $(m,k,r)$ -Flock

Let  $DB$  be a set of trajectories of  $l$  length, a Flock in  $l=[t_i, t_j]$  with  $j-i+1 \geq k$  consists of at least  $m$  objects, so that a disc with radius  $r$ , enclosing all  $m$  objects, exists for each discrete time  $t_l$  where  $i \leq l \leq j$ .

- **Lemma:** If objects move with constant speed and on a direct line between waypoints, discrete and continuous flocks are equivalent.
- **Advantage:** Turning a continuous problem to a discrete one.  
**But:** Complexity remains unchanged and comes from the combination of possible subsets.

The possible number of flocks with  $m$  elements is:  $\binom{|DB|}{m} \cdot (l - k + 1)$

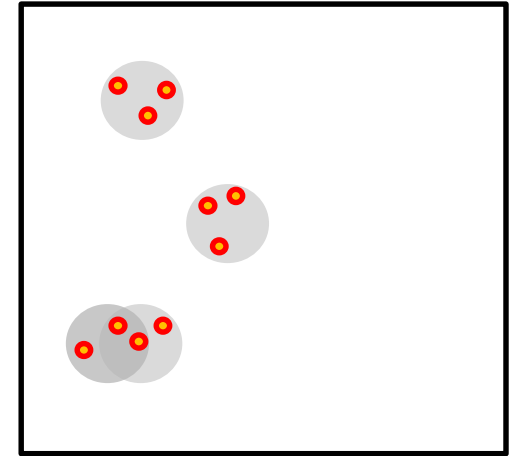
# Searching for Flocks

**Procedure encompasses 2 subtasks:**

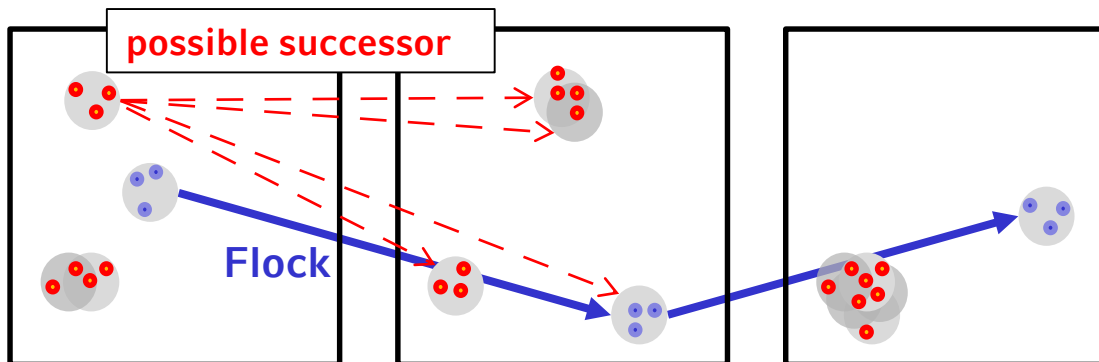
1. Find all discs of radius  $r$ , containing at least  $m$  points for time  $t_i$ .

=> sequence of subsets of DB

=> one trajectory may be present in several subsets.



2. Find sequence  $(S(t_i), \dots, S(t_j))$  of discs  $S(t_l)$  for the points in time  $t_l$  with  $i \leq l \leq j$  for which the following condition holds:  $\left| \bigcap_{i \leq l \leq j} S(t_l) \right| \geq m$





# Find all Discs for the Point in Time $t$

**Discs( $t_i$ )**

build grid index  $I$  for  $DB_i$

**FOR ALL** non-empty cells  $gx \in I$  **DO**

$Pr = gx$

$Ps = \text{NeighborCells}(gx)$

**IF**  $|Ps| \geq m$  **THEN**

**FOR EACH**  $pr \in Pr$  **DO**

$H = \text{Range}(pr, 2r)$

**FOR each**  $pj \in H$  **DO**

**IF** not computed  $\{pr, pj\}$  **THEN**

compute disks  $\{c1, c2\}$  from  $\{pr, pj\}$

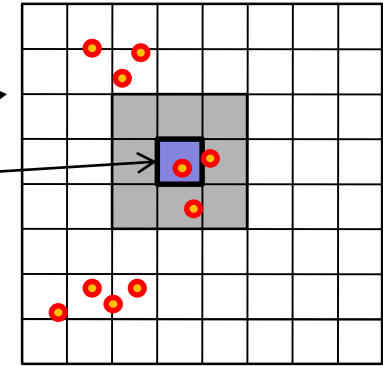
**FOR EACH** disk  $ck \in \{c1, c2\}$  **DO**

$c = ck \cap H$

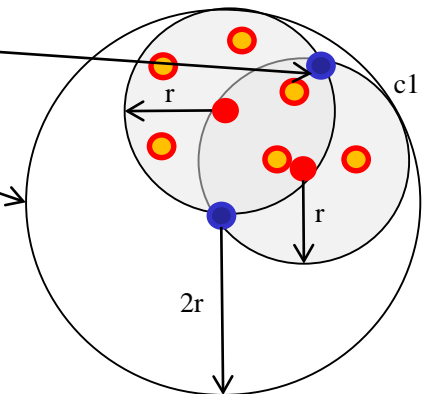
**IF**  $|c| \geq m$  **THEN**

$C.add(c)$

**RETURN**  $C$



$c2$



# Finding (m,k,r)-Flocks

## Continuous Refinement Evaluation (CRE)

### CRE(DB,k)

**FOR EACH** point in time  $t_i$  **DO**

  L: Trajectories in time interval  $t_{i-k}$  to  $t_i$

$C^1 = \text{Disks}(L[t_{i-k}])$  // all containing trajectories in L at  $t_{i-k}$

$F = \{\}$  // results flocks

**FOR EACH**  $c1 \in C^1$  **DO** // for each start disc

$L'[1] = \text{trajectories in } c1$

$F^1 = c1, F^t = \{\}$

**FOR**  $t = 2$  **to**  $k$  **DO** // for the next k-1 times

$C^t = \text{Disks}(L'[t])$

$F^t = \{\}$

**FOR EACH**  $c \in C^t$  **DO** // for all disc at time t

**FOR EACH**  $f \in F^{t-1}$  **DO** // for currently valid flocks

**IF**  $|c \cap f| \geq m$  **THEN**

$F^t = F^t \cup \{c \cap f\}$  // extend the flock by one point in time

**IF**  $|F^t| = 0$  **THEN**

**BREAK**

$F = F \cup F^t$

**RETURN**  $F$

# Meets (Encounter)

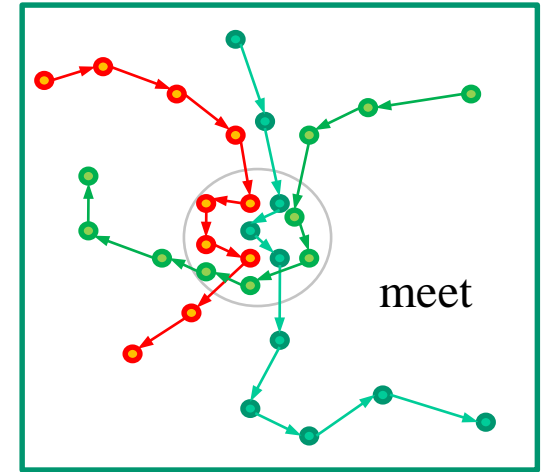
**Idea:** Find objects that stay together in an area for a certain time.

**Examples:** Encounter, Combat.

**Definition:**  $(m,k,r)$ -Meet

Let  $DB$  be a set of trajectories of length  $l$ , a meet within the time interval  $I=[t_i, t_j]$  with  $j-i+1 \geq k$  consists of at least  $m$  objects, so that for every point in time  $t_i \in I$  all  $m$  objects lie within a disc of radius  $r$  and center point  $M$ .

**Remarks:** Calculating meets is easier than calculating flocks because for two consecutive points in time only the discs positions, not their trajectories, must be analyzed.



# Encounter Detection

---

**Idea:** To find out where a team succeeded /failed and find the decisive moments in a game.

- in Dota2 defeating enemy heroes grants the biggest advantage in gold/XP
- find situations where this was possible or succeeded  
=> Encounters

## Encounter characteristics

- encounters represent only a portion of the game
- encounters can happen simultaneously
- often only sub teams are involved in encounters

# Defining Encounters

---

**Idea:** Fights happen when opponents can influence each other.

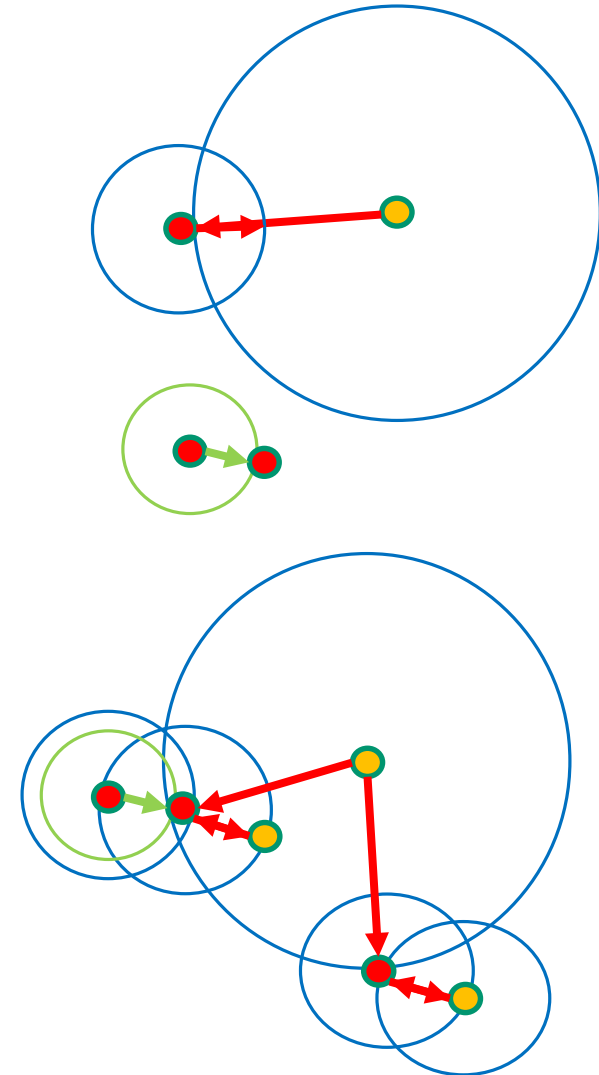
- opponents have to be in fighting range
- each hero unit might have an individual attack range
- heroes can support (e.g. heal) a friendly unit

***Which kind of information is necessary?***

- Spatial position and unit type for each controlled hero unit
- Attack and support ranges for all units types

# Encounter Situations

- **Combat link:** 2 hero units from different teams A and B. Either A can attack B or vice versa
- **Support link:** 2 hero units from the same team A and B. Either A can support B or vice versa
- Each hero type has individual **attack and support ranges** (Ranges are mean values plus to standard deviations)
- **Component Graph:** Connected Graph build by Combat/support Links



# Encounter Situations

---

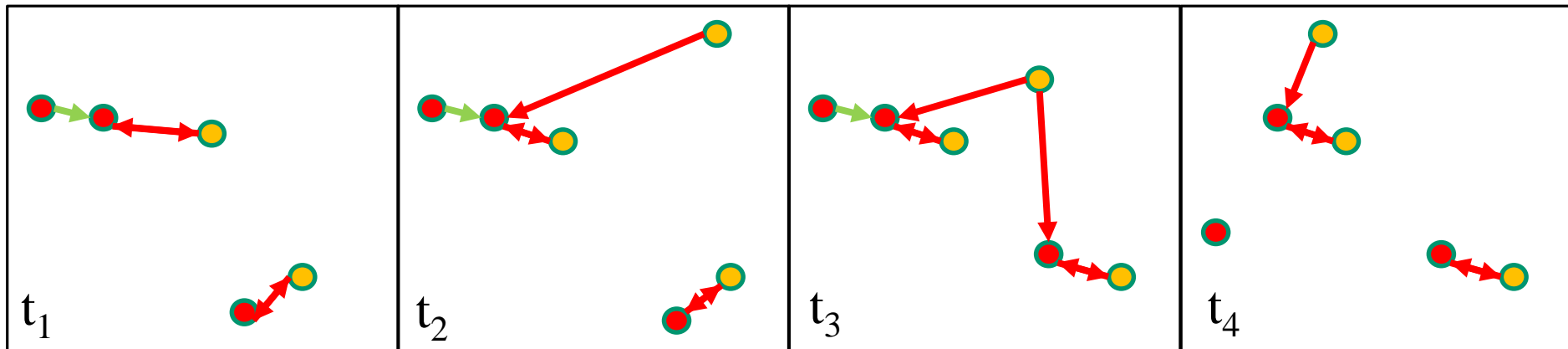
Formally...

## Definition: Combat Component

- units  $U$  and the union  $E_d = CL \cup SL$  of combat links  $CL$  and support links  $SL$  between the units in  $U$ .
- $E_u = \{(u_i, u_j) \mid (u_i, u_j) \in E_d \vee (u_j, u_i) \in E_d\}$
- situation graph  $G(U, E_u)$ .
- combat component  $C$ : connected subgraph  $G(\bar{U}, \bar{E})$  of  $G(U, E_u)$  where  $\bar{U} \subseteq U, \bar{E} \subseteq \bar{U} \times \bar{U}$   
and  $\forall u_1, u_l \in \bar{U}: \exists (u_1, u_2, \dots, u_l)$   
where  $i \in \{1, \dots, l\}: (u_i, u_{i+1}) \in \bar{E}$   
and  $\exists u_i, u_j \in \bar{U}: u_1.team \neq u_2.team$ .

# Defining Encounters

- Component Graphs describe an Encounter at tick  $t$
- An encounter usually lasts multiple consecutive ticks
- Hero Units can join encounters
- Hero Units might be defeated or leave
- Encounters can split
- Encounters can join





# Defining Encounters

---

Formally...

## Definition: Successor

Given a set of components  $CS_t = \{ C_{1,t}, \dots, C_{l,t} \}$  describing encounter  $E$  at tick  $t$ . Let  $\tau$  be a timeout threshold. A component  $C_{t+\Delta t}$  is a successor of  $CS_t$  denoted as  $CS_t \rightarrow C_{t+\Delta t}$  if the following conditions hold:

- $\Delta t \leq \tau$
- $\exists u_1, u_2 \in C_{t+\Delta t} : \exists C_{i,t} \in CS_t : u_1 \in C_{i,t} \wedge C_{j,t} \in CS_t : u_2 \in C_{j,t} \wedge u_1.team \neq u_2.team$

# Defining Encounters

---

Formally....

## **Definition: Encounter**

An encounter is a sequence  $(CS_0, \dots, CS_l)$  of lists of components  $CS_i$  where the following condition holds:  
 $\forall C_{i,t} \in CS_t: CS_{t-1} \rightarrow C_{i,t}$  with  $t \in \{1, \dots, l\}$ .

# Encounter Detection

---

## *What is the input data ?*

- hero type (combat range, support range), team
- time series of position updates (one at a time)

## *Algorithm:*

- initialize hero information
- stream over position updates and update distances
- for each player movement process the impact to the current component graphs
- keep lists of open encounters
- move encounters to a closed set if they time out

# The Algorithm

---

**Encounter Detection (position\_stream)**

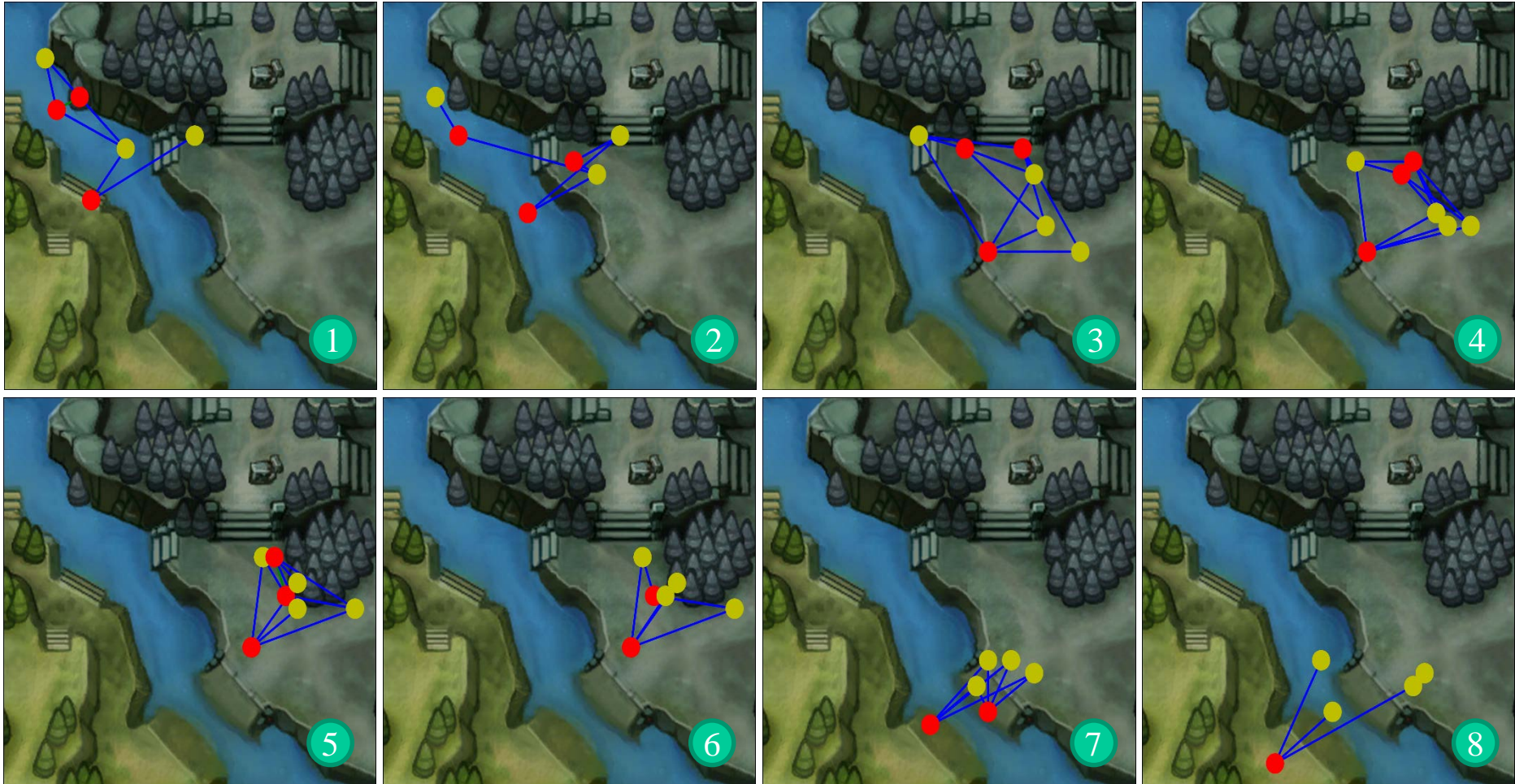
```
While position_stream.hasNext():  
    component = build_component(unit,distance_table)  
    If component is combat component:  
        compute predecessors(component, open_encounters)  
        If predecessors.size() == 0:  
            open_encounters.add(new Encounter(component))  
        If predecessors.size() == 1:  
            predecessors.get(1).update(component)  
        If predecessors.size() >1:  
            open_encounters.join(predecessors,component)  
        For encounter in open_encouters:  
            If encounter has timeout:  
                move encounter from open_encounter to closed_encounters  
For encounter in open_encouters:  
    move encounter from open_encounter to closed_encounters  
return closed_encounters
```

# An Example Encounter

---



# An Example Encounter (Detailed View)



# Learning Goals

---

- use cases for spatial game analytics
- heat maps with bin counting and kernel density estimation
- tasks of spatial data mining
- spatial outlier detection with POD
- trajectories, relative and absolute trajectories
- comparing trajectories (LCSS)
- compressing trajectories
- pattern search in trajectories
  - definition of flocks
  - calculation of flocks
  - definition of meets
  - encounter detection

# Literature

---

- Marcos R. Vieira, Petko Bakalov, and Vassilis J. Tsotras. 2009. **On-line discovery of flock patterns in spatio-temporal data**. In *Proc of the 17<sup>th</sup> ACM SIGSPATIAL Int. Conf. on Advances in Geographic Information Systems (GIS '09)*. ACM, New York, NY, USA, 286-295.
- Yu Zheng, Xiaofang Zhou: **Computing with Spatial Trajectories**, Springer, 2011.
- Marc Benkert, Joachim Gudmundsson, Florian Hübner, and Thomas Wolle. **Reporting flock patterns**. *Comput. Geom. Theory Appl.* 41, 3 (November 2008), 111-125.
- Anders Drachen, Alessandro Canossa : **Evaluating Motion: Spatial User Behavior in Virtual Environments** International Journal of Arts and Technology, 4(3): 1--21, 2011.
- H.K. Pao, K.T. Chen, H.C. Chang: **Game Bot Detection via Avatar Trajectory Analysis** Computational Intelligence and AI in Games, IEEE Transactions on, 2(3): 162--175, 2010.
- Jehn-Ruey Jiang, Ching-Chuan Huang, Chung-Hsien Tsai: **Avatar Path Clustering in Networked Virtual Environments** In Proceedings of the 2010 IEEE 16<sup>th</sup> International Conference on Parallel and Distributed Systems, 2010.
- Yufeng Kou, Chang-Tien Lu, Raimundo F. Dos Santos: **Spatial Outlier Detection: A Graph-Based Approach**, 19th IEEE International Conference on Tools with Artificial Intelligence , pp. 281-288, Vol.1 (ICTAI 2007), 2007.
- Shekhar, Shashi and Schrater, Paul and Vatsavai, Ranga Raju and Wu, Wei Li and Chawla, Sanjay. **Spatial Contextual Classification and Prediction Models for Mining Geospatial Data**. *IEEE Transactions on Multimedia*. 4(2):174-188, 2002.
- Matthias Schubert, Anders Drachen, Tobias Mahlmann (2016). **E-Sports Analytics through Encounter Detection**. 10th Sloan Sports Analytics Conference