

**Machine Learning and Data Mining**  
Summer 2014  
**Exercise Sheet 3**

*Presentation of Solutions to the Exercise Sheet on the 15.05.2014*

**Aufgabe 3-1**    PCA

- a) Please describe what a PCA aims for and under what circumstances it is most helpful.
- b) Which possibly negativ consequences might arise when applying PCA to a dataset of unknown structure?

**Aufgabe 3-2**    PCA

Consider the  $\mathbf{X} \in \mathbb{R}^{M \times N}$  matrix containing six data points  $\mathbf{x}_i \in \mathbb{R}^2$ . Note that in contrast to the conventional representation, the patterns are held in columns here.

dim 1	1	2	3	5	6	7
dim 2	0	0	0	6	6	6

Conduct a PCA on the given data. Please state the eigenvectors, eigenvalues, covariance matrix and visualize the data before and after the PCA.

**Aufgabe 3-3**    Eigenfaces

The term *eigenfaces* describes the eigenvectors of a normalized covariance matrix.

- a) Find the eigenfaces of the number dataset from the `numberMatrix.RTable`.
- b) How many principal components are required to reconstruct the dataset? Are the eigenfaces sufficient for this purpose? Are all patterns reconstructable with equal quality?