

**Knowledge Discovery in Databases II**  
 WS 2014/2015

**Übungsblatt 10: Multi-Instance Data**

**Aufgabe 10-1 Distance measures for multi-instance objects**

A multi-instance object  $O_i$  is a set of objects  $o_i$  from a representation space  $R$ , i.e.  $O_i \subseteq R$ .

Given a distance measure  $dist : R \times R \rightarrow \mathbb{R}_0^+$ , consider the following distance measures for multi-instance objects:

**Hausdorff**

$$d_{Hausdorff}(O_1, O_2) = \max \left( \max_{o_i \in O_1} \left( \min_{o_j \in O_2} (dist(o_i, o_j)) \right), \max_{o_i \in O_2} \left( \min_{o_j \in O_1} (dist(o_i, o_j)) \right) \right)$$

**Minimal Hausdorff**

$$d_{MinimalHausdorff}(O_1, O_2) = \min_{o_i \in O_1} \left( \min_{o_j \in O_2} (dist(o_i, o_j)) \right)$$

**Sum of Minimal Distances**

$$d_{SMD}(O_1, O_2) = \frac{1}{2} \left( \frac{1}{|O_1|} \sum_{o_i \in O_1} \left( \min_{o_j \in O_2} (dist(o_i, o_j)) \right) + \frac{1}{|O_2|} \sum_{o_j \in O_2} \left( \min_{o_i \in O_1} (dist(o_i, o_j)) \right) \right)$$

**Minimal Matching Distanz** – w.l.o.g. be  $|O_1| \geq |O_2|$ ,

$\Pi(O_1)$  the set of all permutations of the elements of  $O_1$ ,

$w(o_i, j)$  a penalty term for unmatched distances:

$$d_{MM} = \min_{\pi_i \in \Pi(O_1)} \left( \sum_{k=1}^{|O_2|} dist(O_{1,\pi(k)}, O_{2,k}) + \sum_{l=|O_2|+1}^{|O_1|} w(O_{1,\pi(l)}) \right)$$

Discuss the pros and cons of these distance measures.

Given a distance measure  $dist : S \times S \rightarrow \mathbb{R}_0^+$  and arbitrary objects  $x, y, z \in S$ , consider whether the following properties (which together define a metric) hold:

- (a)  $dist$  is reflexive, iff:  $x = y \Rightarrow dist(x, y) = 0$
- (b)  $dist$  is symmetric, iff:  $dist(x, y) = dist(y, x)$
- (c)  $dist$  is strict, iff:  $dist(x, y) = 0 \Rightarrow x = y$
- (d)  $dist$  satisfies the triangle inequality, iff:  $dist(x, z) \leq dist(x, y) + dist(y, z)$

**Aufgabe 10-2 Hausdorff-Distance**

Show that the Hausdorff distance satisfies all the properties of a metric.

**Aufgabe 10-3 Kuhn-Munkres Algorithm**

Given the following cost matrix  $K$ . Perform Hungarian Matching on the following matrices:

$$K_1 = \begin{pmatrix} 2 & 1 & 3 \\ 6 & 5 & 4 \\ 7 & 8 & 9 \end{pmatrix}$$

$$K_2 = \begin{pmatrix} 90 & 75 & 75 & 80 \\ 35 & 85 & 55 & 65 \\ 125 & 95 & 90 & 105 \\ 45 & 110 & 95 & 115 \end{pmatrix}$$