

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$

Data Mining Tutorial

Clusteranalyse – Teil II

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Ludwig-Maximilians-Universität München

2013-05-10 — KDD Übung

Sei:

- ▶ M_i = Modell (= Menge der Medoide) nach Iteration i .
- ▶ $TD(M_i)$ = Kosten von Modell M_i .

Aufgabe 3-1

Aufgabe 3-2

Beispiel
Berechnung

Aufgabe 3-3

 $\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$

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- ▶ M_i = Modell (= Menge der Medoide) nach Iteration i .
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PAM konvergiert, wenn

$$TD(M_i) = TD(M_{i+1})$$

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 $\text{minPts} = 4$

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$$\forall i \in \mathbb{N} : TD(M_i) > TD(M_{i+1})$$

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Es gibt $\binom{n}{k}$ mögliche Modelle, aber \mathbb{N} Iterationen.

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$$\Rightarrow \exists_{t_1 < t_2} M_{t_1} = M_{t_2}$$

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PAM konvergiert nicht, wenn

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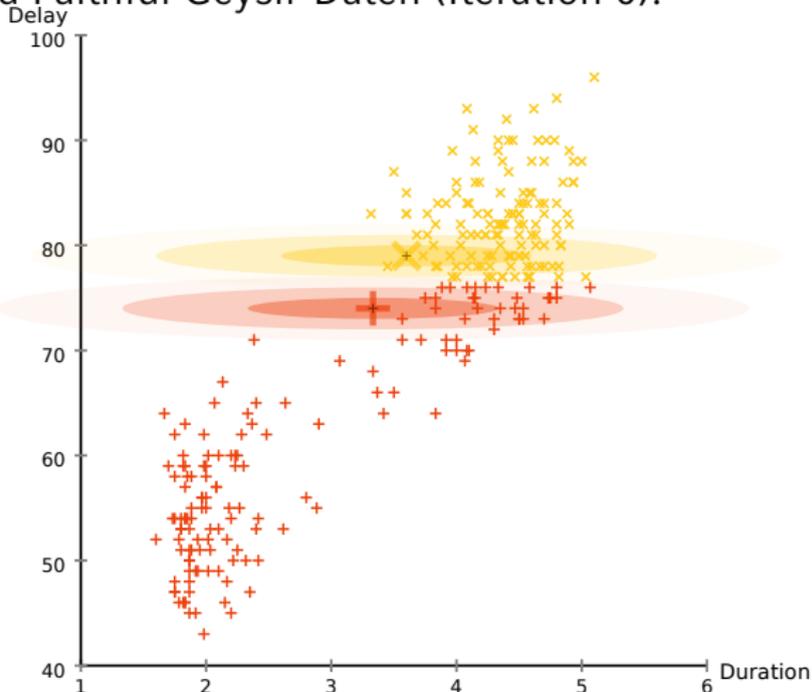
Es gibt $\binom{n}{k}$ mögliche Modelle, aber \mathbb{N} Iterationen.

$$\Rightarrow \exists_{t_1 < t_2} M_{t_1} = M_{t_2}$$

$$\Rightarrow TD(M_{t_1}) = TD(M_{t_2}) \quad \text{Widerspruch!}$$

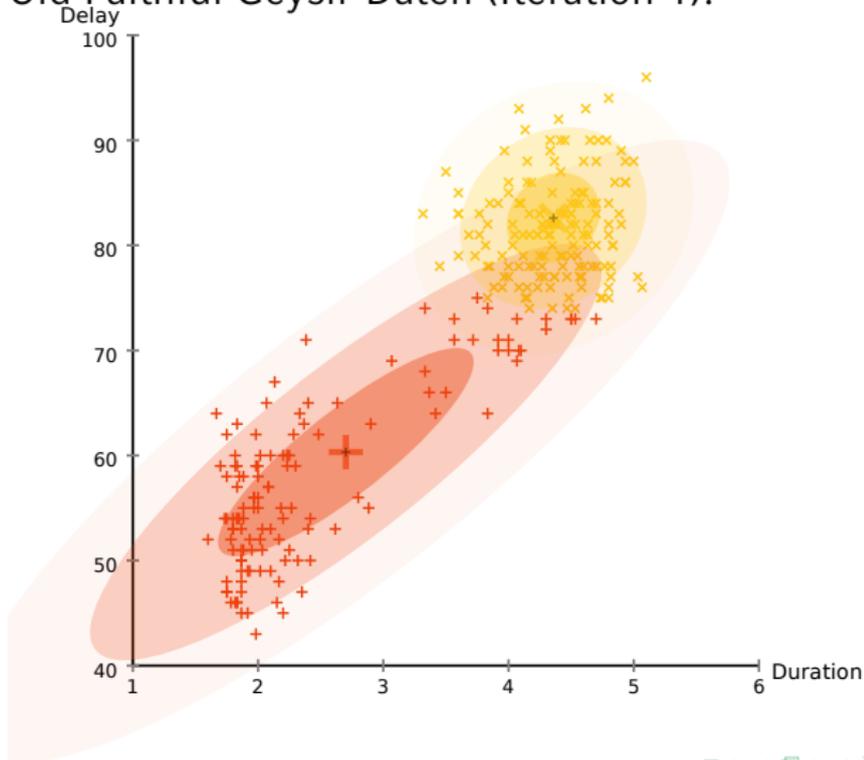
$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

Old Faithful Geysir Daten (Iteration 0):



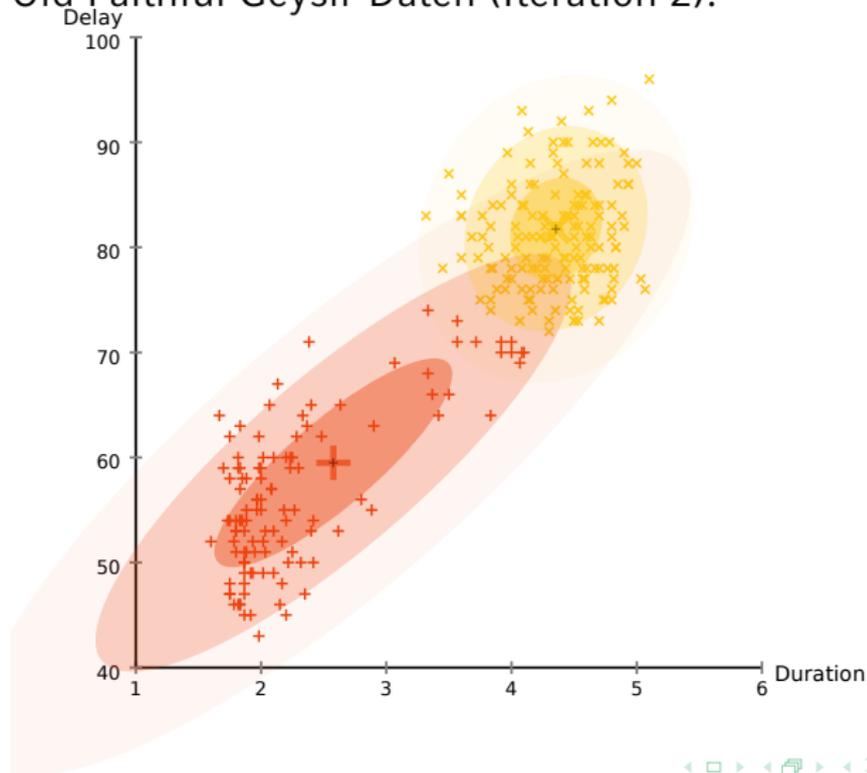
$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

Old Faithful Geysir Daten (Iteration 1):



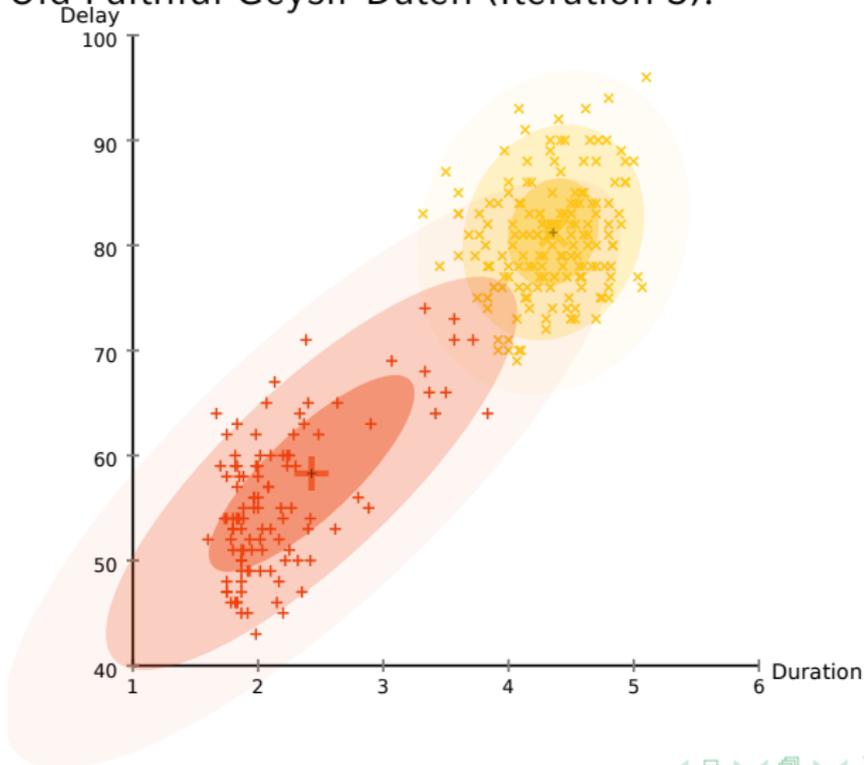
$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

Old Faithful Geysir Daten (Iteration 2):



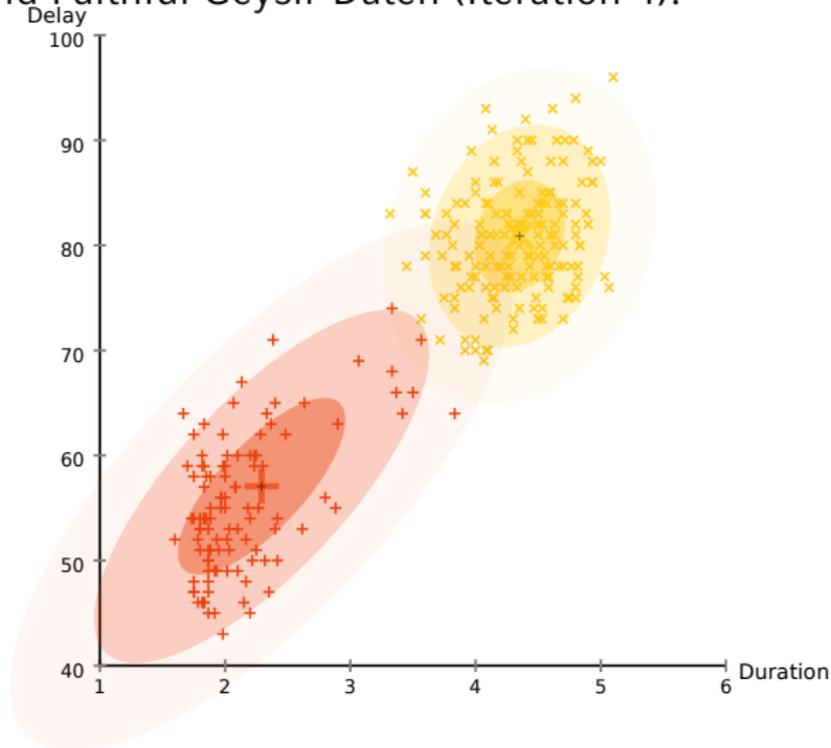
$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

Old Faithful Geysir Daten (Iteration 3):



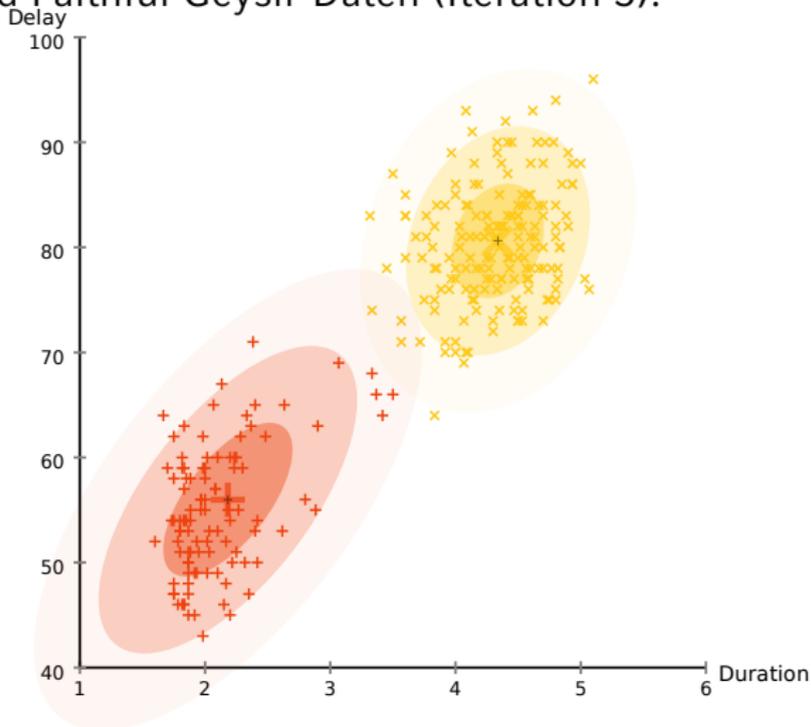
$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

Old Faithful Geysir Daten (Iteration 4):



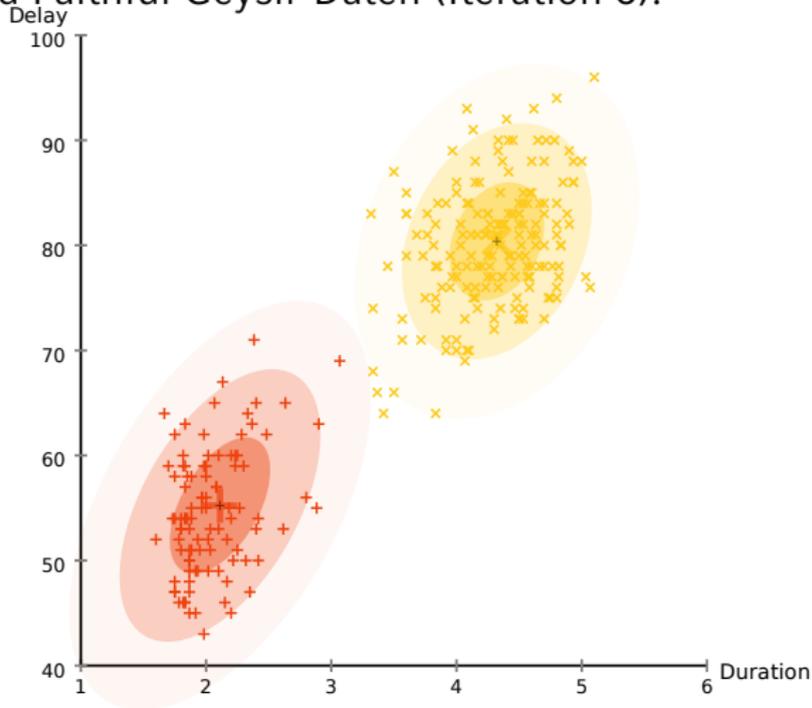
$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

Old Faithful Geysir Daten (Iteration 5):



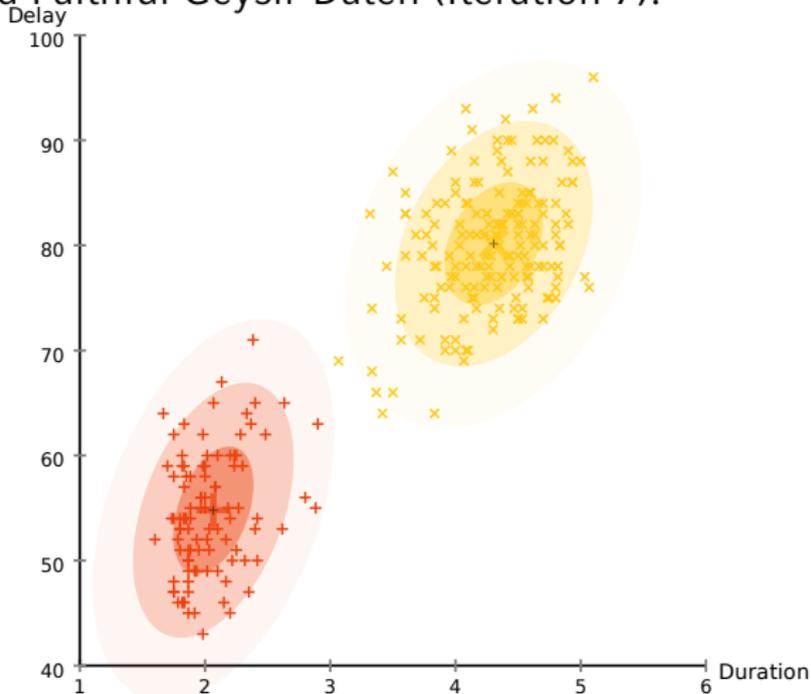
$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$

Old Faithful Geysir Daten (Iteration 6):



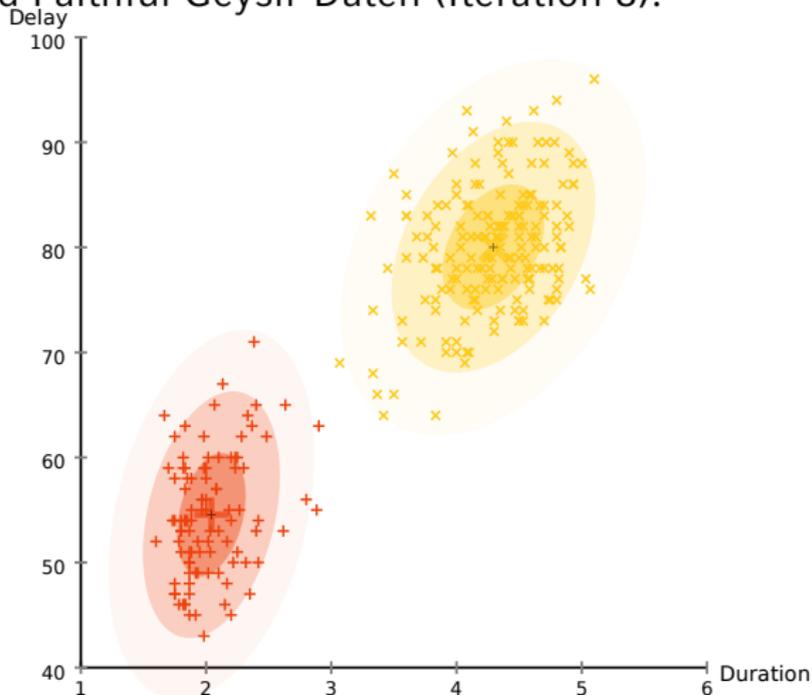
$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$

Old Faithful Geysir Daten (Iteration 7):



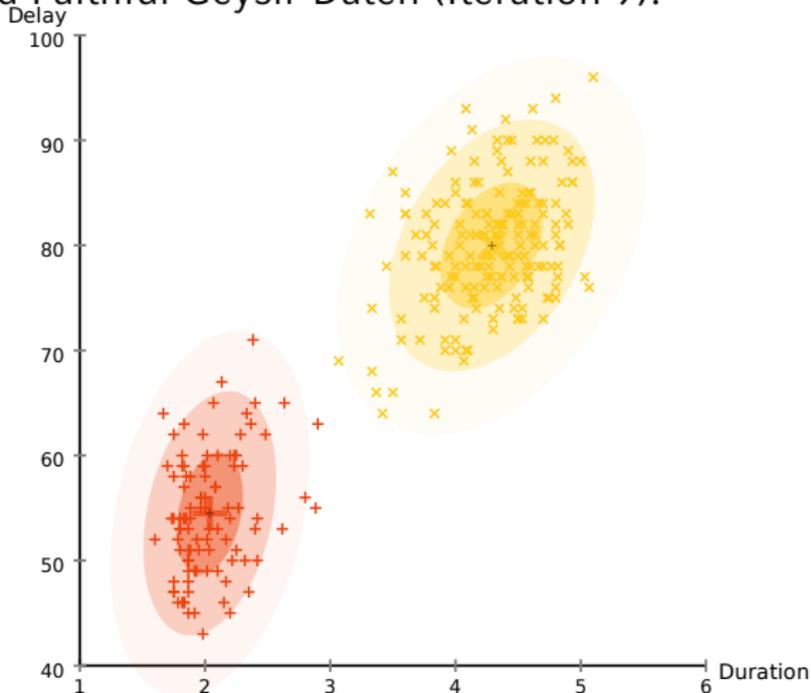
$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$

Old Faithful Geysir Daten (Iteration 8):



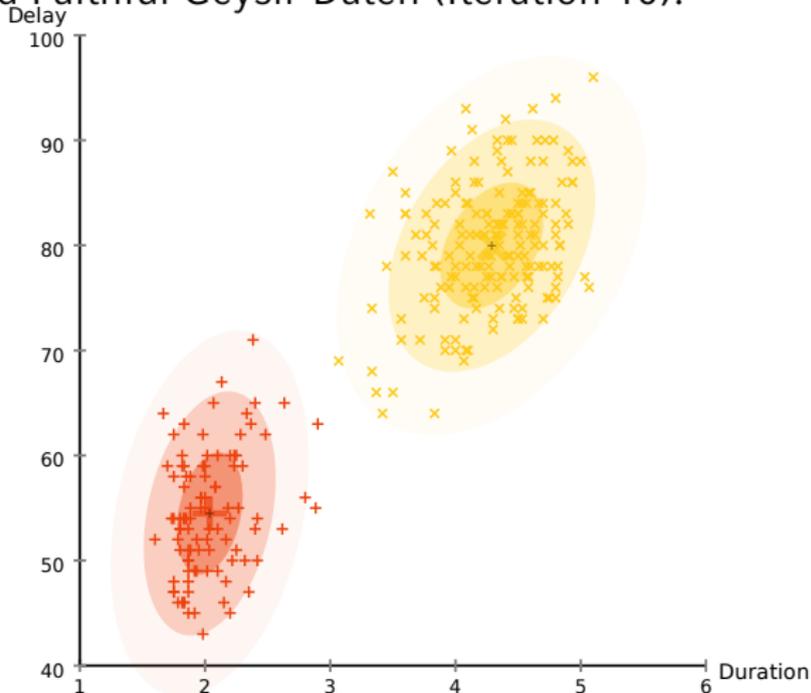
$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

Old Faithful Geysir Daten (Iteration 9):



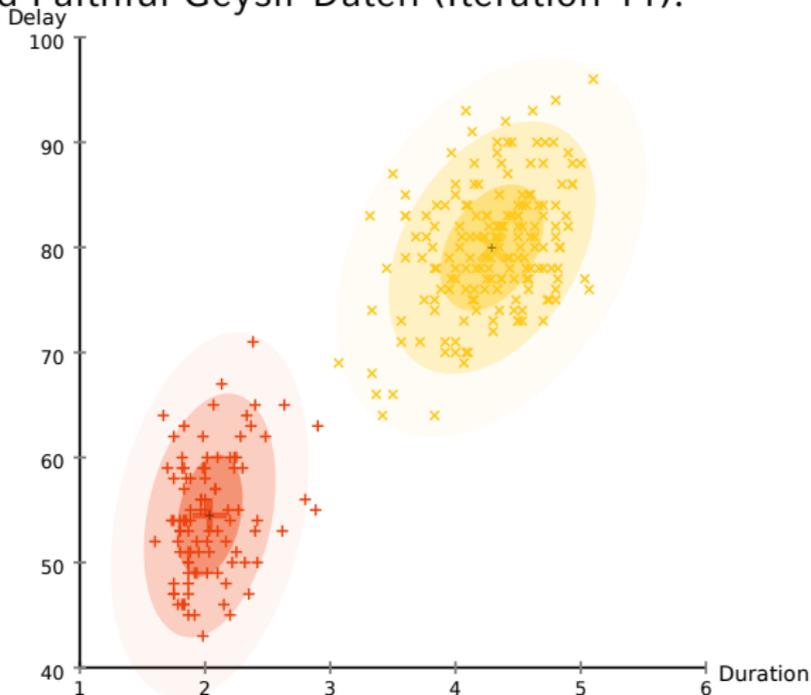
$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

Old Faithful Geysir Daten (Iteration 10):



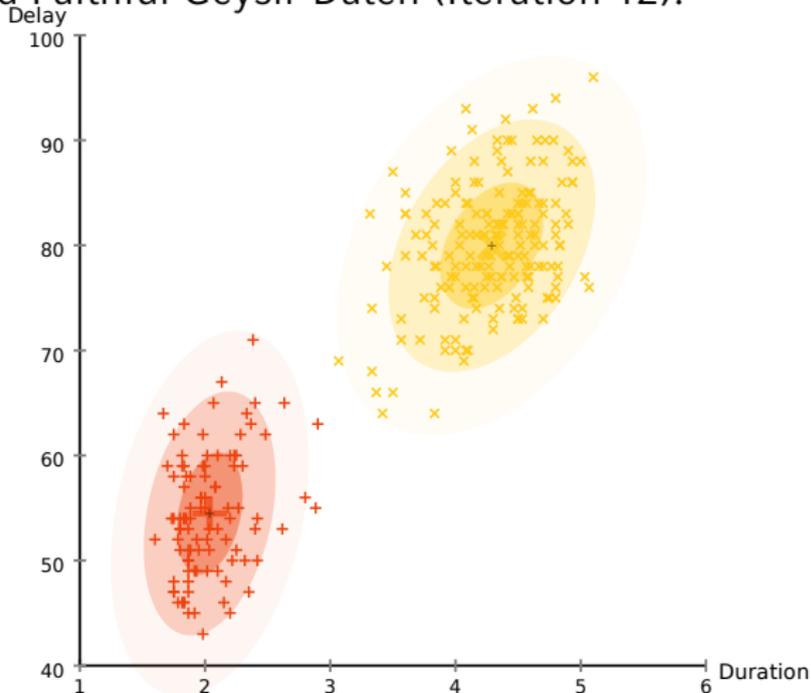
$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

Old Faithful Geysir Daten (Iteration 11):



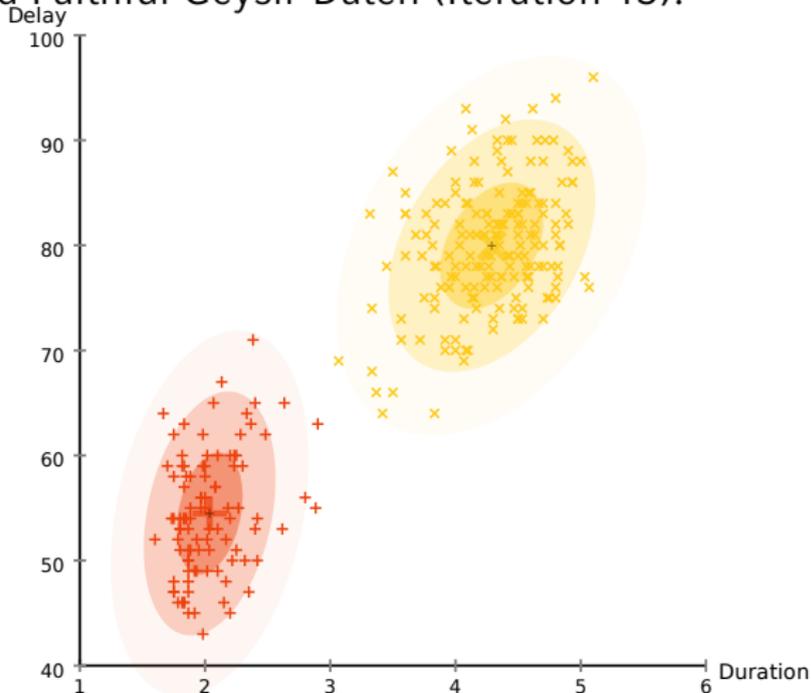
$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

Old Faithful Geysir Daten (Iteration 12):



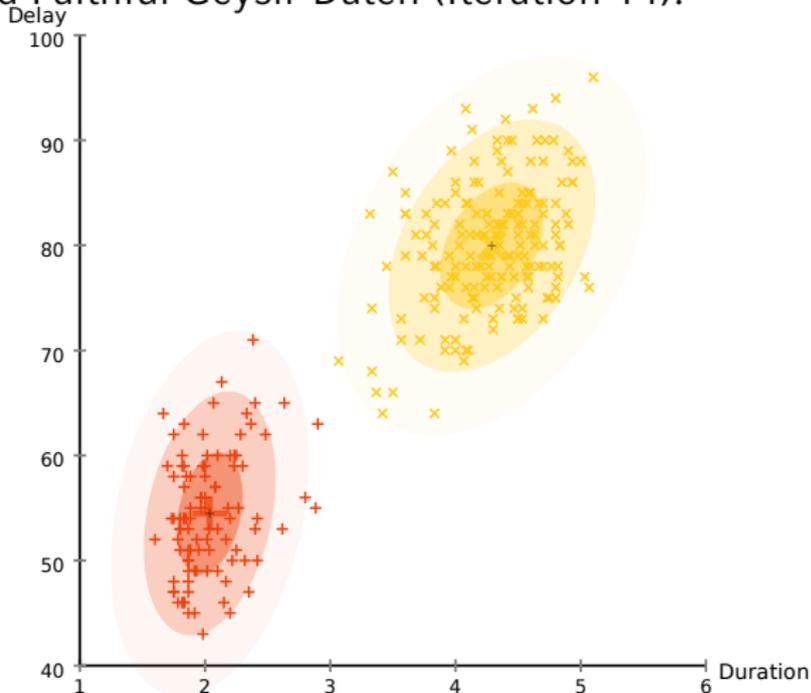
$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

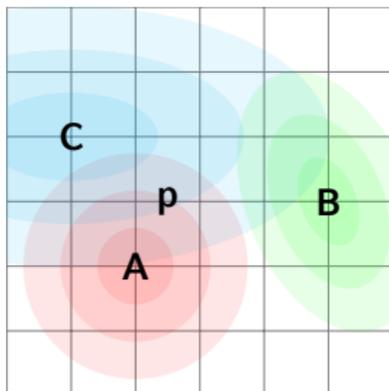
Old Faithful Geysir Daten (Iteration 13):



$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

Old Faithful Geysir Daten (Iteration 14):



$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

$\epsilon = 1.1$
minPts = 2

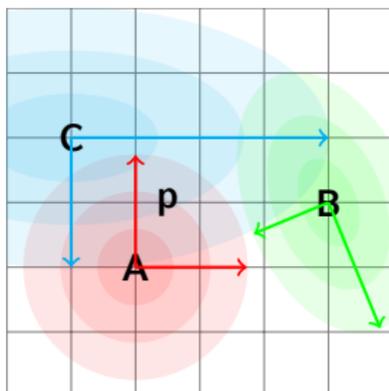
$\epsilon = 1.1$
minPts = 3

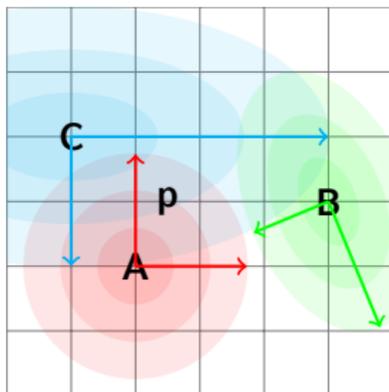
$\epsilon = 1.1$
minPts = 4

$\epsilon = 2.1$
minPts = 4

$\epsilon = 4.1$
minPts = 5

$\epsilon = 4.1$
minPts = 4



$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

$$\Sigma_A = \begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix} \quad \Sigma_A^{-1} = \begin{pmatrix} \frac{1}{3} & 0 \\ 0 & \frac{1}{3} \end{pmatrix}$$

$\epsilon = 1.1$

minPts = 2

 $\epsilon = 1.1$

minPts = 3

 $\epsilon = 1.1$

minPts = 4

 $\epsilon = 2.1$

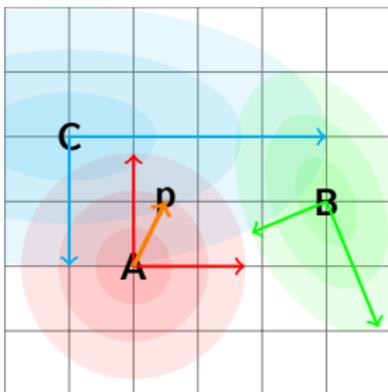
minPts = 4

 $\epsilon = 4.1$

minPts = 5

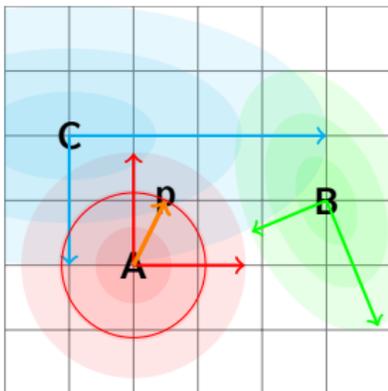
 $\epsilon = 4.1$

minPts = 4



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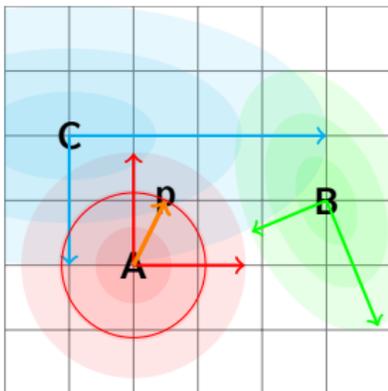
$$p - \mu_A = (0.5, 1)$$

$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
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$$p - \mu_A = (0.5, 1)$$

$$\text{dist}^2 = (p - \mu)^T \Sigma^{-1} (p - \mu) \approx 0.41666$$

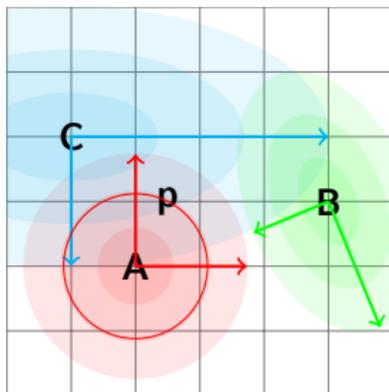
$\epsilon = 1.1$
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minPts = 4 $\epsilon = 2.1$
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$$p - \mu_A = (0.5, 1)$$

$$\text{dist}^2 = (p - \mu)^T \Sigma^{-1} (p - \mu) \approx 0.41666$$

$$\begin{aligned} \text{prob}_A &\approx \frac{1}{\sqrt{(2\pi)^2 \cdot 9}} e^{-\frac{1}{2} \cdot 0.41666} \\ &\approx 0.04307456 \end{aligned}$$

$\epsilon = 1.1$
minPts= 2 $\epsilon = 1.1$
minPts= 3 $\epsilon = 1.1$
minPts= 4 $\epsilon = 2.1$
minPts= 4 $\epsilon = 4.1$
minPts= 5 $\epsilon = 4.1$
minPts= 4

$$\Sigma_B^{-1} \approx \begin{pmatrix} 0.571428 & -0.142857 \\ -0.142857 & 0.285714 \end{pmatrix}$$

$\epsilon = 1.1$
minPts = 2

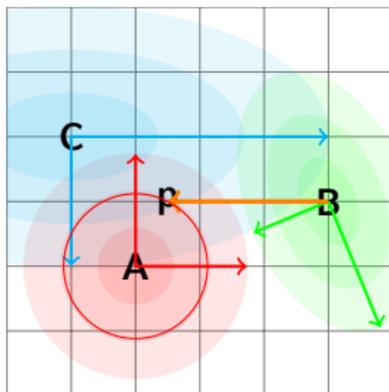
$\epsilon = 1.1$
minPts = 3

$\epsilon = 1.1$
minPts = 4

$\epsilon = 2.1$
minPts = 4

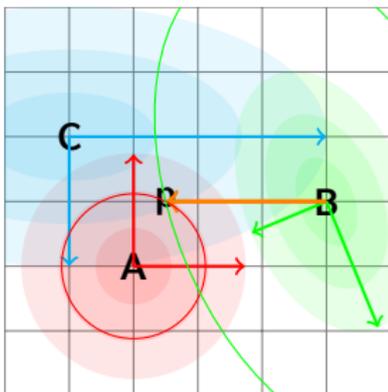
$\epsilon = 4.1$
minPts = 5

$\epsilon = 4.1$
minPts = 4



$$\Sigma_B^{-1} \approx \begin{pmatrix} 0.571428 & -0.142857 \\ -0.142857 & 0.285714 \end{pmatrix}$$

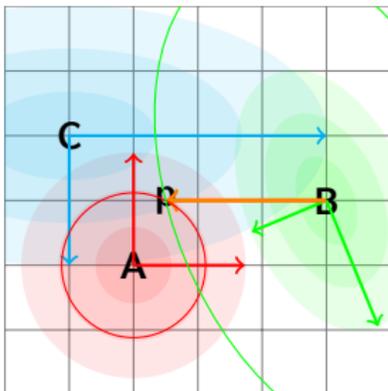
$$p - \mu_B = (-2.5, 0)$$

$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

$$\Sigma_B^{-1} \approx \begin{pmatrix} 0.571428 & -0.142857 \\ -0.142857 & 0.285714 \end{pmatrix}$$

$$p - \mu_B = (-2.5, 0)$$

$$dist^2 = (p - \mu)^T \Sigma^{-1} (p - \mu) \approx 3.5714285$$

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minPts= 2 $\epsilon = 1.1$
minPts= 3 $\epsilon = 1.1$
minPts= 4 $\epsilon = 2.1$
minPts= 4 $\epsilon = 4.1$
minPts= 5 $\epsilon = 4.1$
minPts= 4

$$\Sigma_B^{-1} \approx \begin{pmatrix} 0.571428 & -0.142857 \\ -0.142857 & 0.285714 \end{pmatrix}$$

$$p - \mu_B = (-2.5, 0)$$

$$\text{dist}^2 = (p - \mu)^T \Sigma^{-1} (p - \mu) \approx 3.5714285$$

$$\begin{aligned} \text{prob}_B &\approx \frac{1}{\sqrt{(2\pi)^2 \cdot 7}} e^{-\frac{1}{2} 3.5714285} \\ &\approx 0.01008661 \end{aligned}$$

$\epsilon = 1.1$
minPts = 2

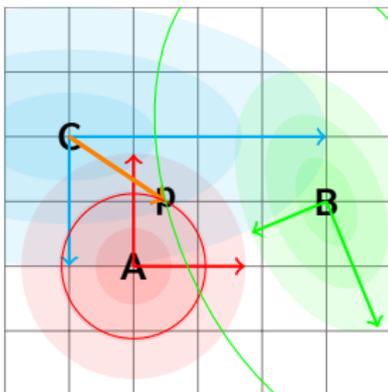
$\epsilon = 1.1$
minPts = 3

$\epsilon = 1.1$
minPts = 4

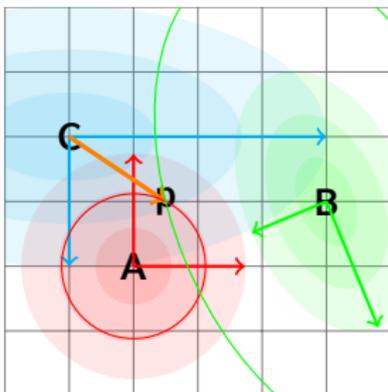
$\epsilon = 2.1$
minPts = 4

$\epsilon = 4.1$
minPts = 5

$\epsilon = 4.1$
minPts = 4

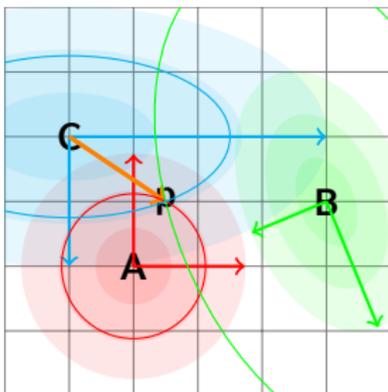


$$\Sigma_C = \begin{pmatrix} 16 & 0 \\ 0 & 4 \end{pmatrix} \quad \Sigma_C^{-1} = \begin{pmatrix} \frac{1}{16} & 0 \\ 0 & \frac{1}{4} \end{pmatrix}$$

$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

$$\Sigma_C = \begin{pmatrix} 16 & 0 \\ 0 & 4 \end{pmatrix} \quad \Sigma_C^{-1} = \begin{pmatrix} \frac{1}{16} & 0 \\ 0 & \frac{1}{4} \end{pmatrix}$$

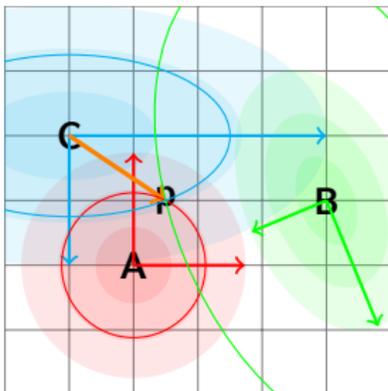
$$p - \mu_C = (1.5, -1)$$

$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

$$\Sigma_C = \begin{pmatrix} 16 & 0 \\ 0 & 4 \end{pmatrix} \quad \Sigma_C^{-1} = \begin{pmatrix} \frac{1}{16} & 0 \\ 0 & \frac{1}{4} \end{pmatrix}$$

$$p - \mu_C = (1.5, -1)$$

$$dist^2 = (p - \mu)^T \Sigma^{-1} (p - \mu) \approx 0.390625$$

$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

$$\Sigma_C = \begin{pmatrix} 16 & 0 \\ 0 & 4 \end{pmatrix} \quad \Sigma_C^{-1} = \begin{pmatrix} \frac{1}{16} & 0 \\ 0 & \frac{1}{4} \end{pmatrix}$$

$$p - \mu_C = (1.5, -1)$$

$$\text{dist}^2 = (p - \mu)^T \Sigma^{-1} (p - \mu) \approx 0.390625$$

$$\begin{aligned} \text{prob}_C &\approx \frac{1}{\sqrt{(2\pi)^2 \cdot 64}} e^{-\frac{1}{2} \cdot 0.390625} \\ &\approx 0.01636466 \end{aligned}$$

$\epsilon = 1.1$
minPts = 2

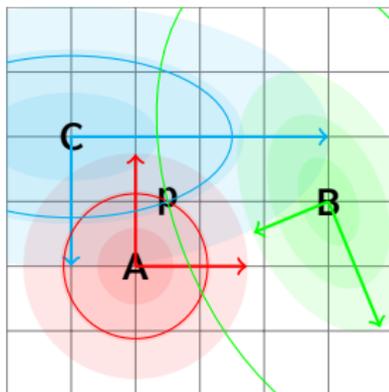
$\epsilon = 1.1$
minPts = 3

$\epsilon = 1.1$
minPts = 4

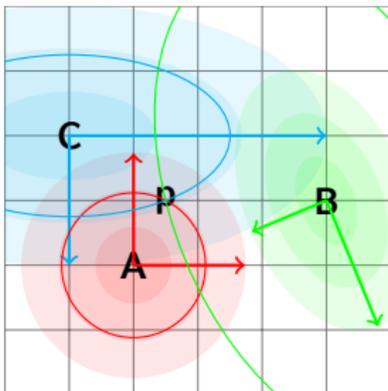
$\epsilon = 2.1$
minPts = 4

$\epsilon = 4.1$
minPts = 5

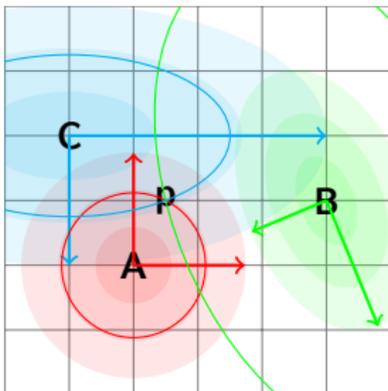
$\epsilon = 4.1$
minPts = 4



| | A | B | C |
|-------------|----------|----------|----------|
| <i>prob</i> | 0.043075 | 0.010087 | 0.016365 |
| <i>size</i> | 30% | 20% | 50% |

$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

| | <i>A</i> | <i>B</i> | <i>C</i> |
|--------------|----------|----------|----------|
| <i>prob</i> | 0.043075 | 0.010087 | 0.016365 |
| <i>size</i> | 30% | 20% | 50% |
| <i>score</i> | 0.012922 | 0.002017 | 0.008182 |

$\epsilon = 1.1$
minPts= 2 $\epsilon = 1.1$
minPts= 3 $\epsilon = 1.1$
minPts= 4 $\epsilon = 2.1$
minPts= 4 $\epsilon = 4.1$
minPts= 5 $\epsilon = 4.1$
minPts= 4

| | <i>A</i> | <i>B</i> | <i>C</i> |
|--------------|--------------------|----------|----------|
| <i>prob</i> | 0.043075 | 0.010087 | 0.016365 |
| <i>size</i> | 30% | 20% | 50% |
| <i>score</i> | 0.012922 | 0.002017 | 0.008182 |
| <i>sum</i> | divide by 0.023122 | | |

$\epsilon = 1.1$
minPts = 2

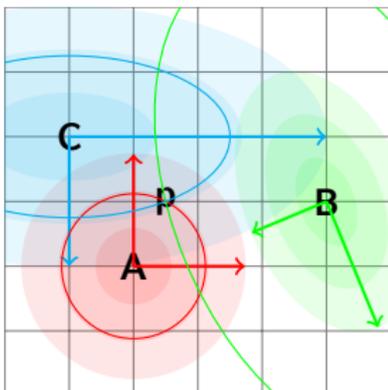
$\epsilon = 1.1$
minPts = 3

$\epsilon = 1.1$
minPts = 4

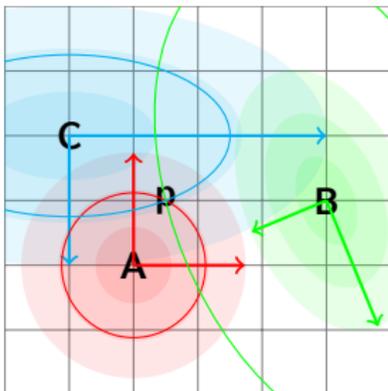
$\epsilon = 2.1$
minPts = 4

$\epsilon = 4.1$
minPts = 5

$\epsilon = 4.1$
minPts = 4

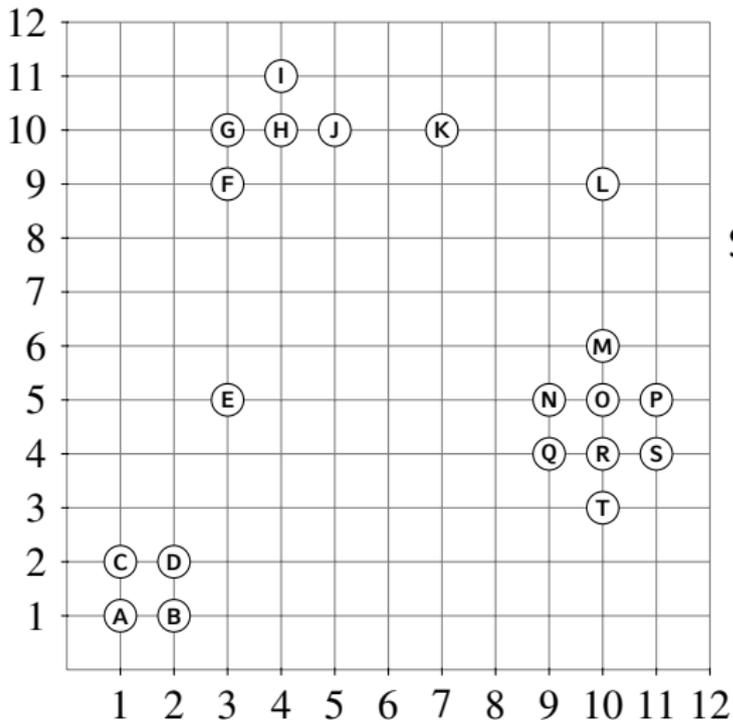


| | A | B | C |
|---------------|--------------------|-----------------|------------------|
| <i>prob</i> | 0.043075 | 0.010087 | 0.016365 |
| <i>size</i> | 30% | 20% | 50% |
| <i>score</i> | 0.012922 | 0.002017 | 0.008182 |
| <i>sum</i> | divide by 0.023122 | | |
| <i>weight</i> | $\approx 55.9\%$ | $\approx 8.2\%$ | $\approx 35.4\%$ |

$\epsilon = 1.1$
minPts = 2 $\epsilon = 1.1$
minPts = 3 $\epsilon = 1.1$
minPts = 4 $\epsilon = 2.1$
minPts = 4 $\epsilon = 4.1$
minPts = 5 $\epsilon = 4.1$
minPts = 4

| | A | B | C |
|---------------|--------------------|-----------------|------------------|
| <i>prob</i> | 0.043075 | 0.010087 | 0.016365 |
| <i>size</i> | 30% | 20% | 50% |
| <i>score</i> | 0.012922 | 0.002017 | 0.008182 |
| <i>sum</i> | divide by 0.023122 | | |
| <i>weight</i> | $\approx 55.9\%$ | $\approx 8.2\%$ | $\approx 35.4\%$ |

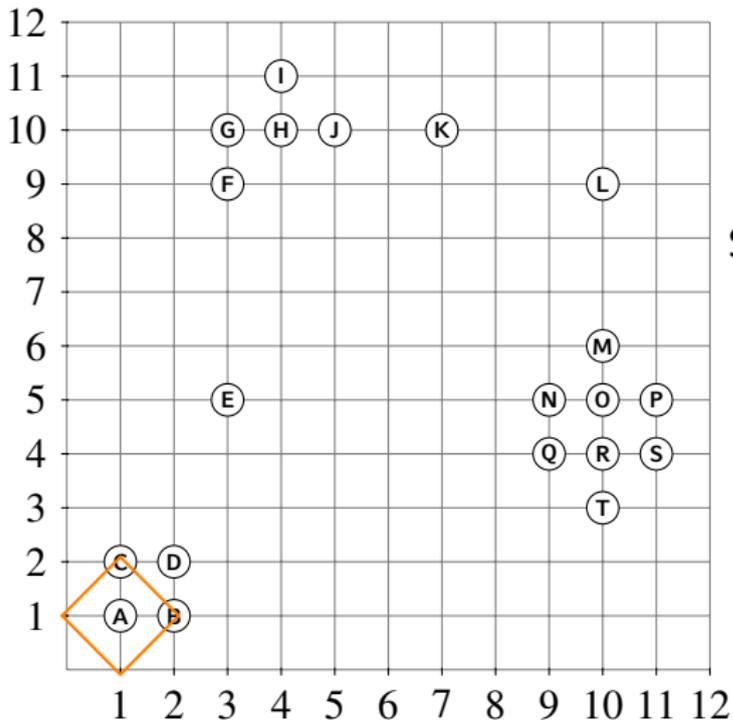
Point p belongs mostly to cluster A!



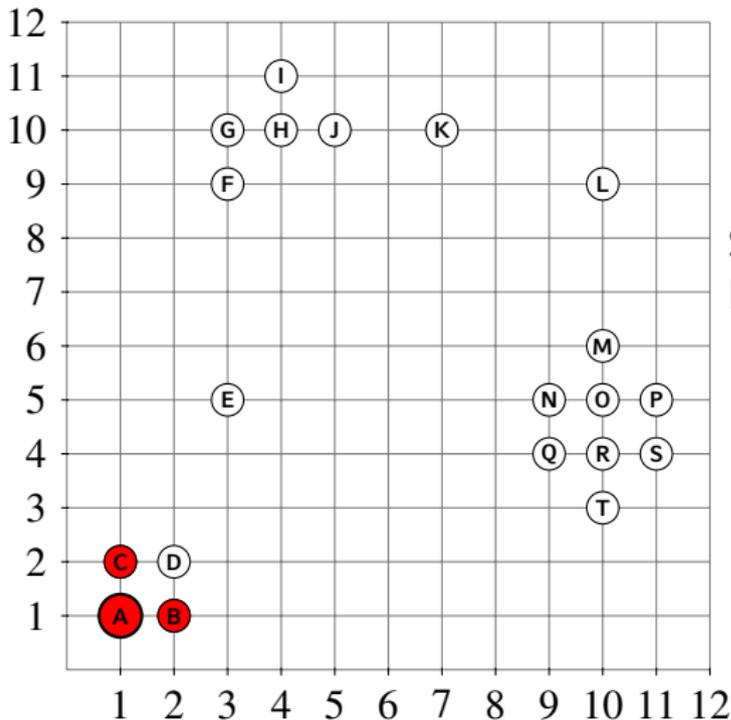
$$\epsilon = 1.1$$

$$\text{minPts} = 2$$

Seed list:

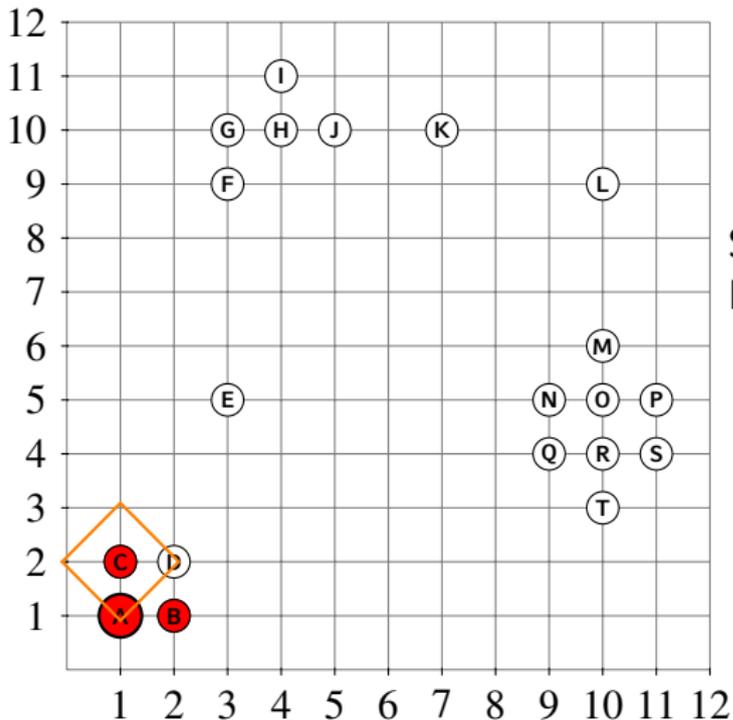
 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 2$

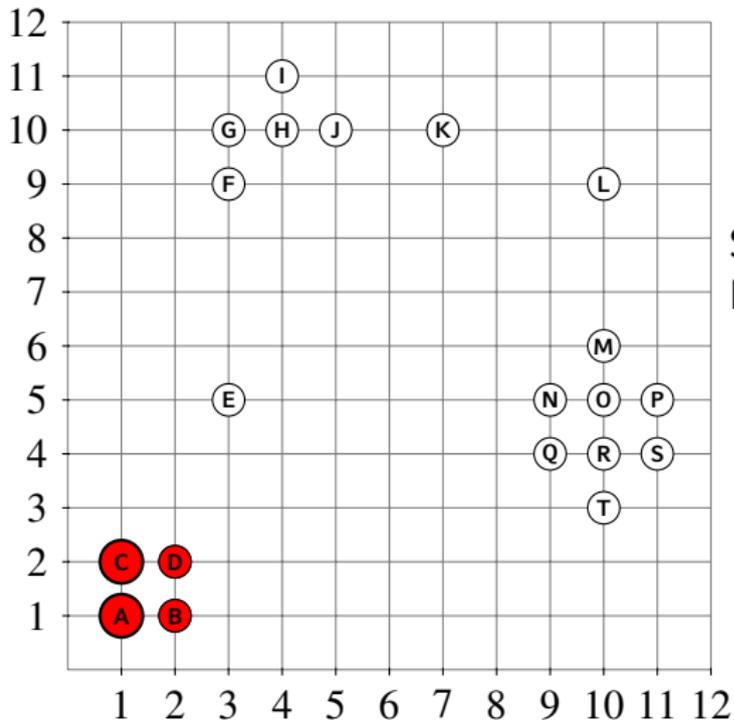
Seed list:

BC

 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

B

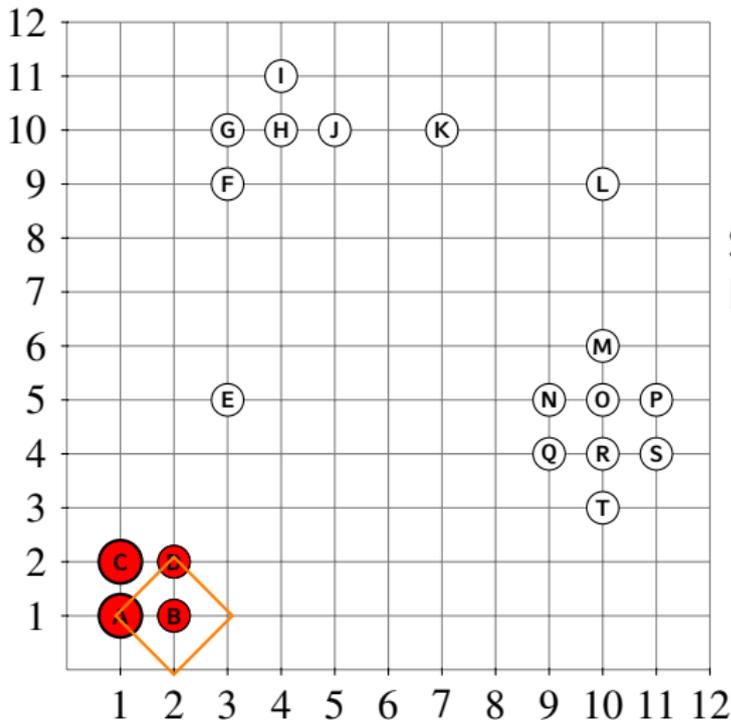


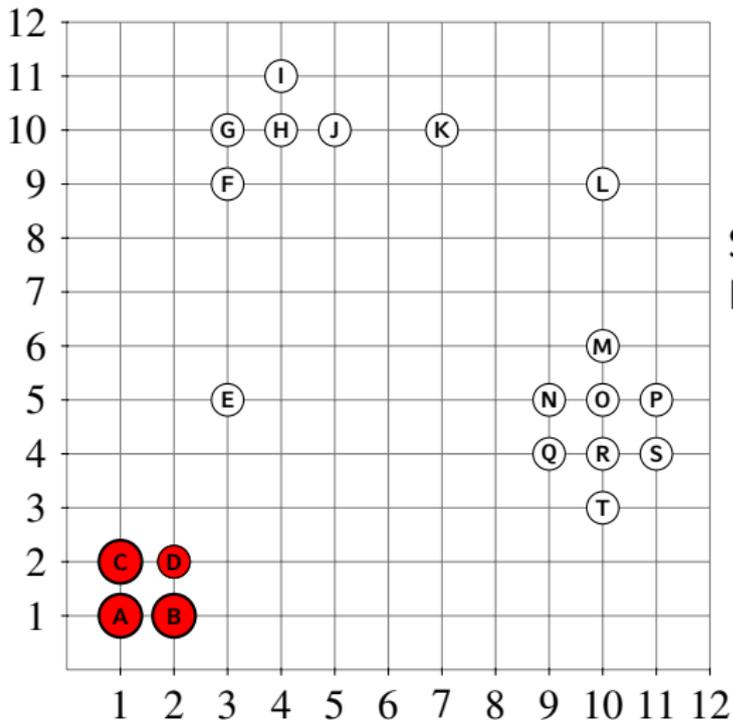
$$\epsilon = 1.1$$

$$\text{minPts} = 2$$

Seed list:

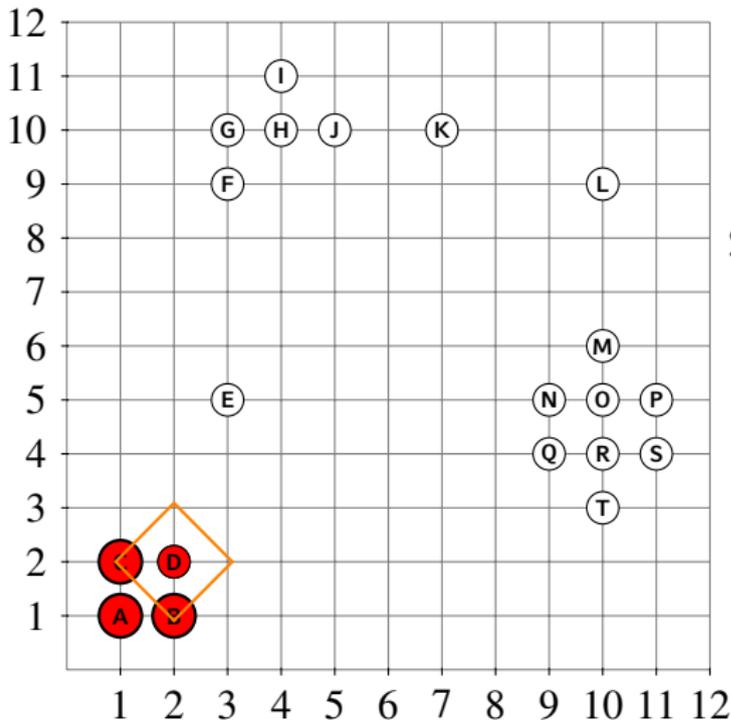
BD



 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

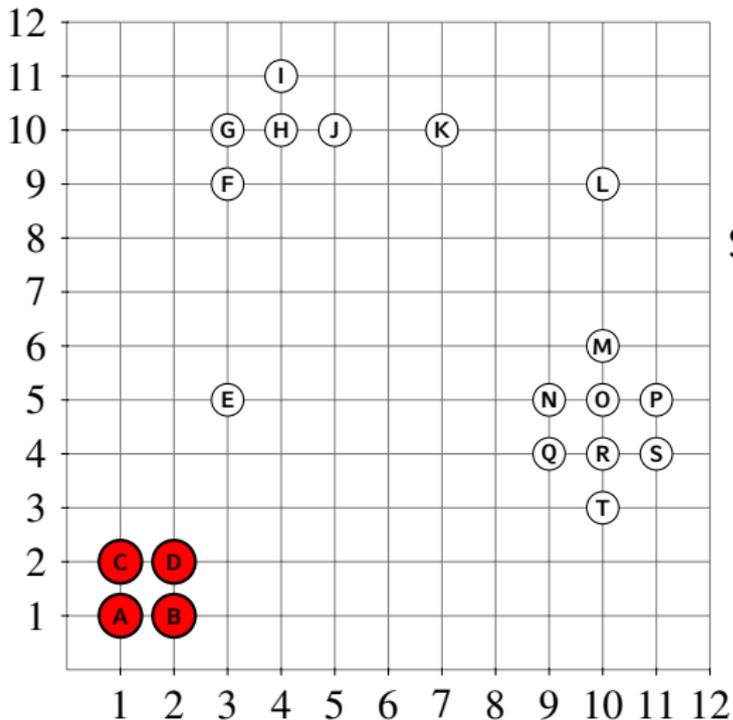
D



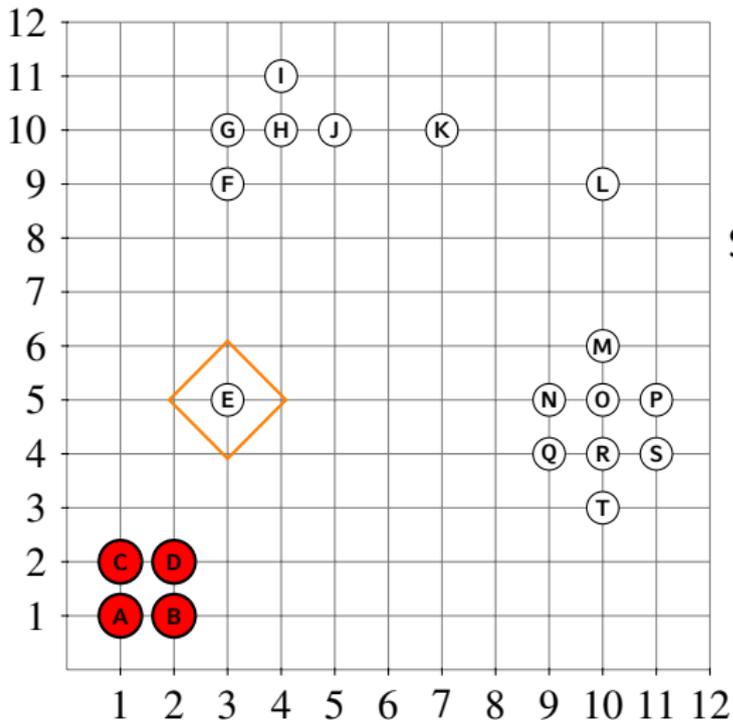
$\epsilon = 1.1$

$minPts = 2$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 2$

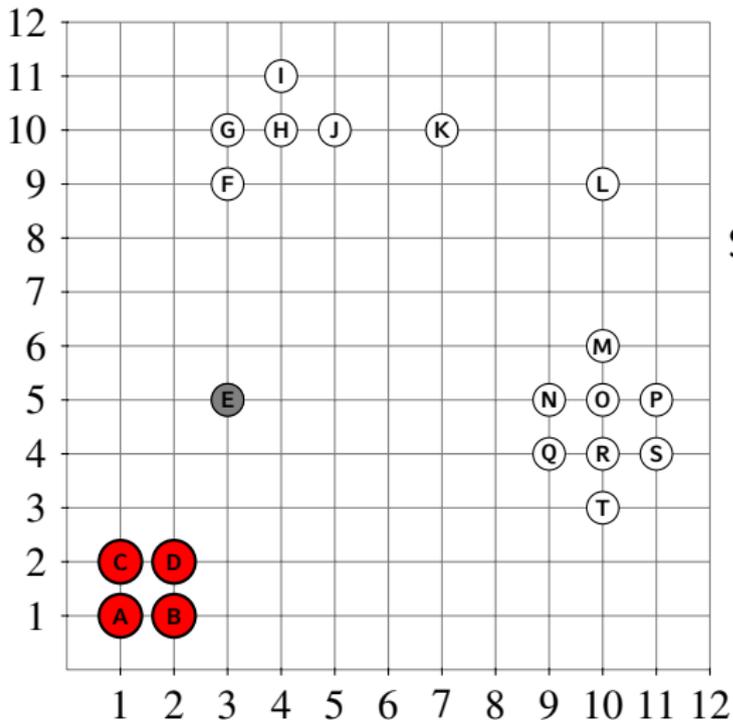
Seed list:



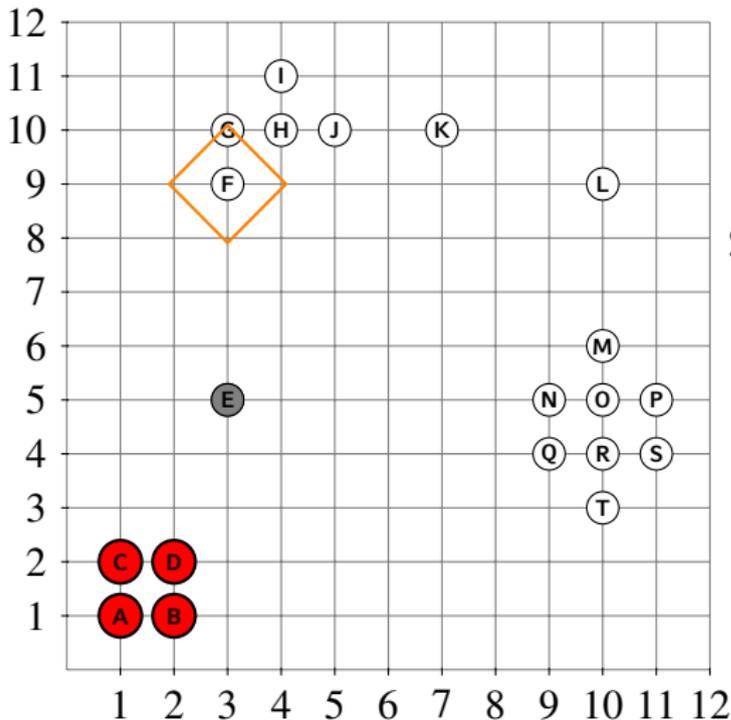
$$\epsilon = 1.1$$

$$\text{minPts} = 2$$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 2$

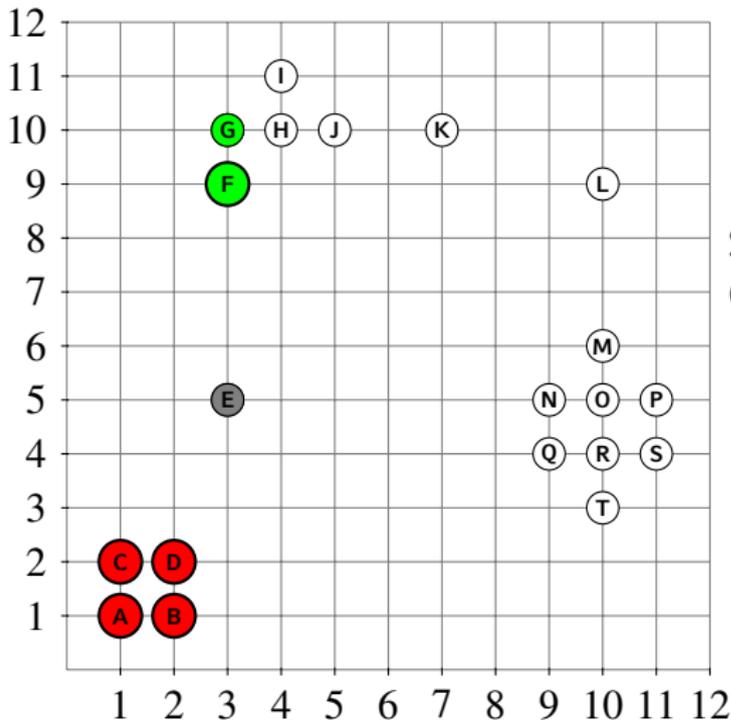
Seed list:



$\epsilon = 1.1$

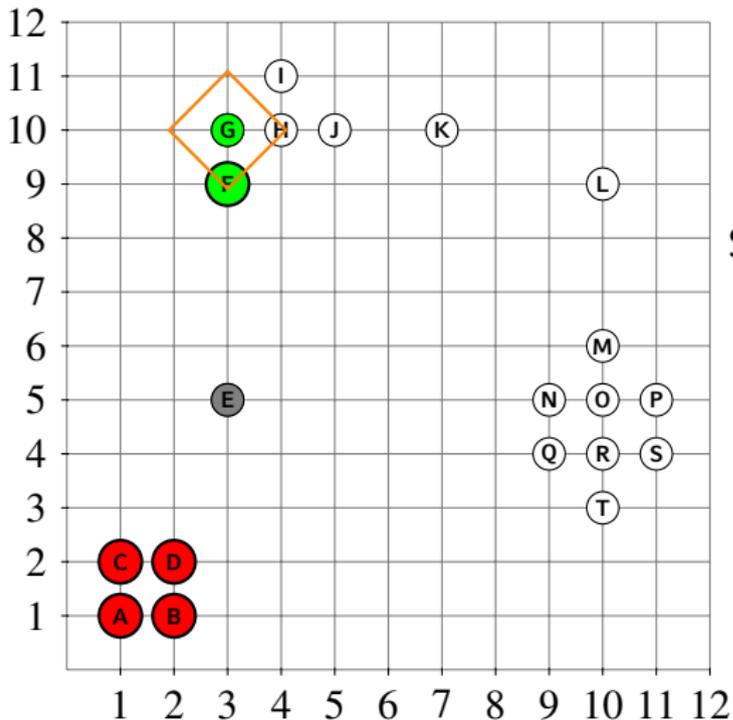
$minPts = 2$

Seed list:

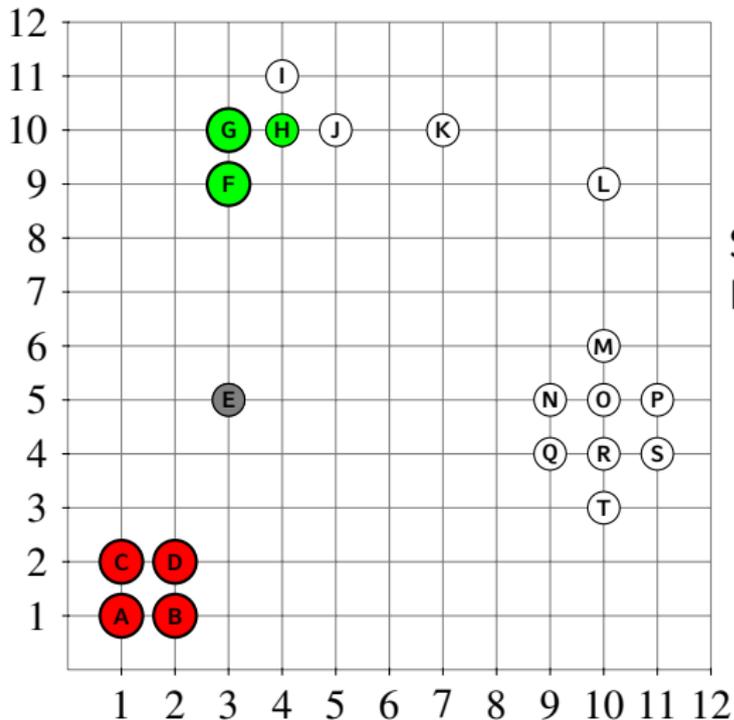
 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

G

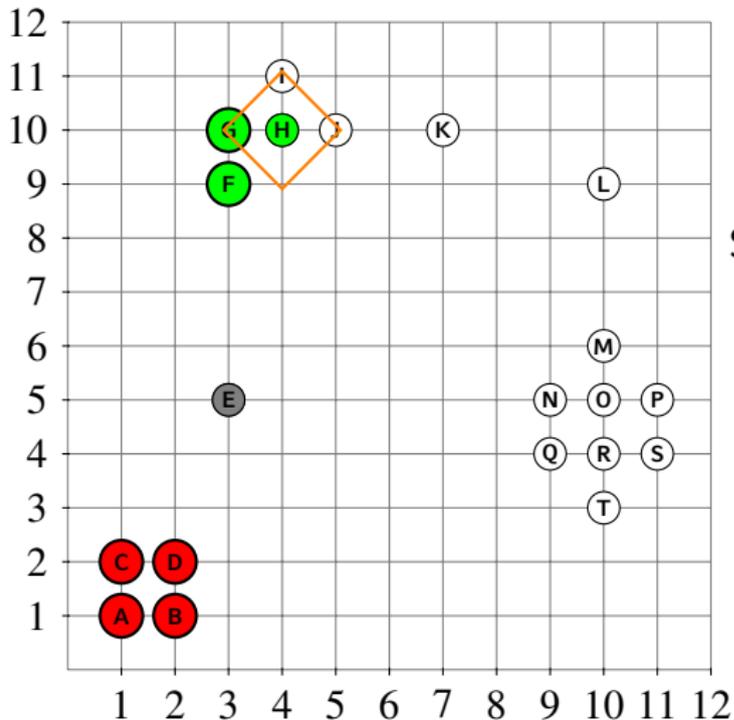
 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

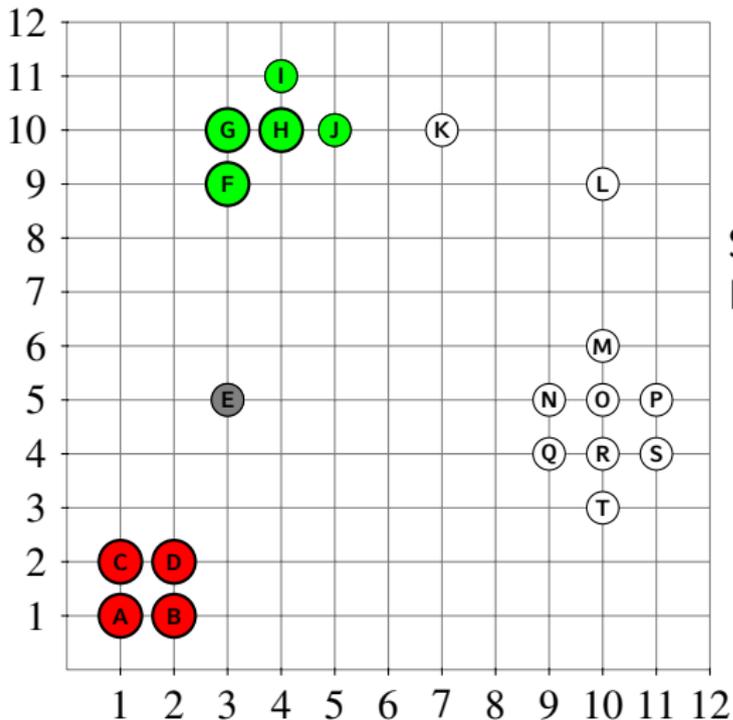
H



$$\epsilon = 1.1$$

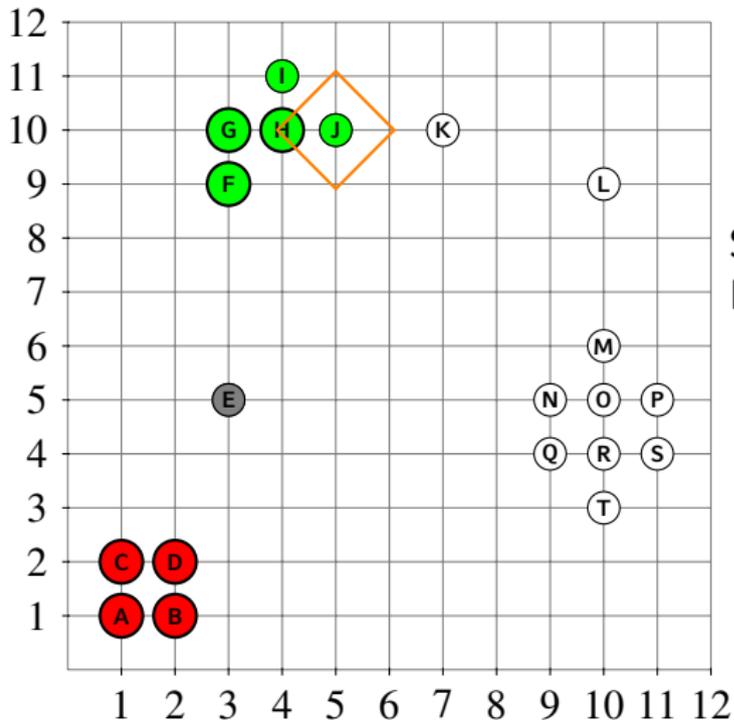
$$\text{minPts} = 2$$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

IJ

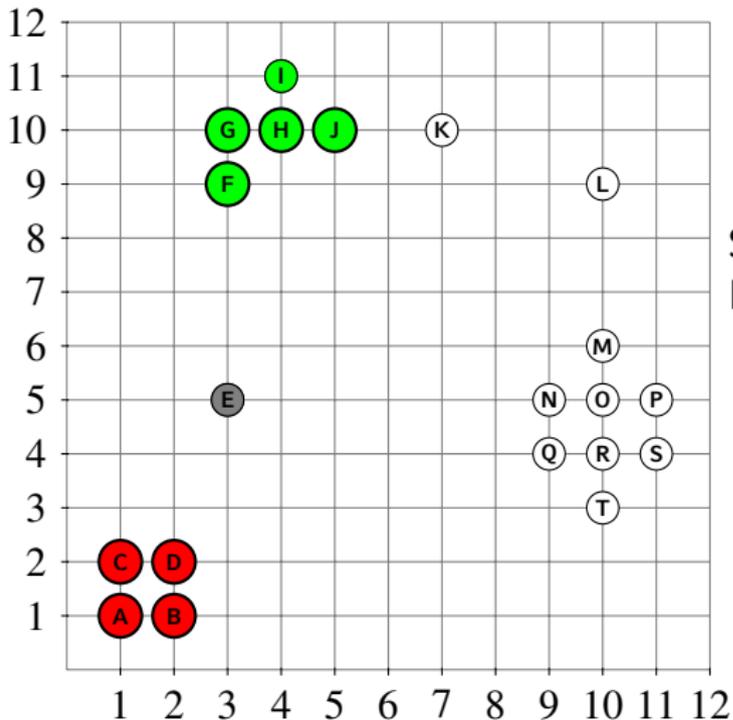


$$\epsilon = 1.1$$

$$minPts = 2$$

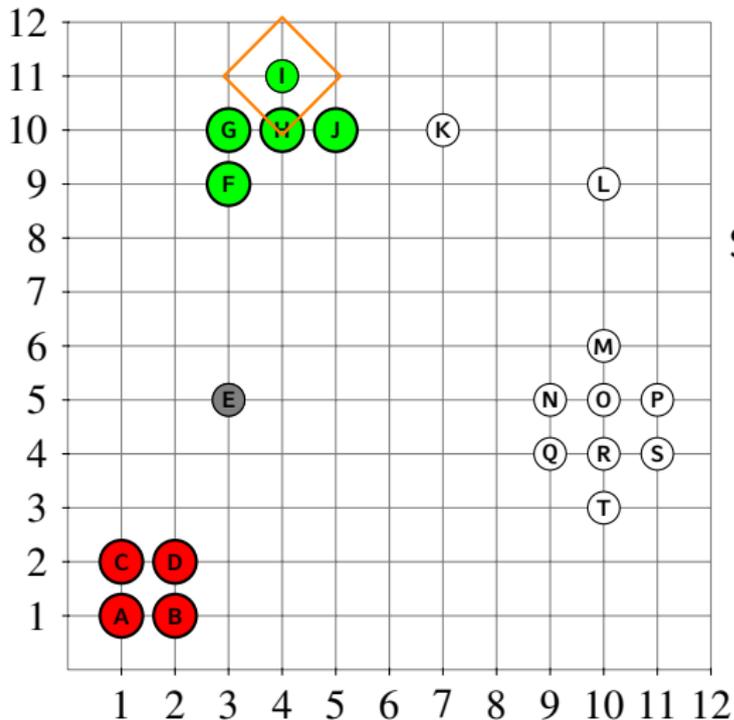
Seed list:

I

 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

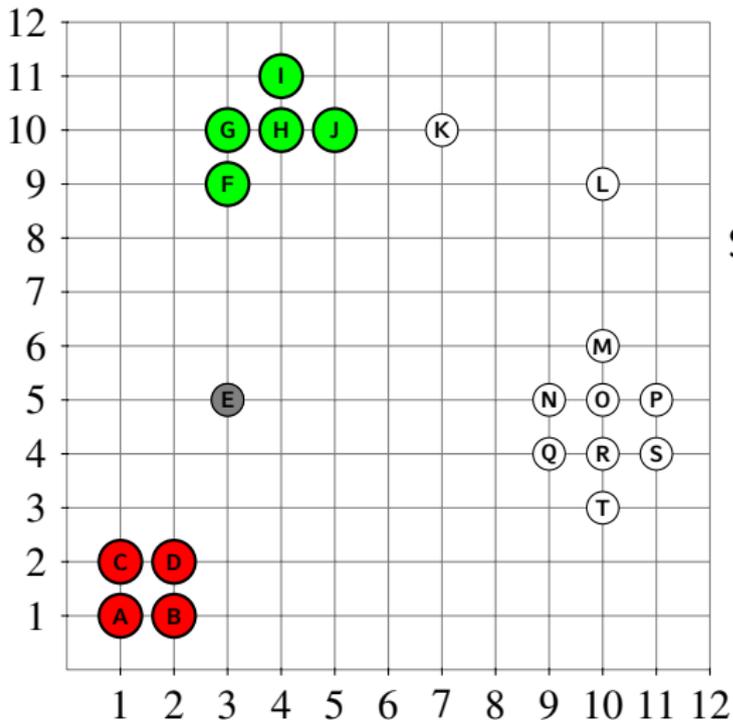
I



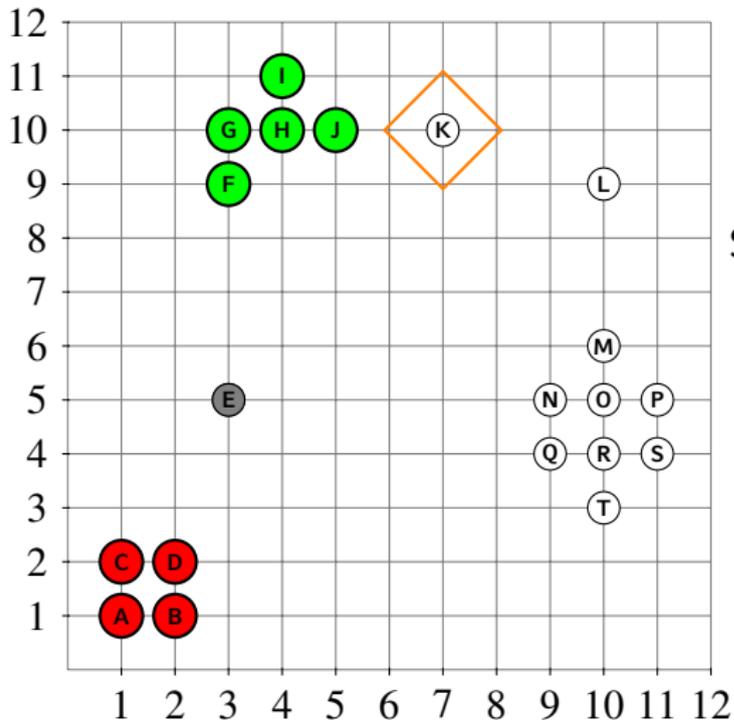
$$\epsilon = 1.1$$

$$\text{minPts} = 2$$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:



$$\epsilon = 1.1$$

$$\text{minPts} = 2$$

Seed list:

$\epsilon = 1.1$
 $minPts = 2$

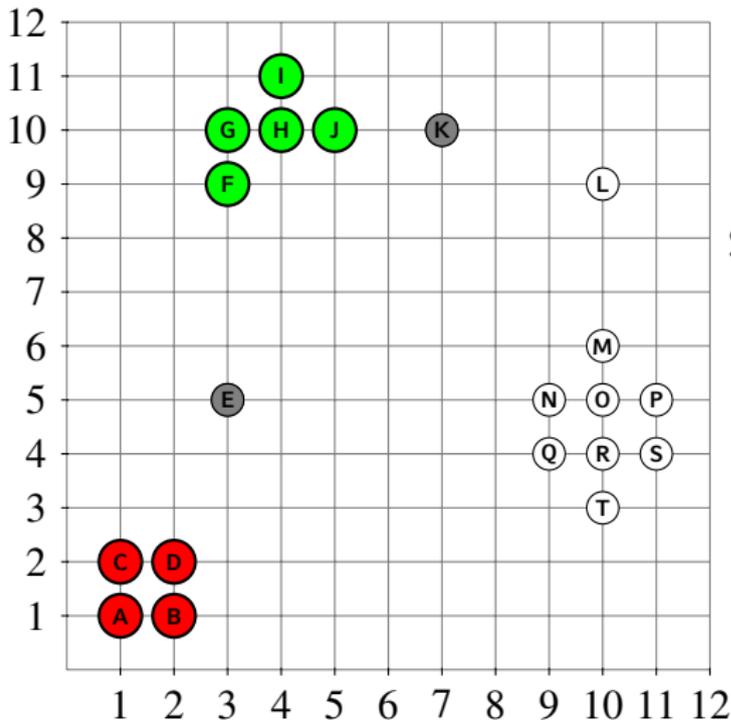
$\epsilon = 1.1$
 $minPts = 3$

$\epsilon = 1.1$
 $minPts = 4$

$\epsilon = 2.1$
 $minPts = 4$

$\epsilon = 4.1$
 $minPts = 5$

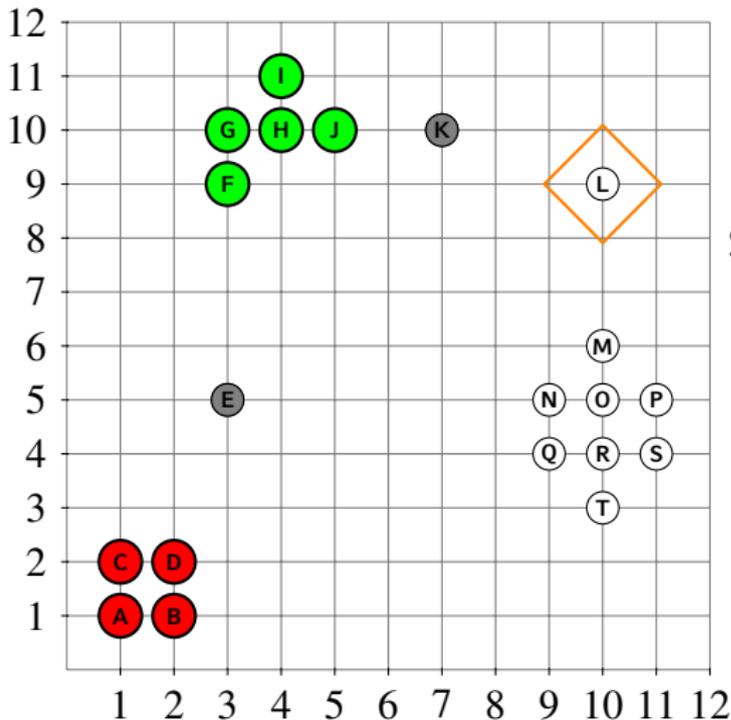
$\epsilon = 4.1$
 $minPts = 4$



$\epsilon = 1.1$

$minPts = 2$

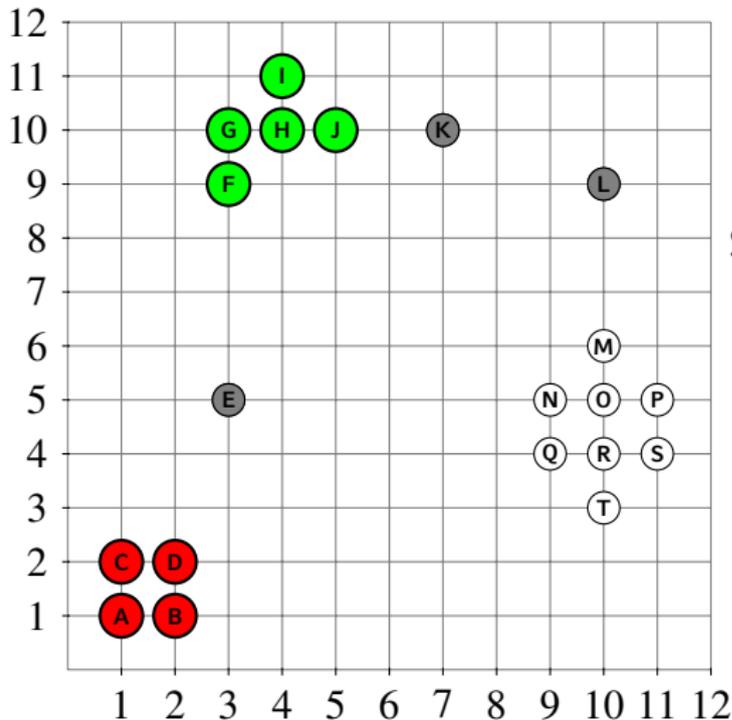
Seed list:



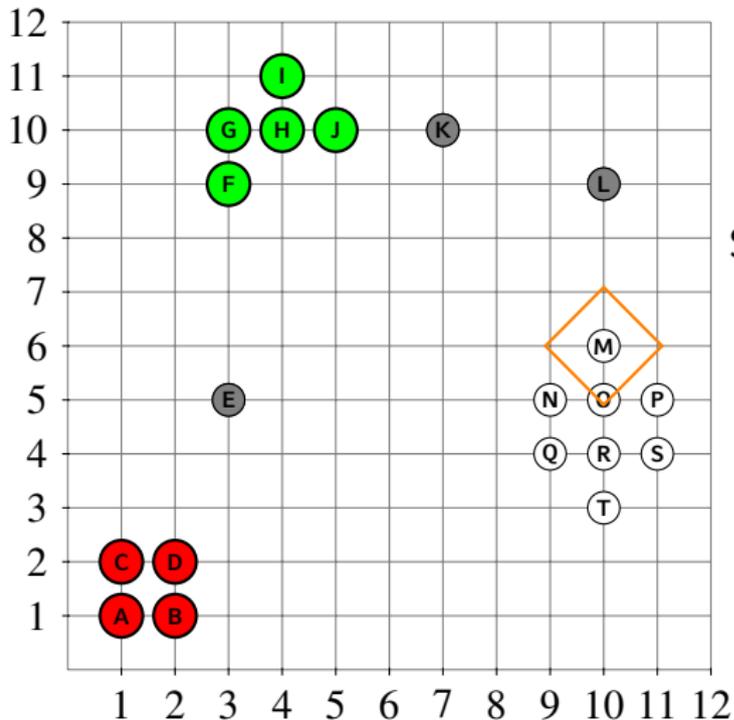
$$\epsilon = 1.1$$

$$\text{minPts} = 2$$

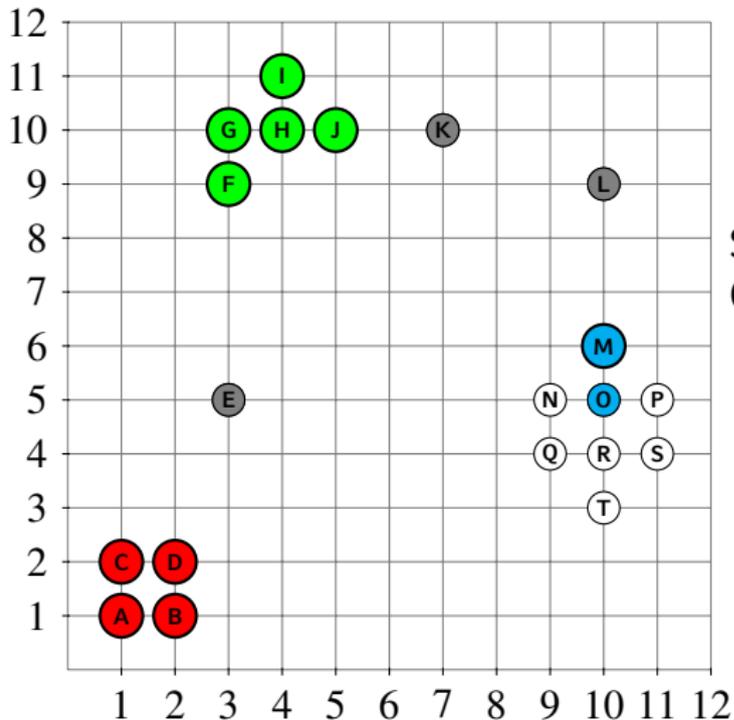
Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

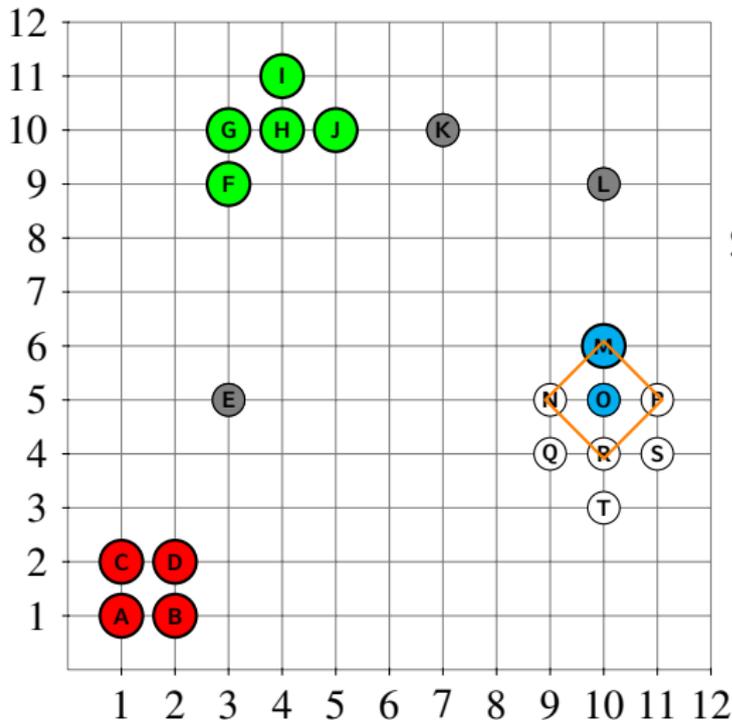
 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

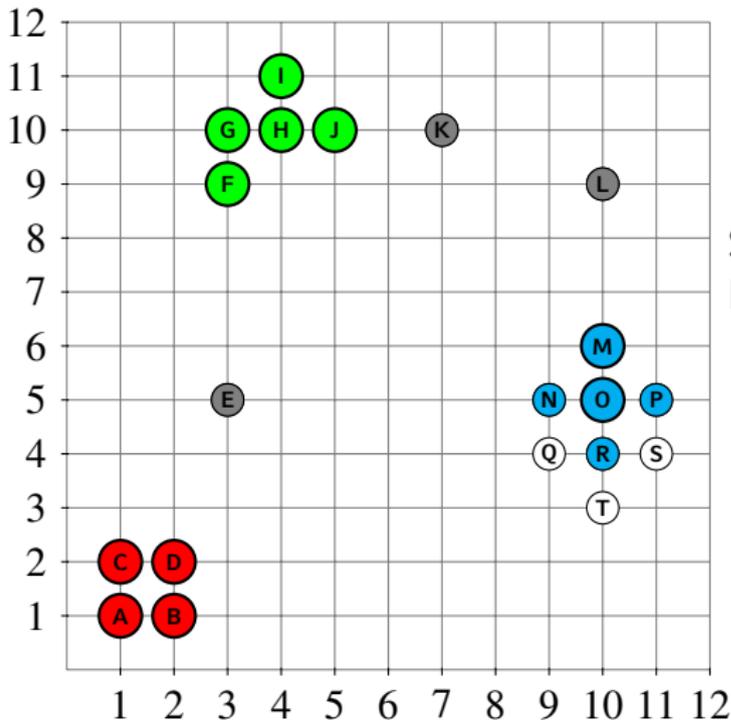
0

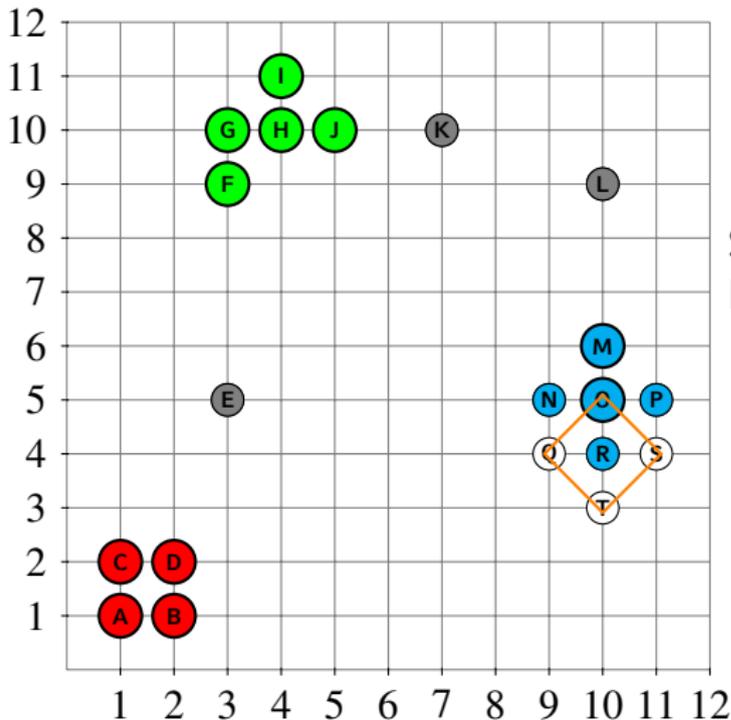


$\epsilon = 1.1$

$minPts = 2$

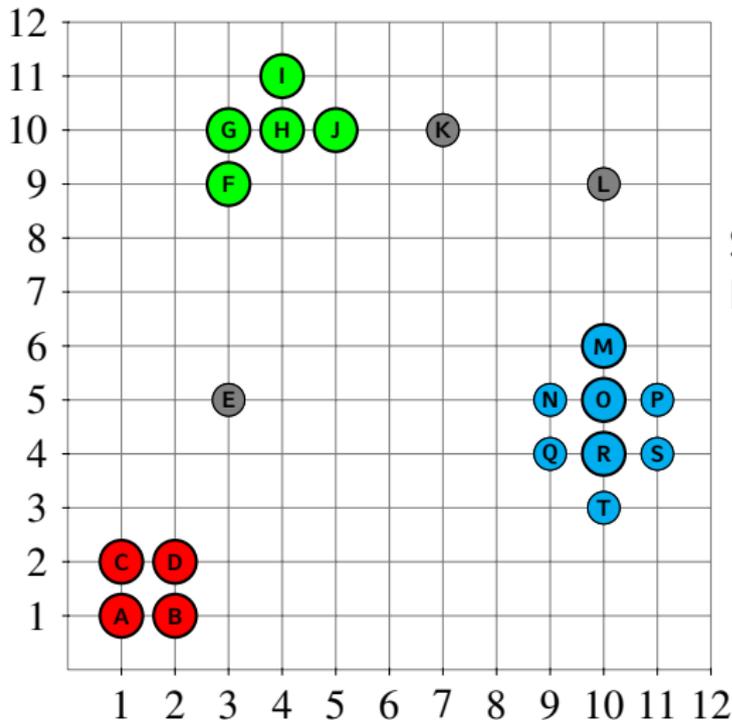
Seed list:

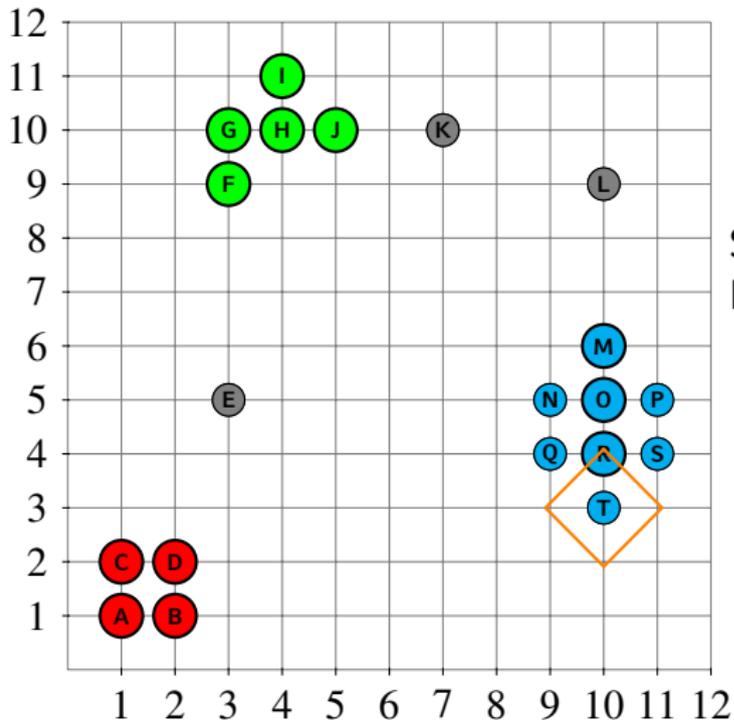
 $\epsilon = 1.1$ $\text{minPts} = 2$ Seed list:
NPR

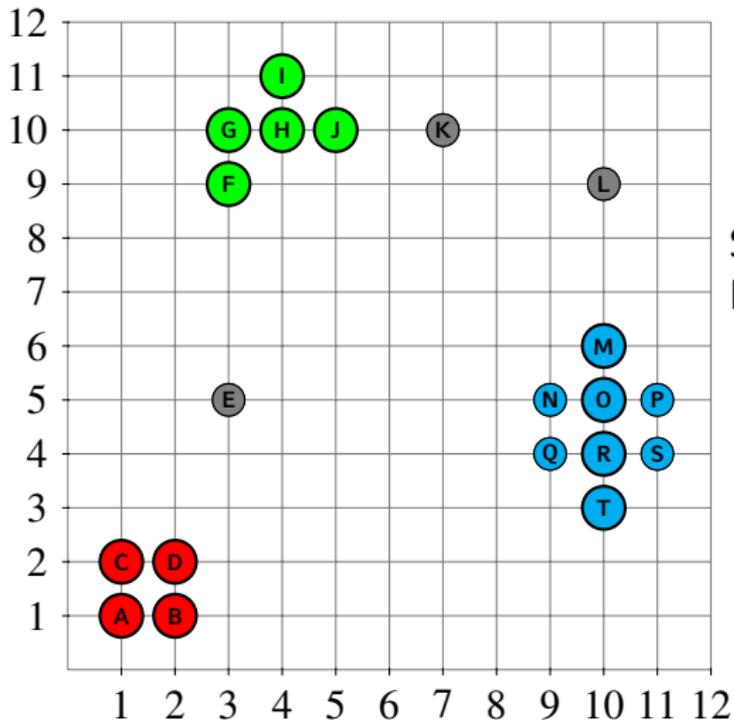
 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

NP

 $\epsilon = 1.1$ $\text{minPts} = 2$ Seed list:
NPQST

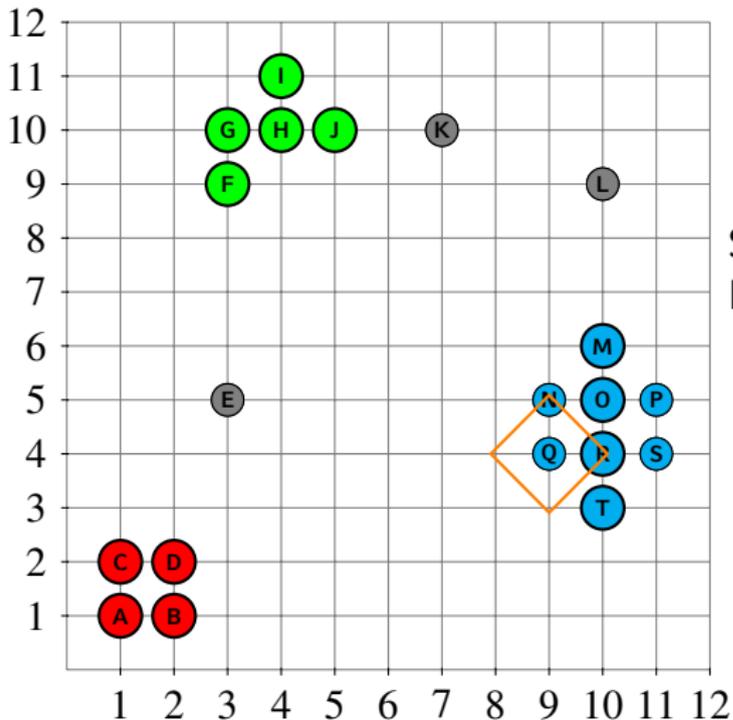




$$\epsilon = 1.1$$

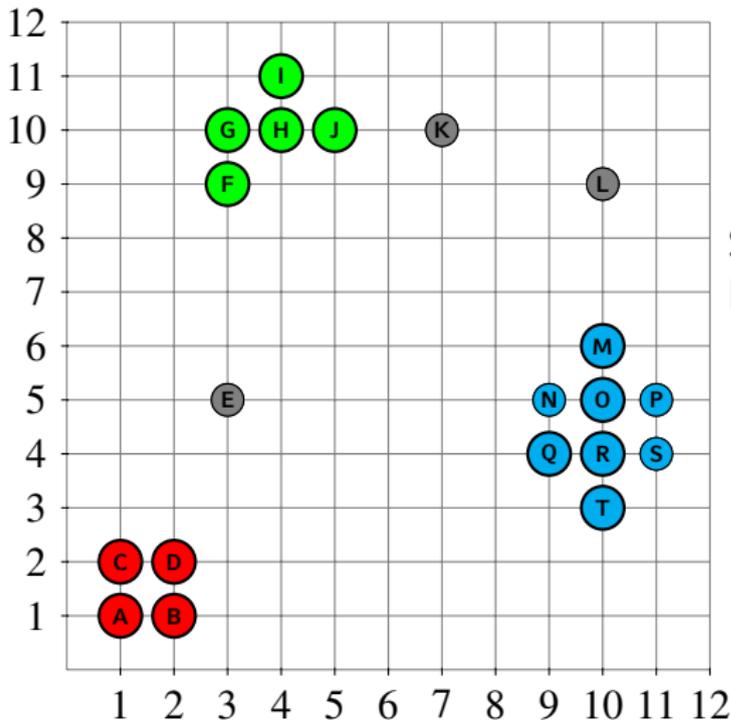
$$\text{minPts} = 2$$

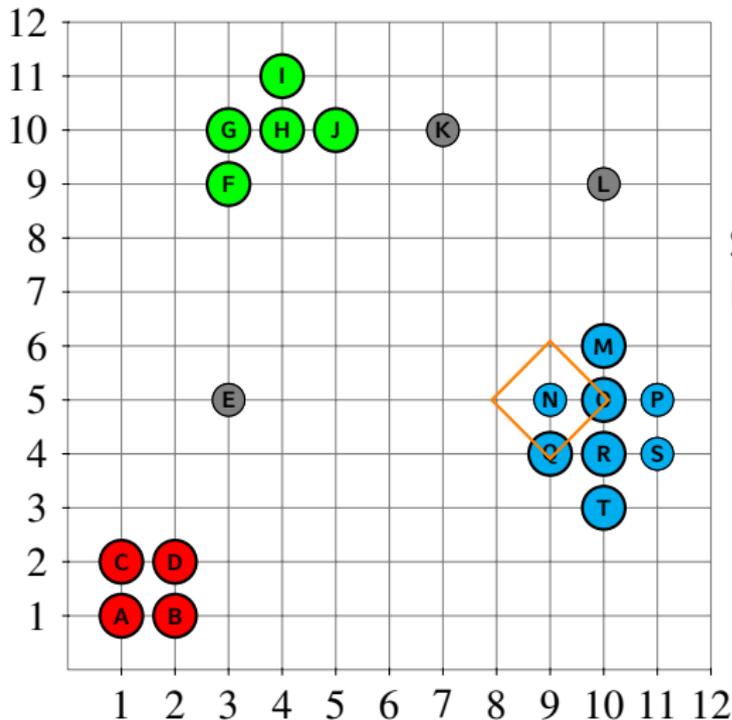
Seed list:
NPQS

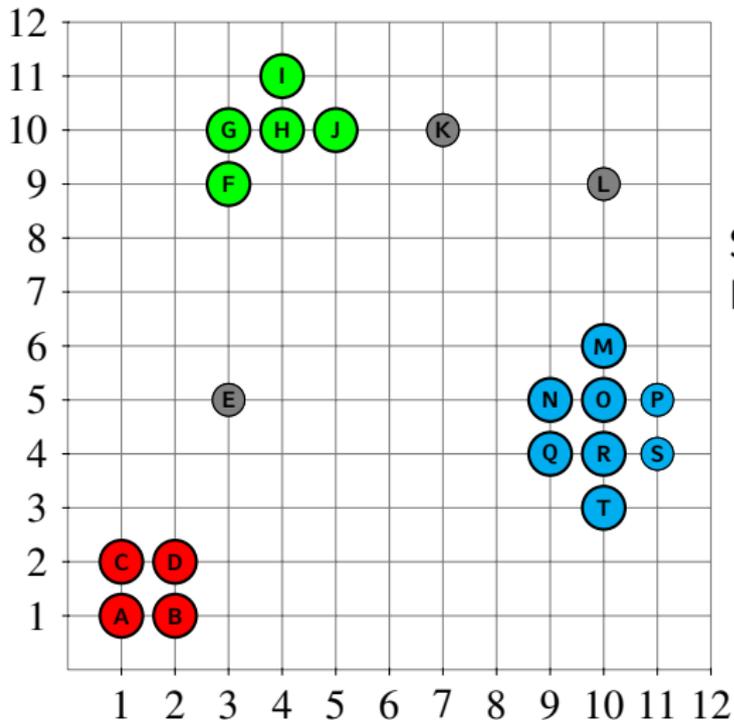
 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

NPS

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 1.1$ $\text{minPts} = 2$ Seed list:
NPS

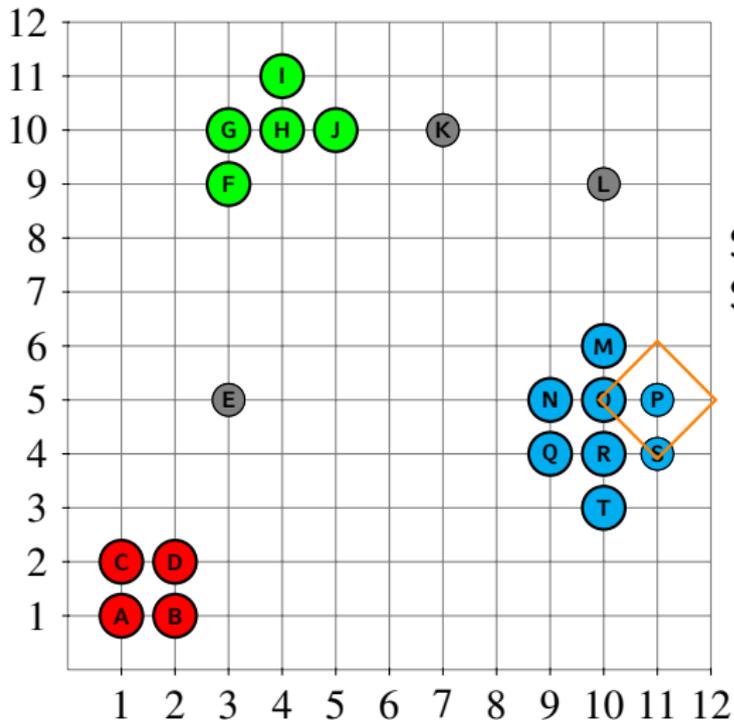
 $\epsilon = 1.1$ $\text{minPts} = 2$ Seed list:
PS



$$\epsilon = 1.1$$

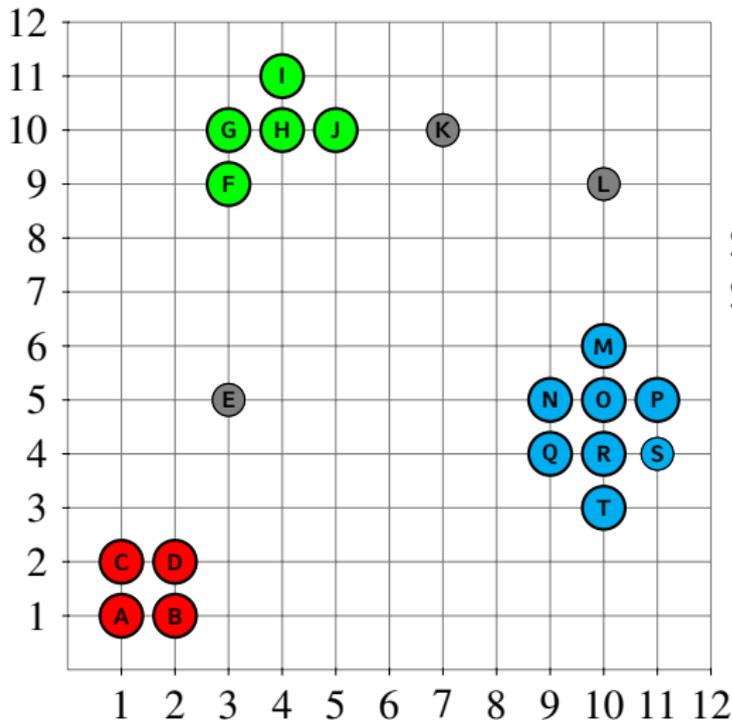
$$\text{minPts} = 2$$

Seed list:
PS

 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

S

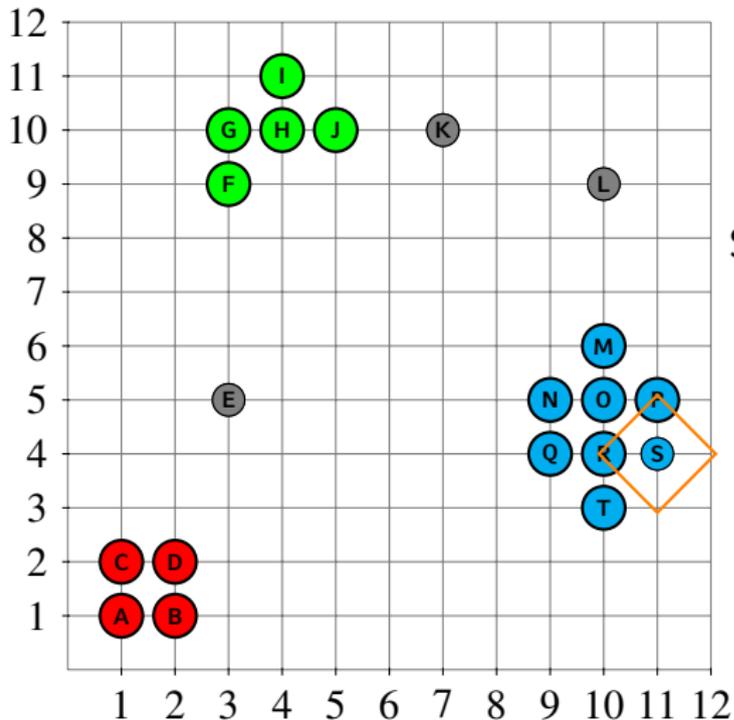


$\epsilon = 1.1$

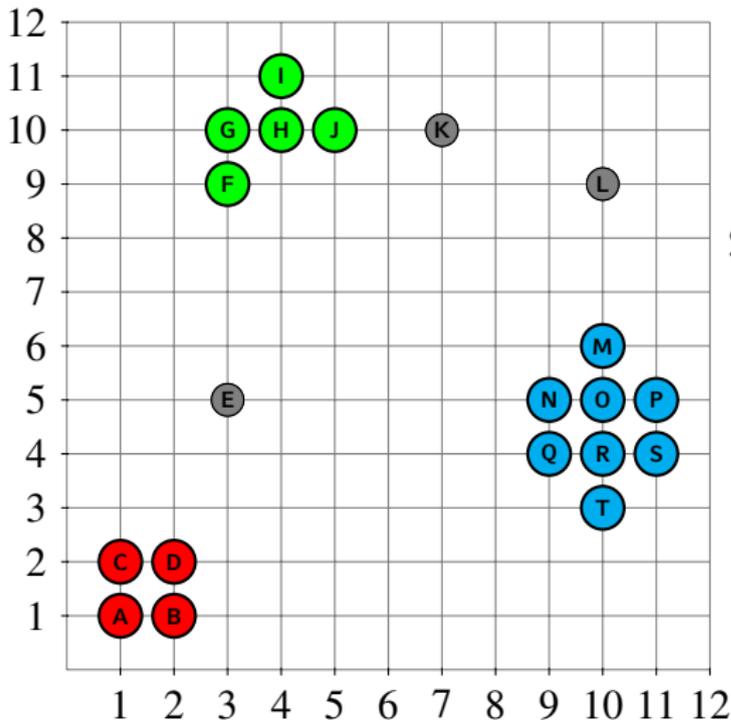
$minPts = 2$

Seed list:

S

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 1.1$ $\text{minPts} = 2$

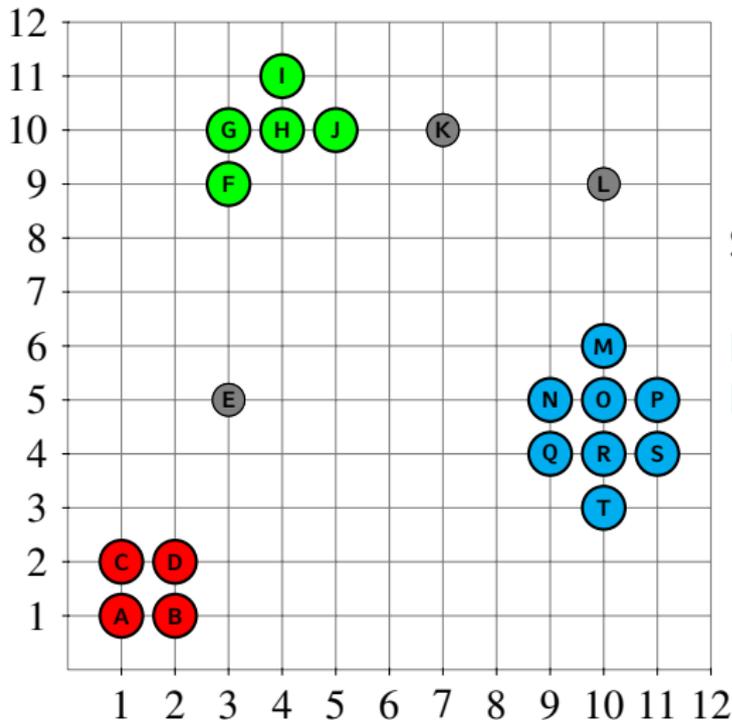
Seed list:

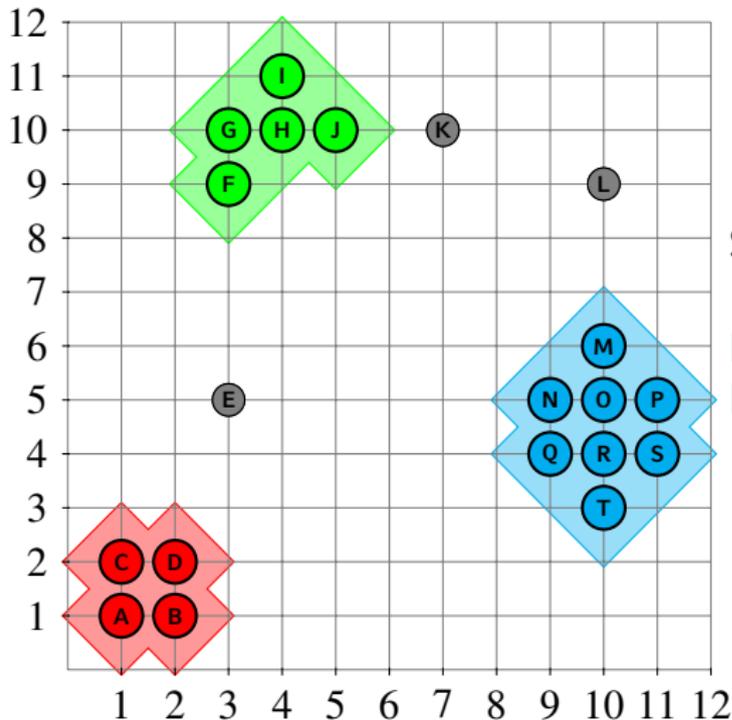


$\epsilon = 1.1$

$minPts = 2$

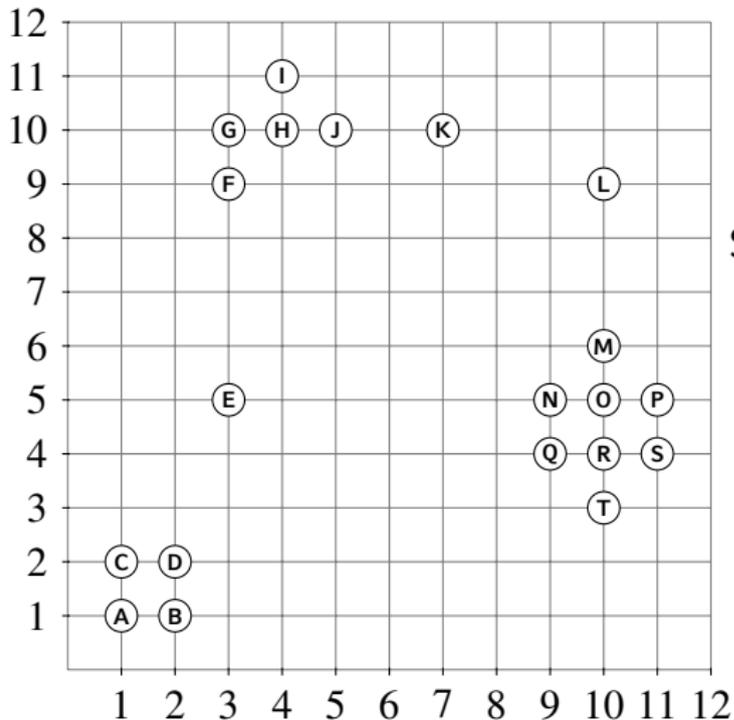
Seed list:



 $\epsilon = 1.1$ $\text{minPts} = 2$

Seed list:

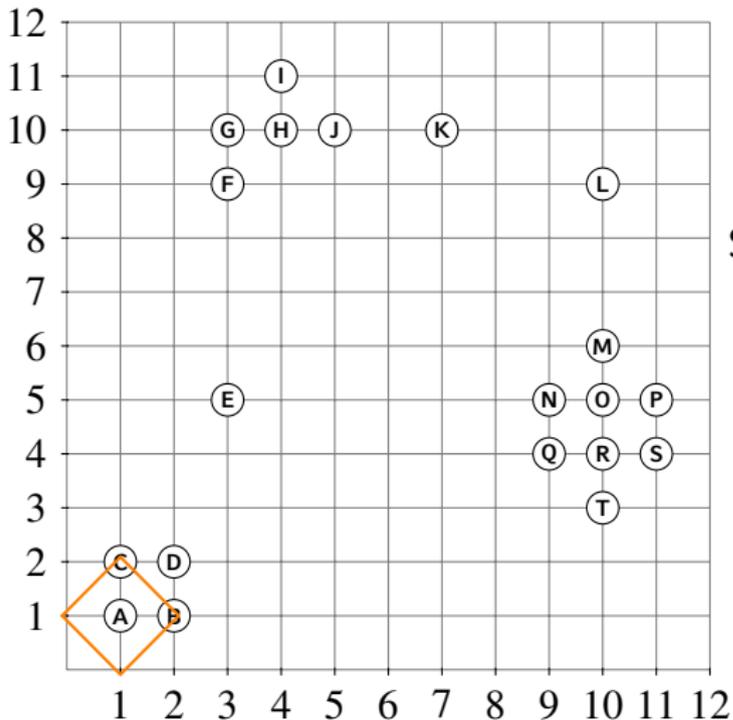
Keine
Randpunkte!



$$\epsilon = 1.1$$

$$\text{minPts} = 3$$

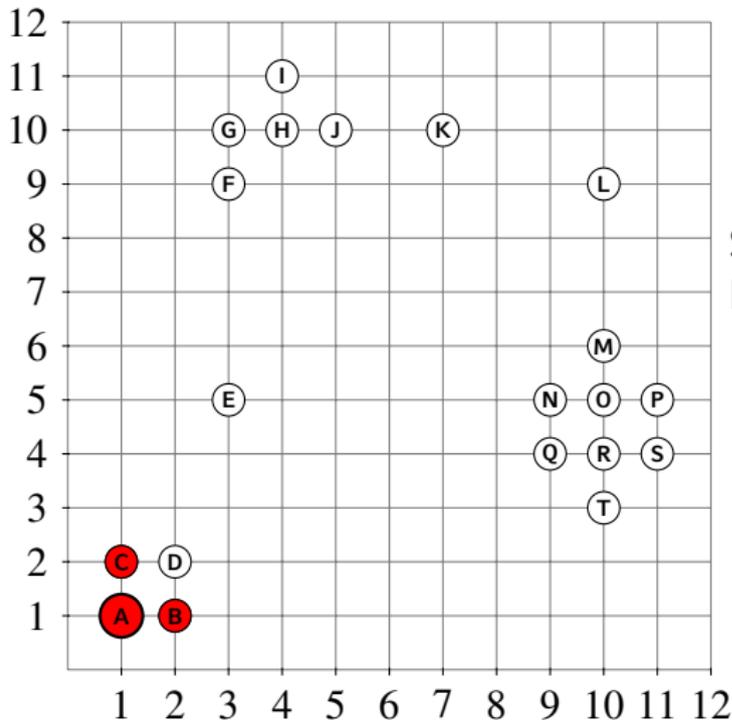
Seed list:

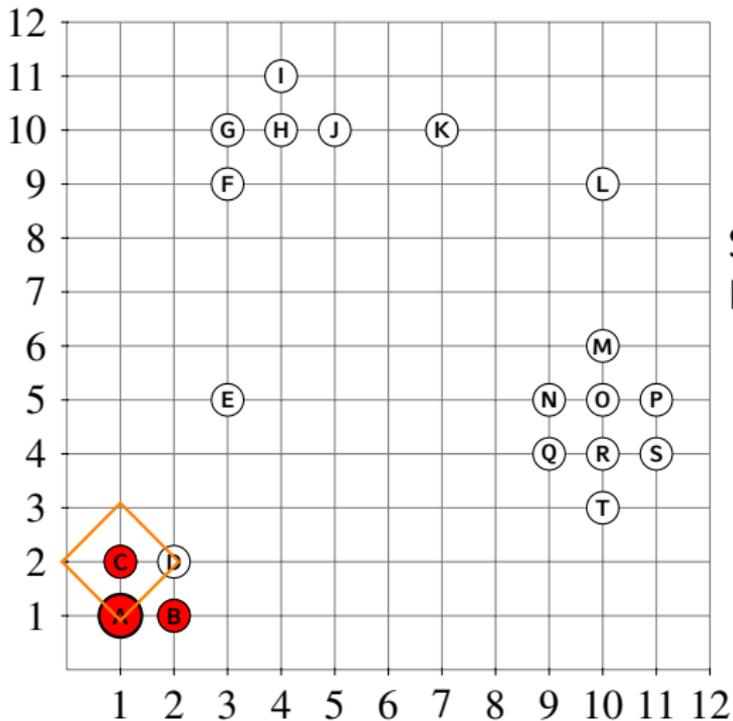


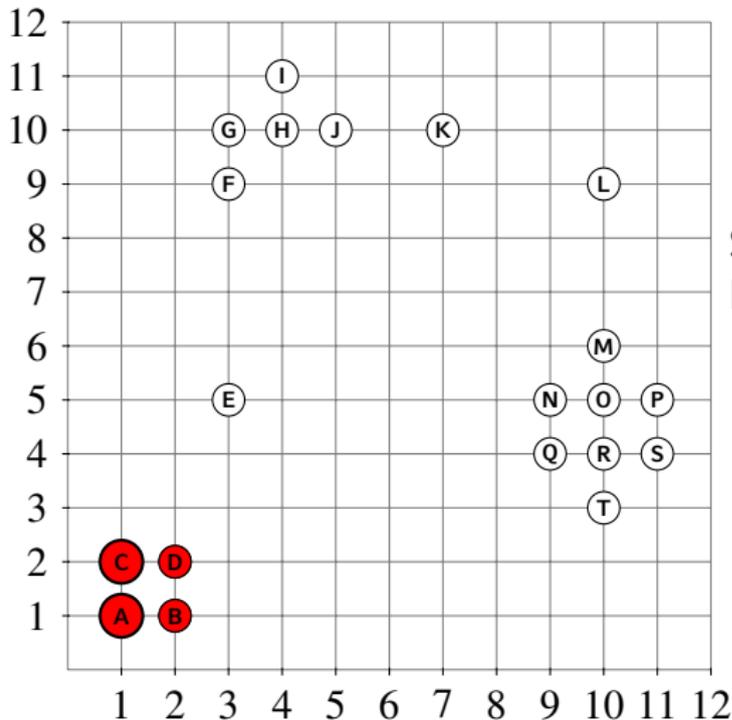
$$\epsilon = 1.1$$

$$\text{minPts} = 3$$

Seed list:

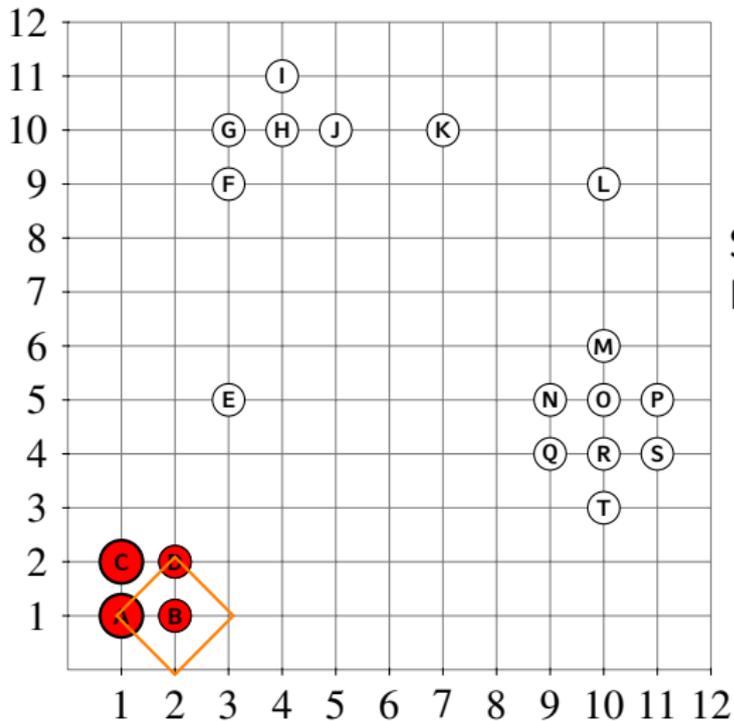
 $\epsilon = 1.1$ $\text{minPts} = 3$ Seed list:
BC



 $\epsilon = 1.1$ $\text{minPts} = 3$

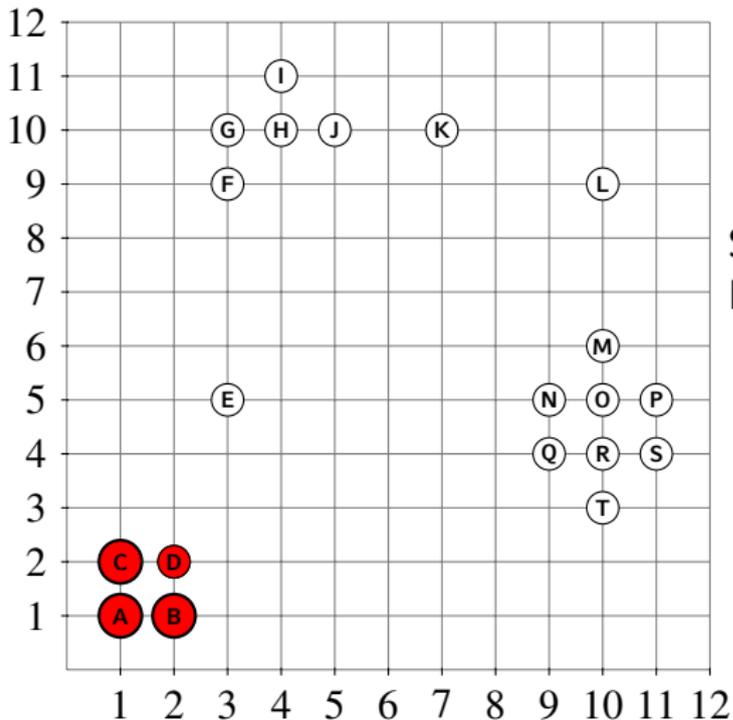
Seed list:

BD

 $\epsilon = 1.1$ $\text{minPts} = 3$

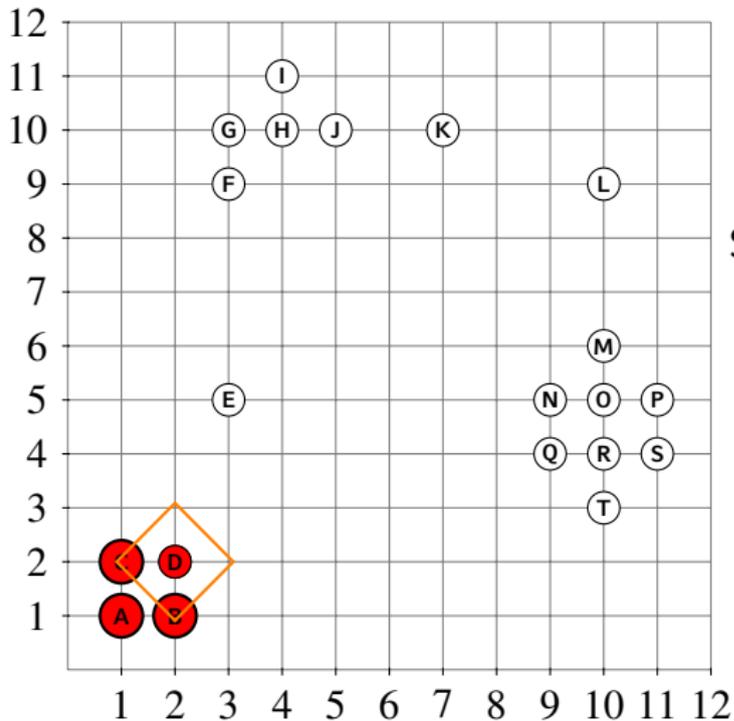
Seed list:

D

 $\epsilon = 1.1$ $\text{minPts} = 3$

Seed list:

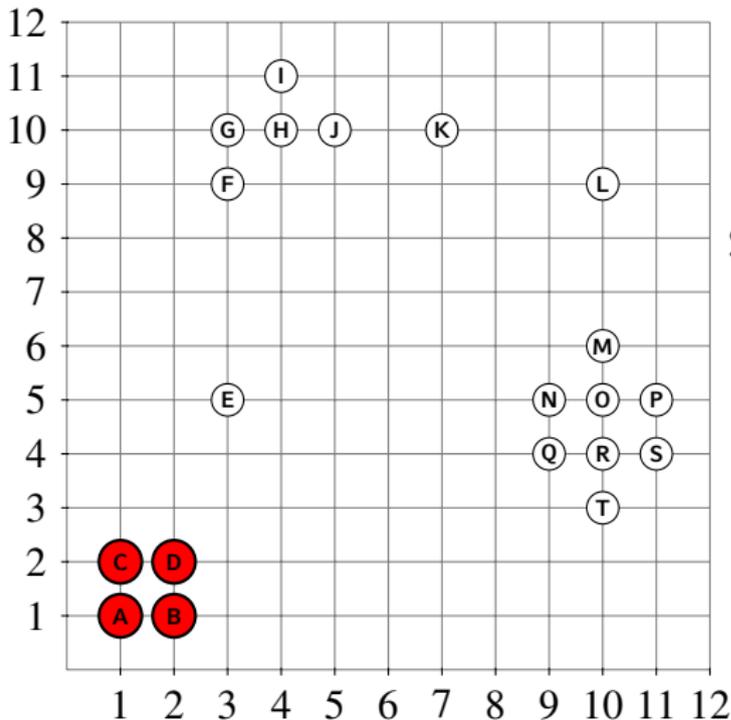
D



$$\epsilon = 1.1$$

$$\text{minPts} = 3$$

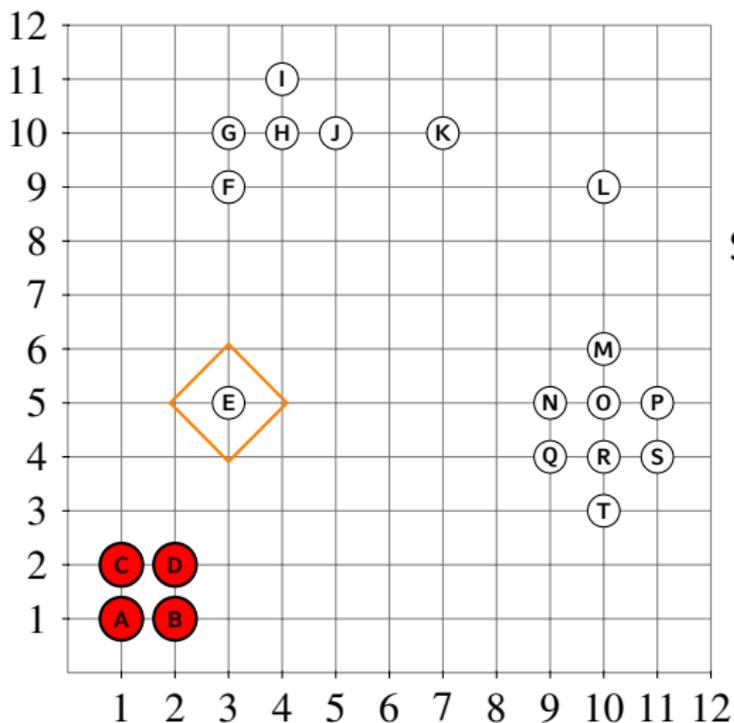
Seed list:



$$\epsilon = 1.1$$

$$\text{minPts} = 3$$

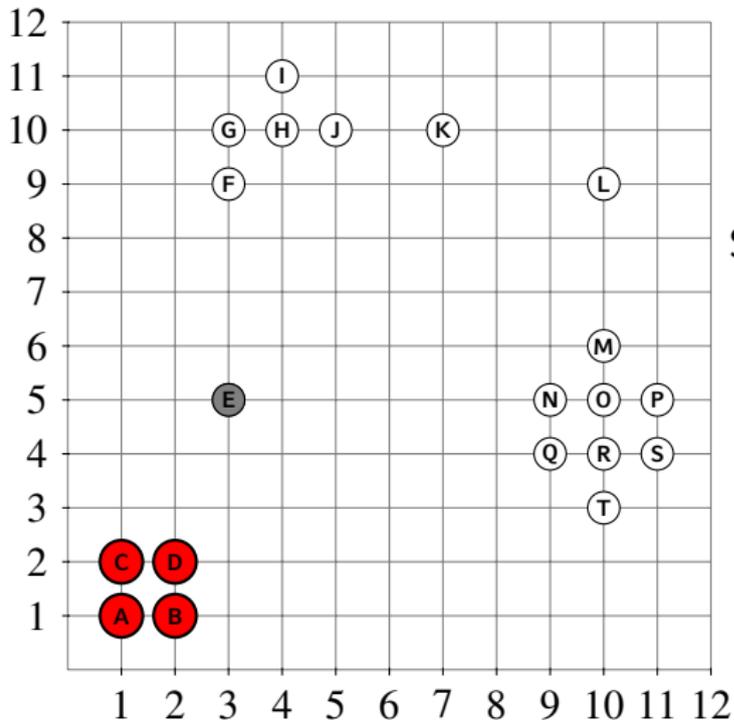
Seed list:



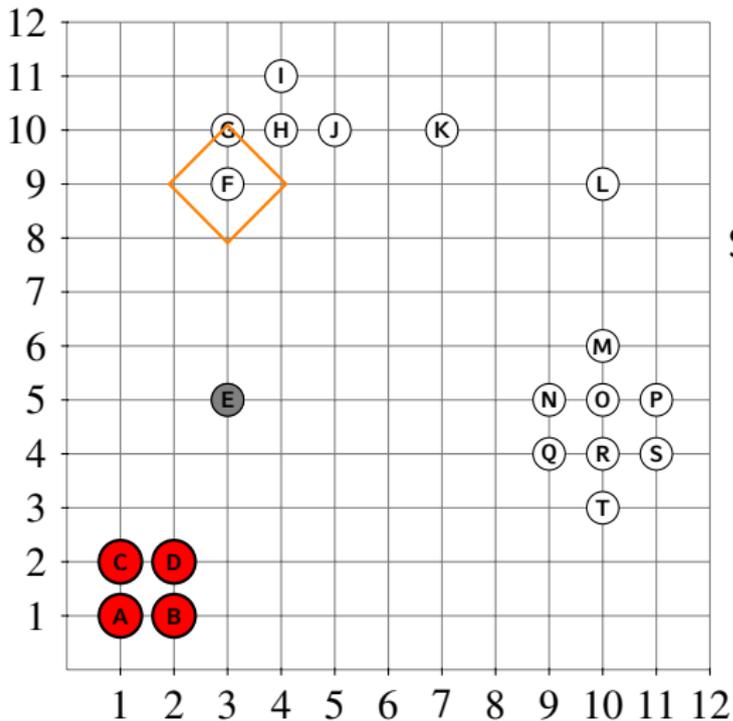
$\epsilon = 1.1$

$\text{minPts} = 3$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 3$

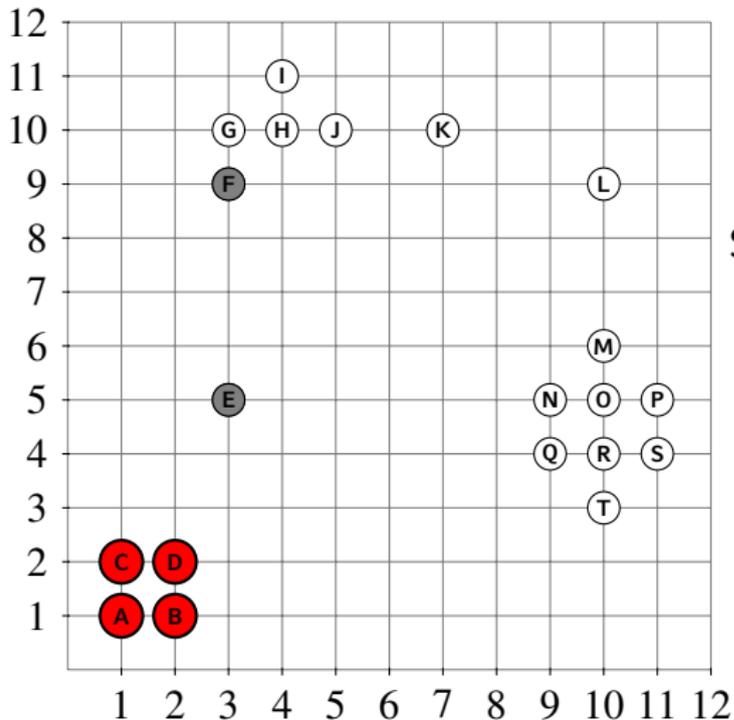
Seed list:



$\epsilon = 1.1$

$\text{minPts} = 3$

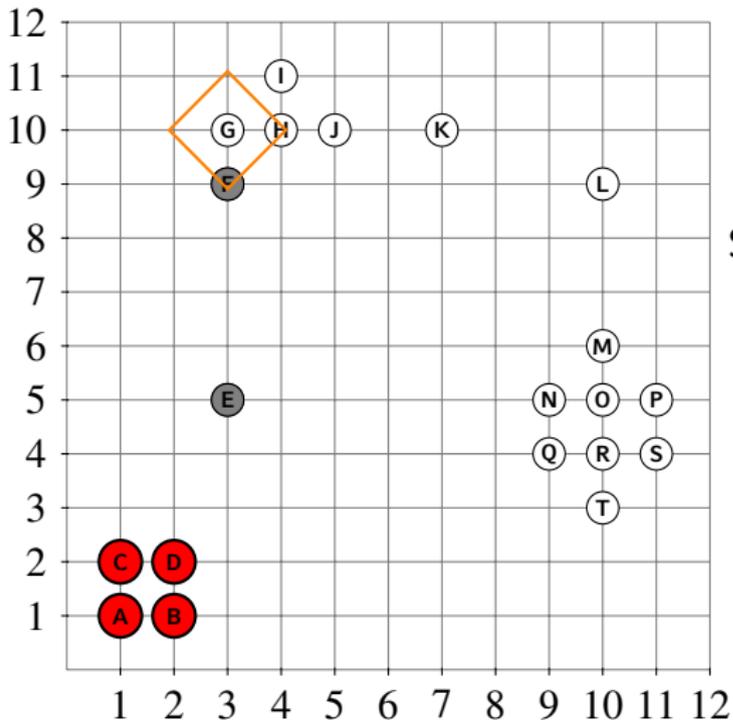
Seed list:



$\epsilon = 1.1$

$\text{minPts} = 3$

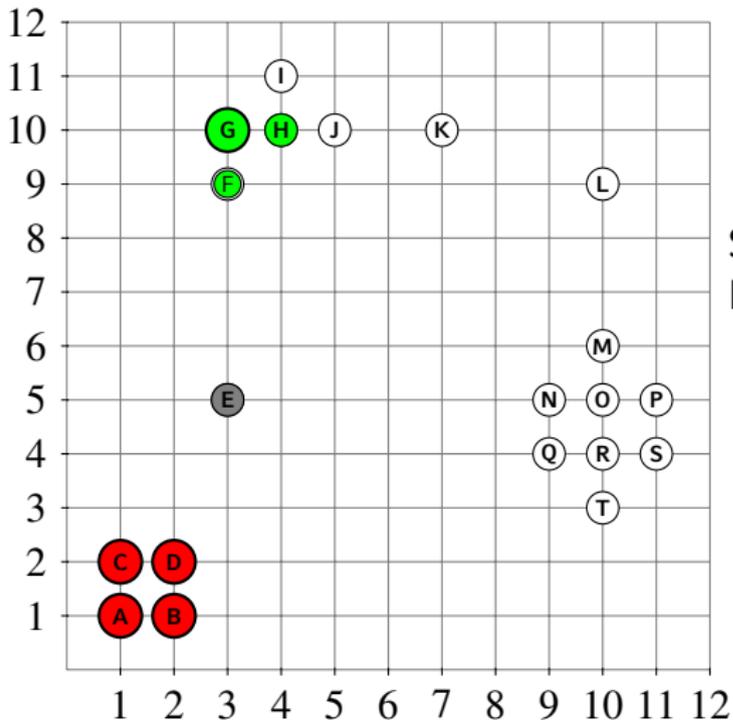
Seed list:

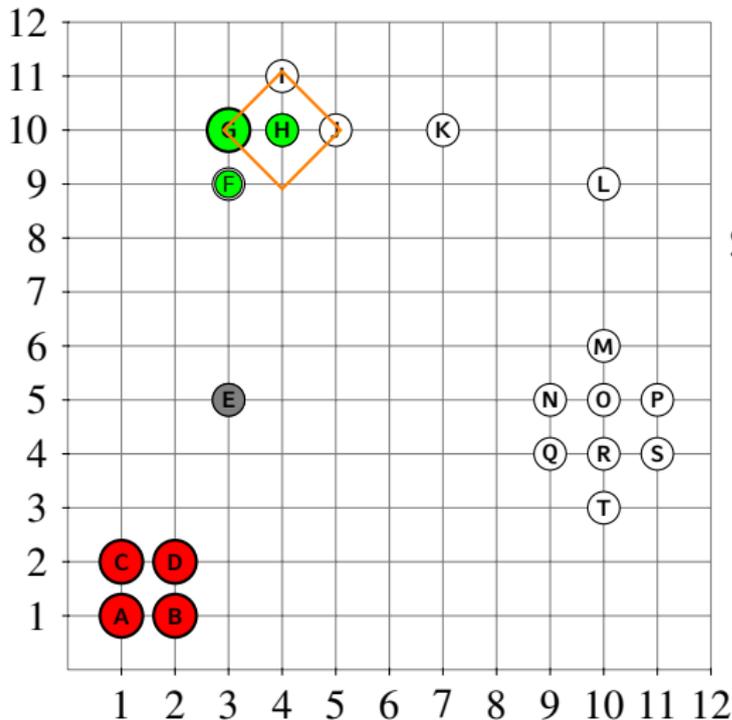


$\epsilon = 1.1$

$\text{minPts} = 3$

Seed list:

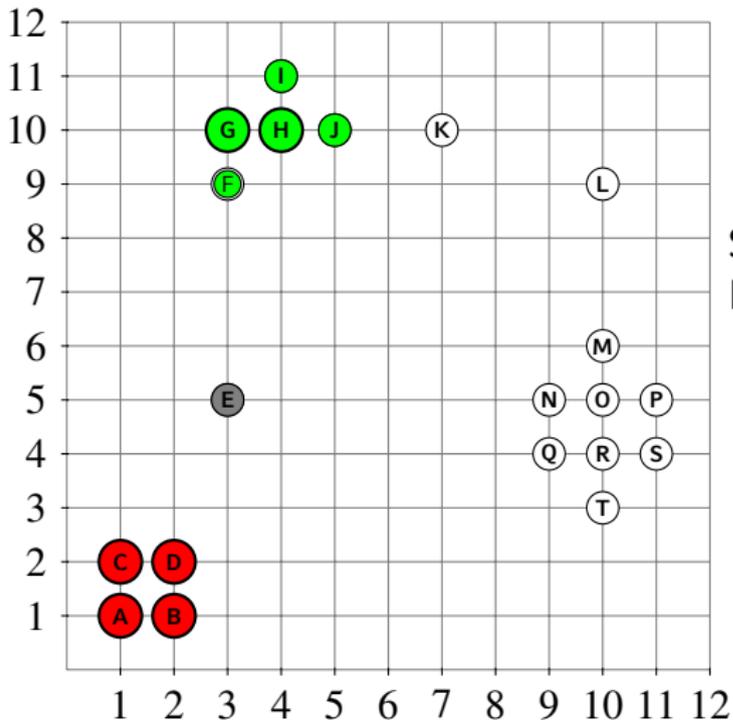


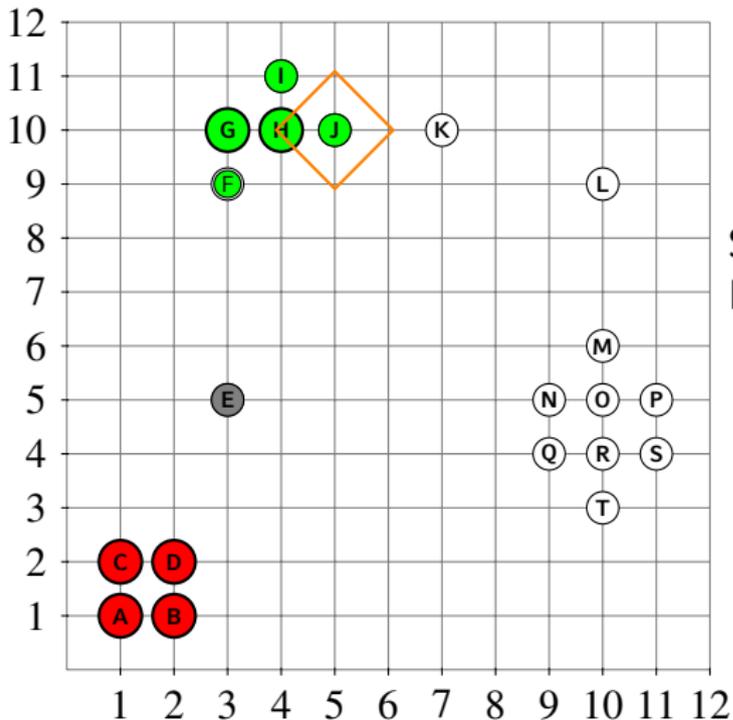


$$\epsilon = 1.1$$

$$\text{minPts} = 3$$

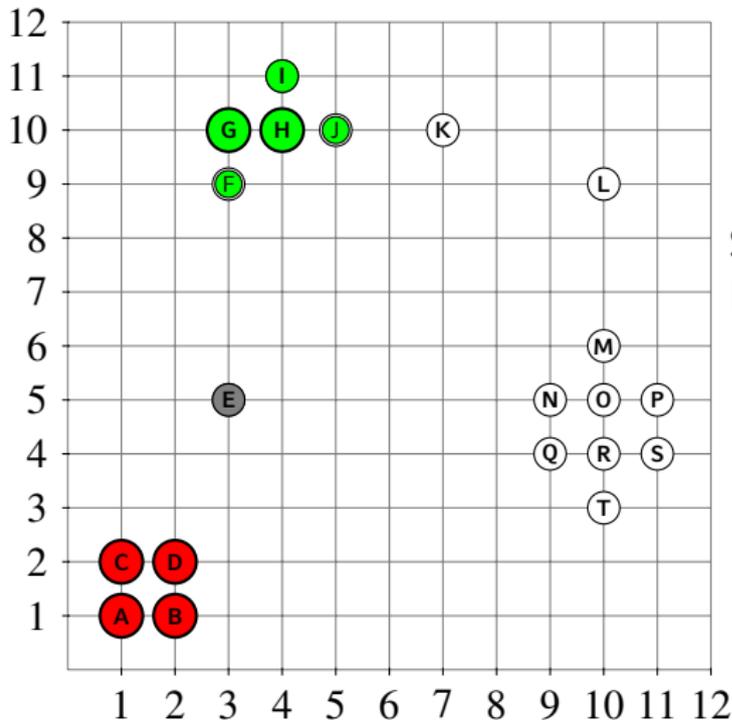
Seed list:



 $\epsilon = 1.1$ $\text{minPts} = 3$

Seed list:

I

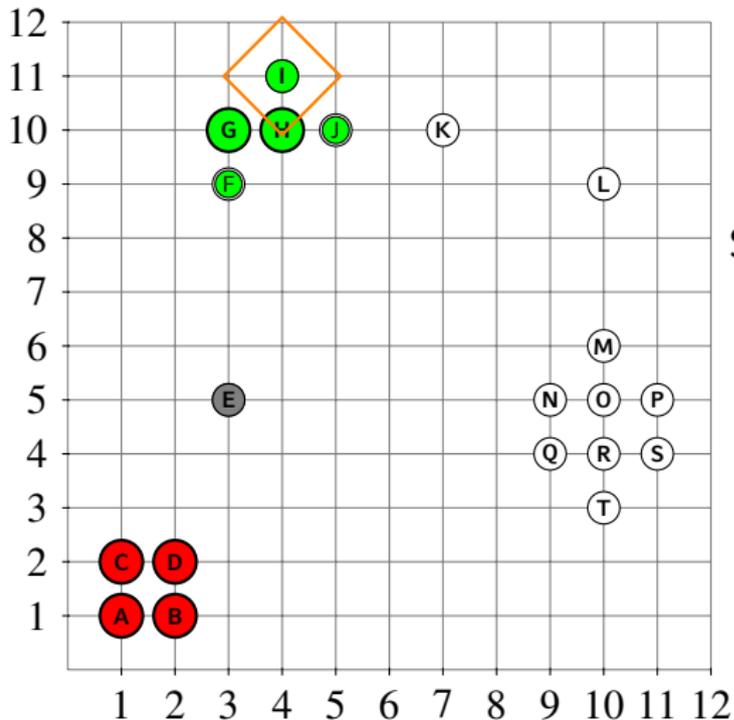


$\epsilon = 1.1$

$minPts = 3$

Seed list:

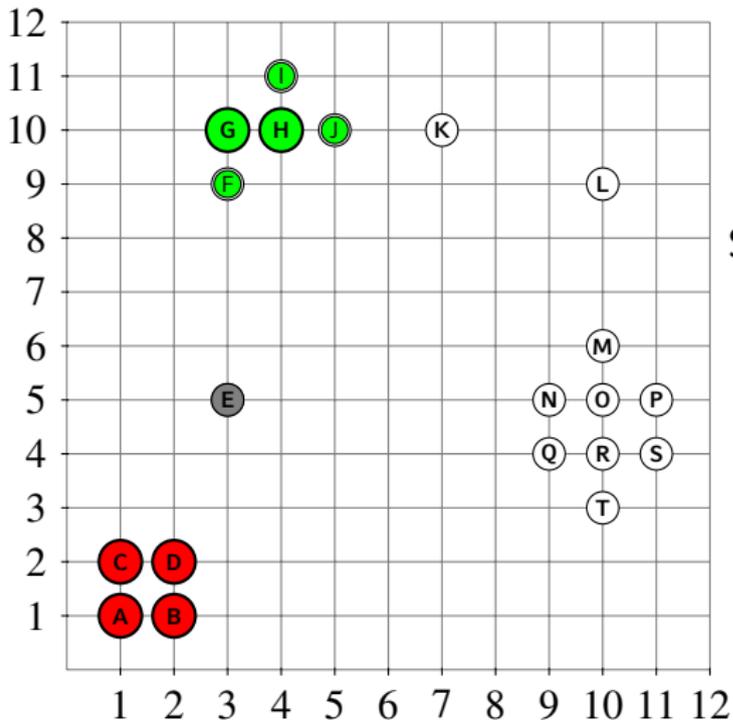
I



$$\epsilon = 1.1$$

$$\text{minPts} = 3$$

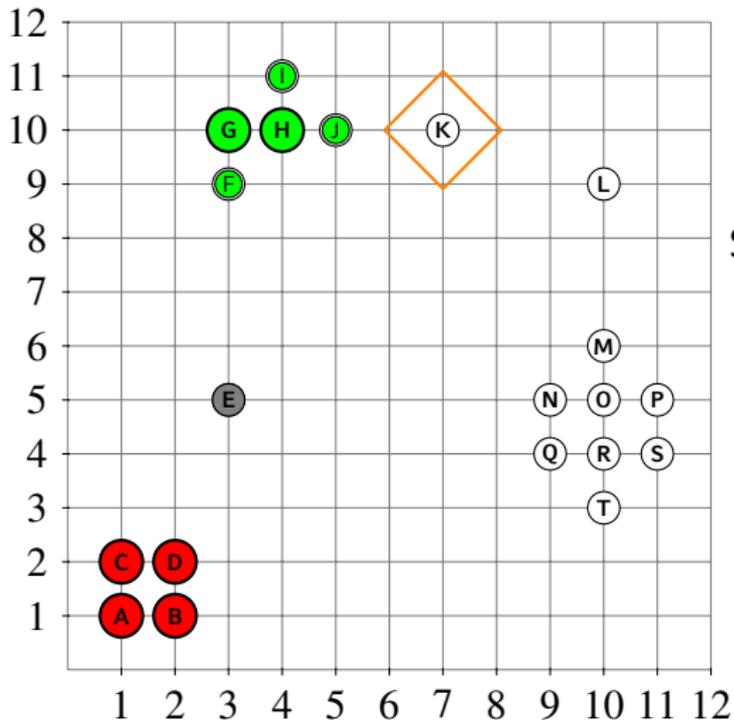
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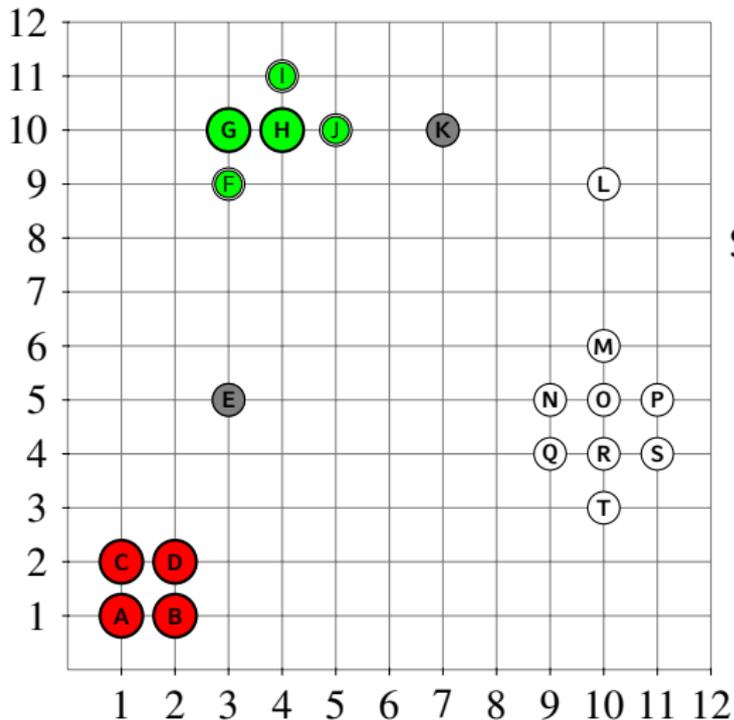
$$\epsilon = 1.1$$

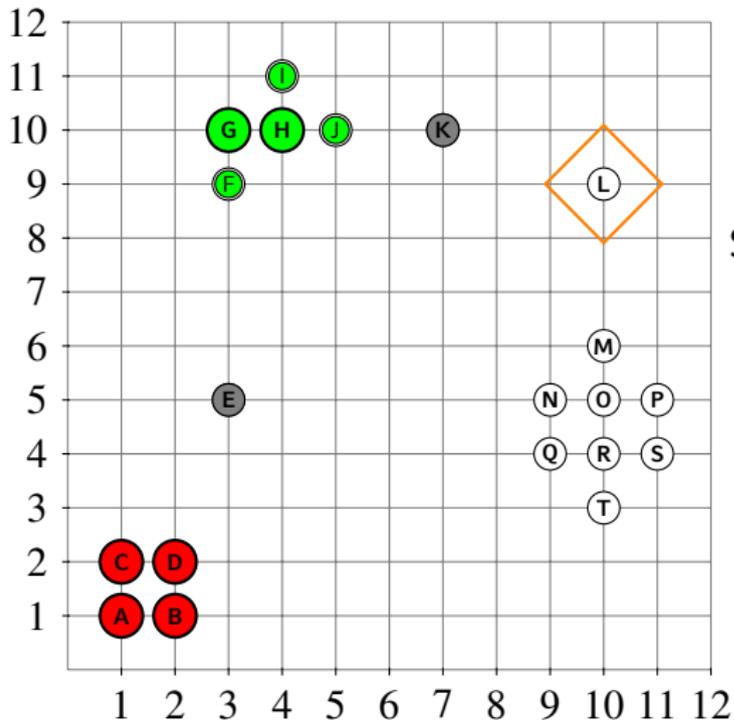
$$\text{minPts} = 3$$

Seed list:

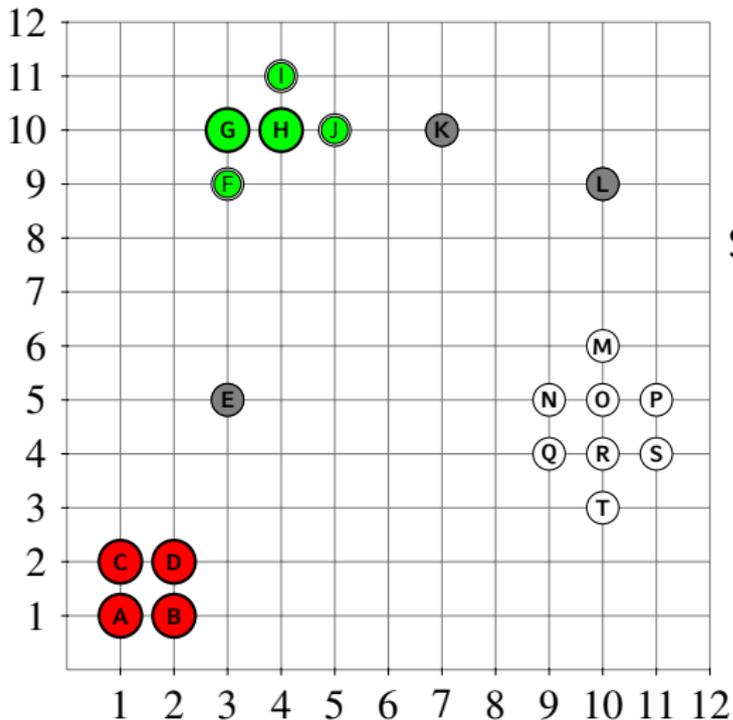
 $\epsilon = 1.1$ $\text{minPts} = 3$

Seed list:



 $\epsilon = 1.1$ $\text{minPts} = 3$

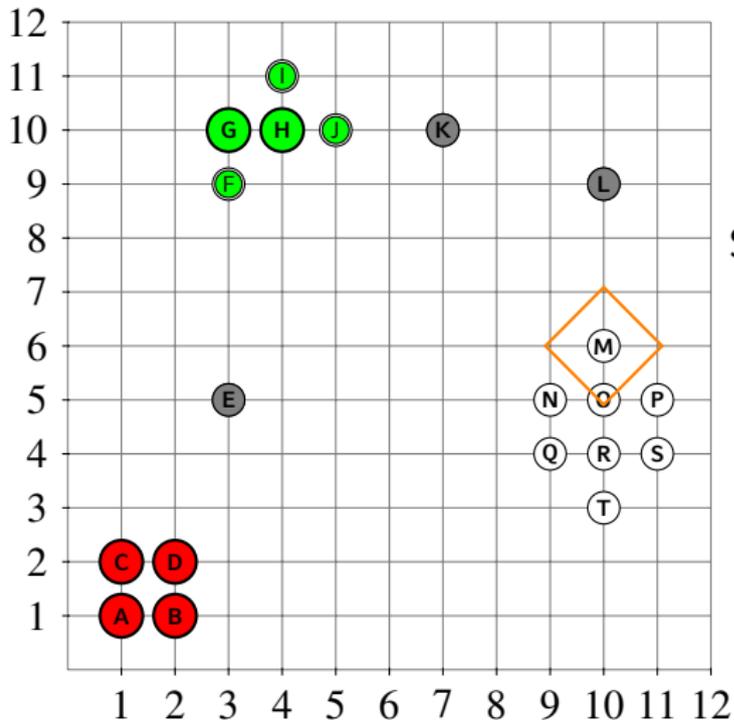
Seed list:



$$\epsilon = 1.1$$

$$\text{minPts} = 3$$

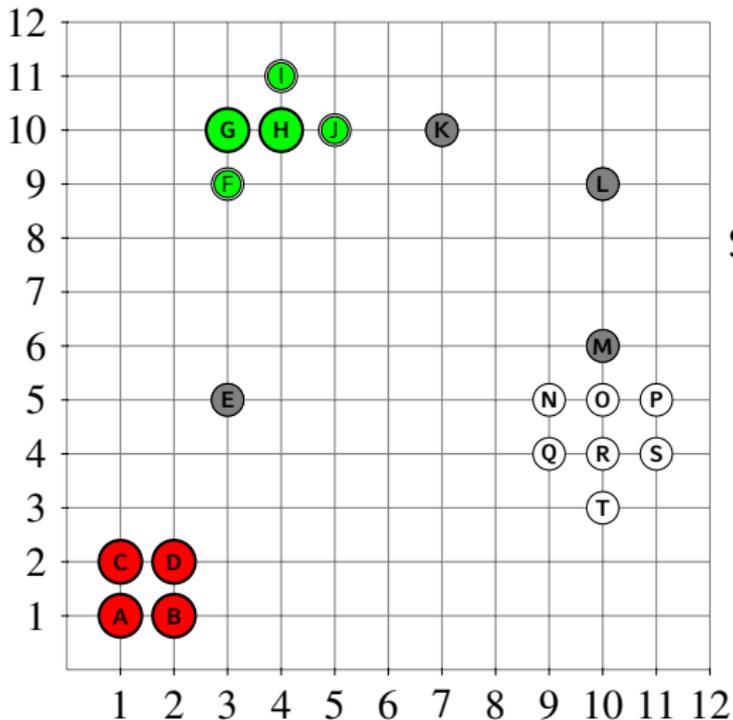
Seed list:



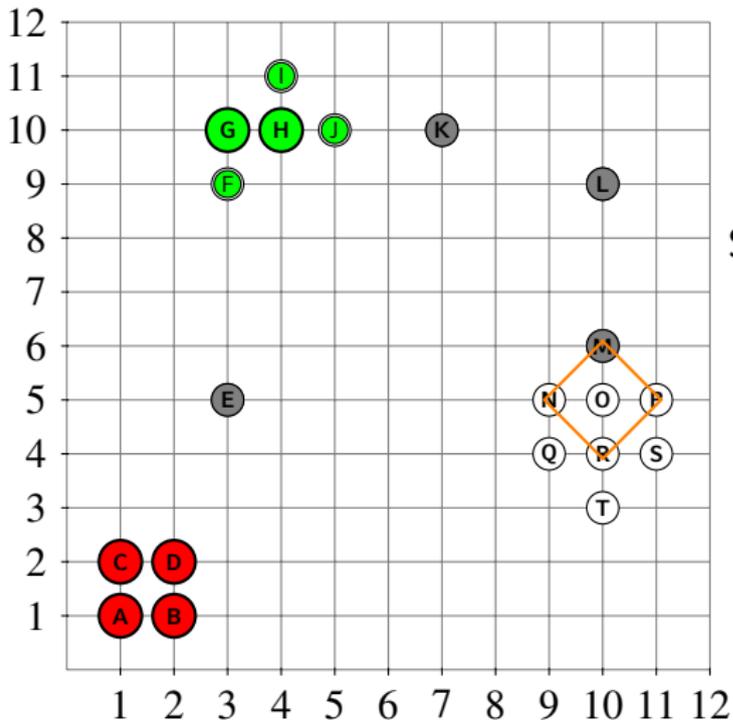
$\epsilon = 1.1$

$minPts = 3$

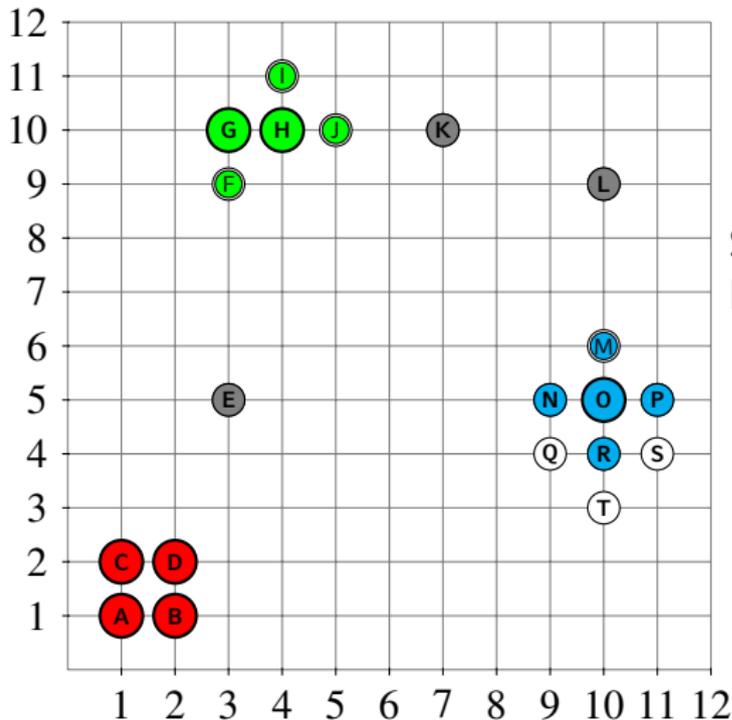
Seed list:

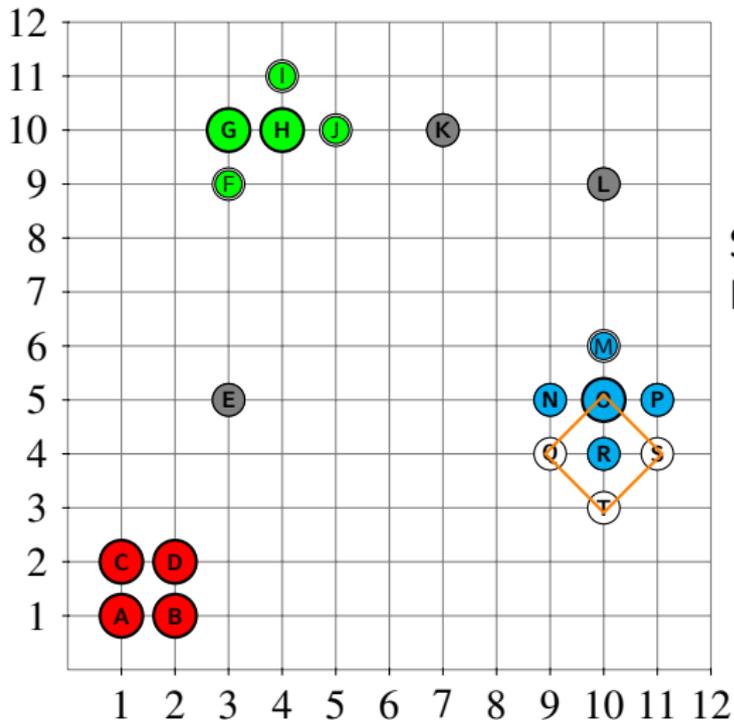
 $\epsilon = 1.1$ $\text{minPts} = 3$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 3$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 3$ Seed list:
NPR

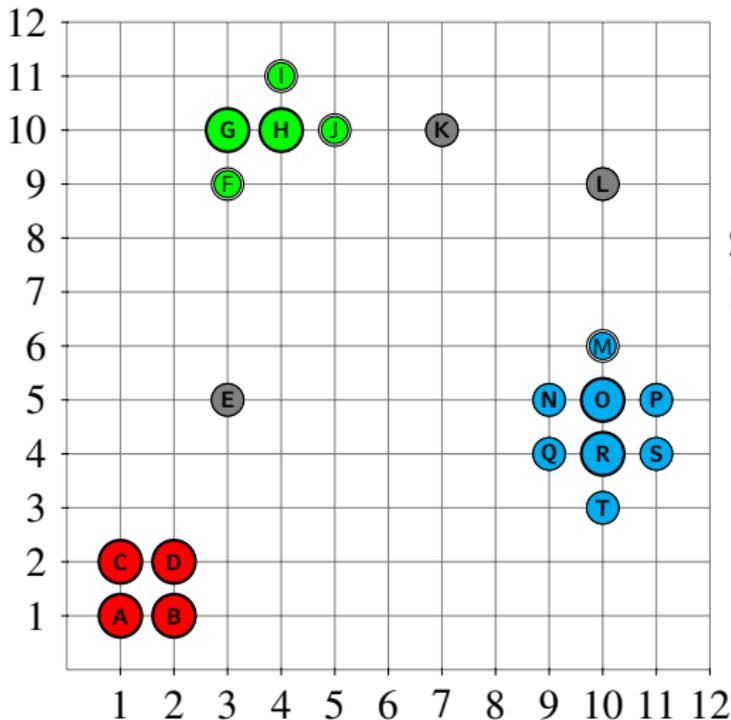


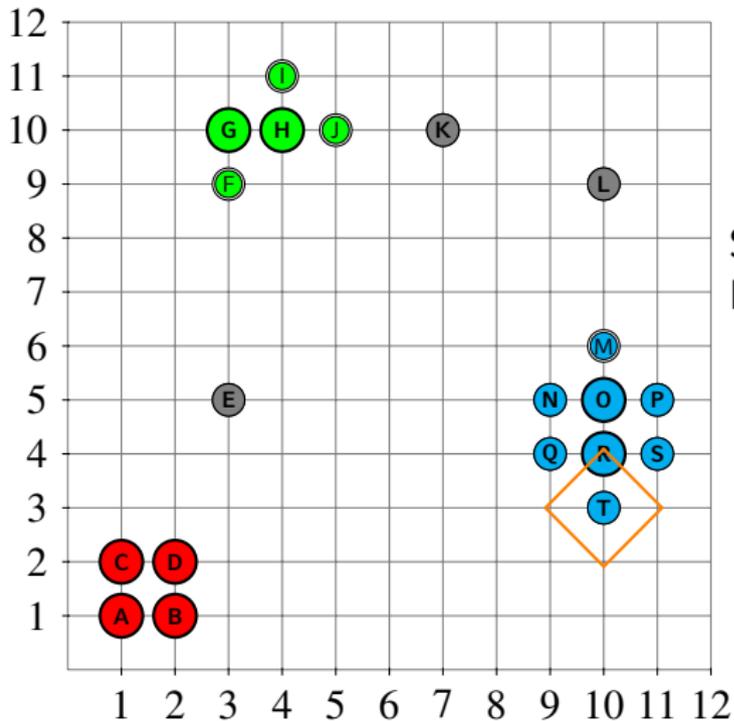
$\epsilon = 1.1$

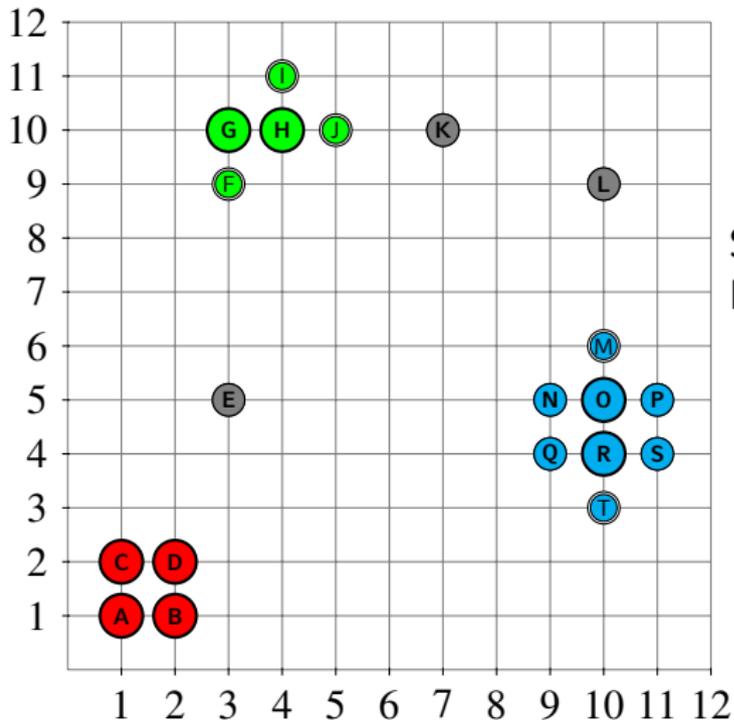
$minPts = 3$

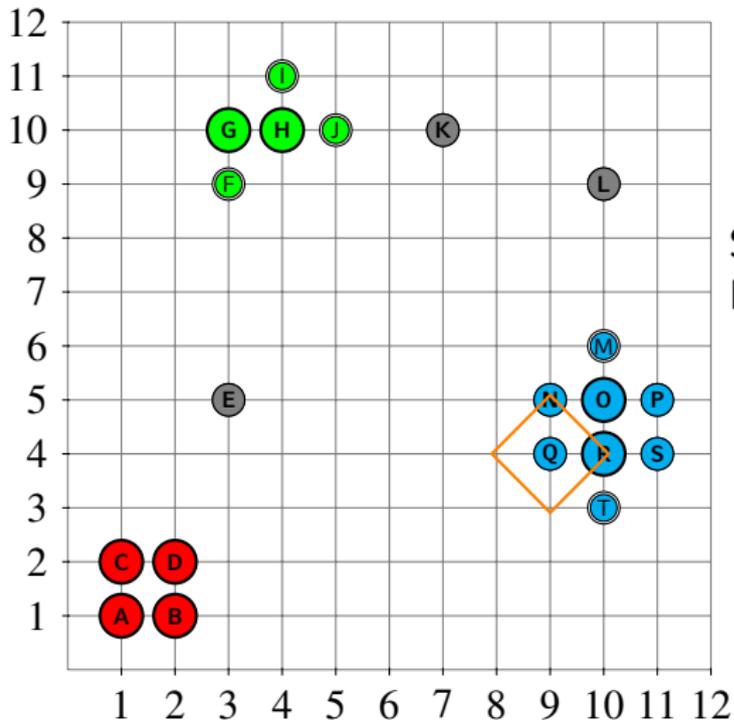
Seed list:

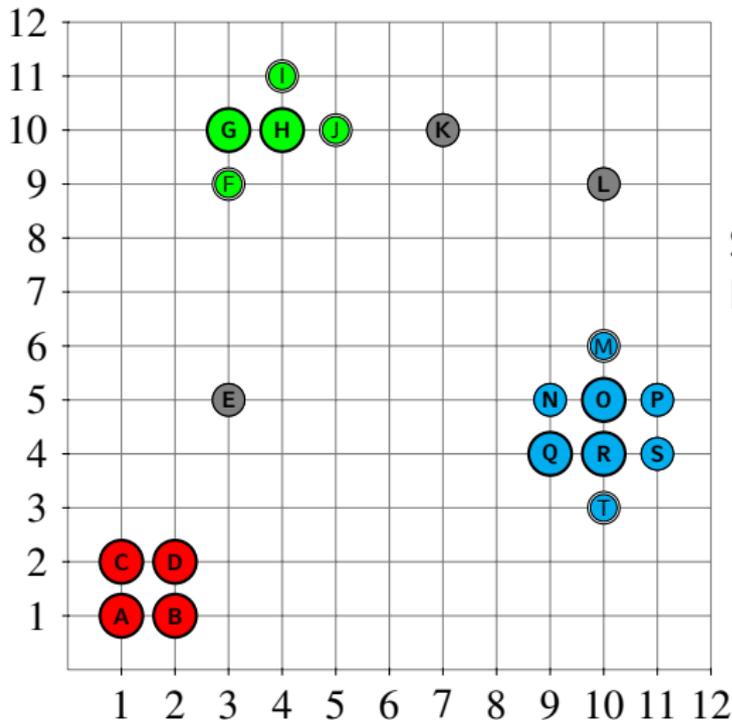
NP

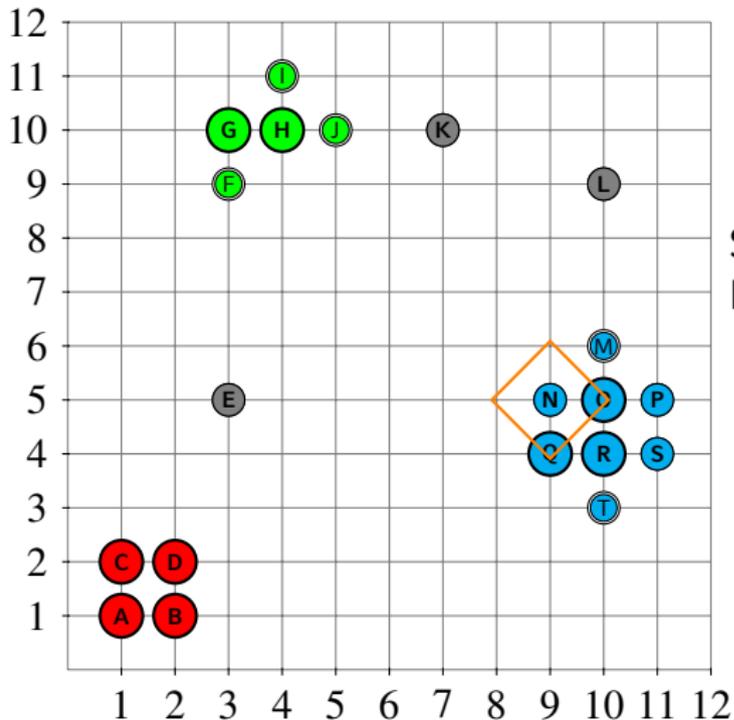
 $\epsilon = 1.1$ $\text{minPts} = 3$ Seed list:
NPQST

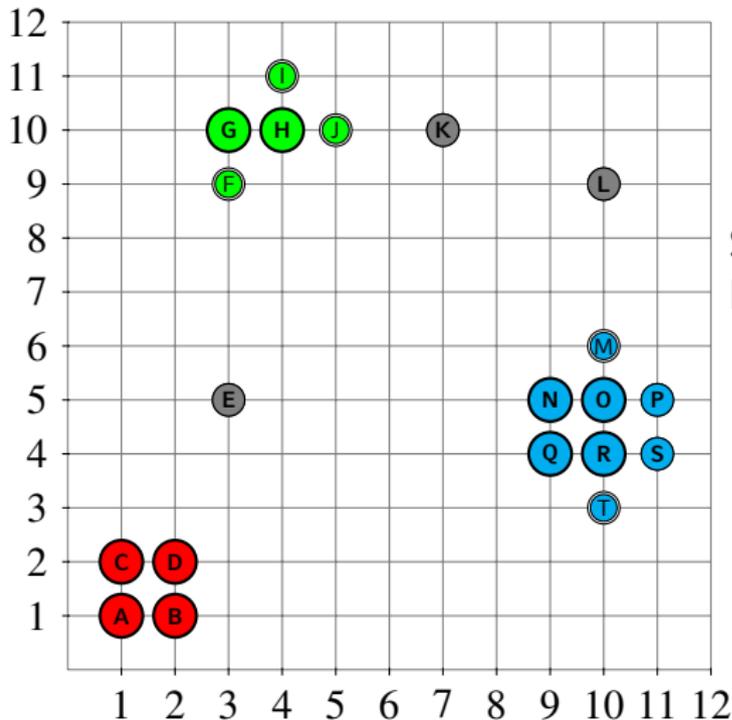
 $\epsilon = 1.1$ $\text{minPts} = 3$ Seed list:
NPQS

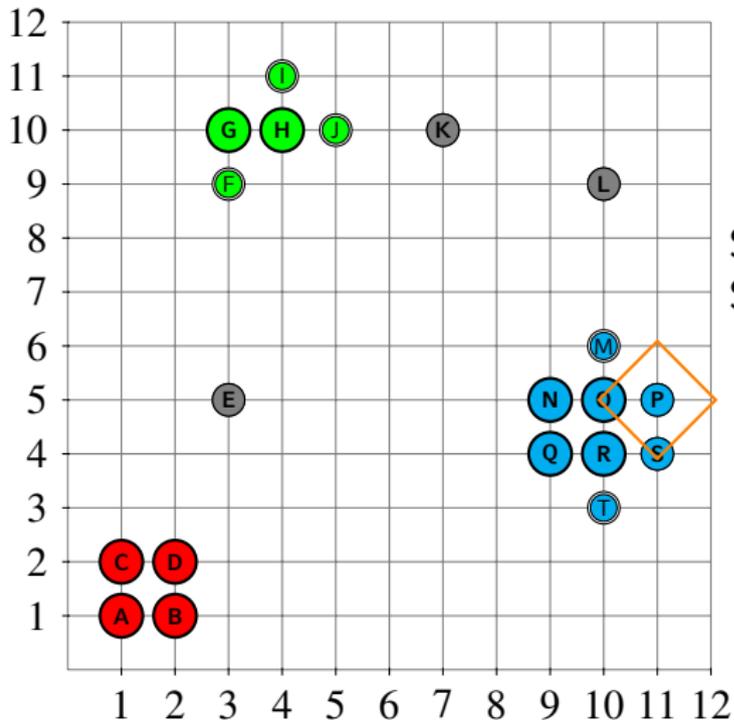
 $\epsilon = 1.1$ $\text{minPts} = 3$ Seed list:
NPQS

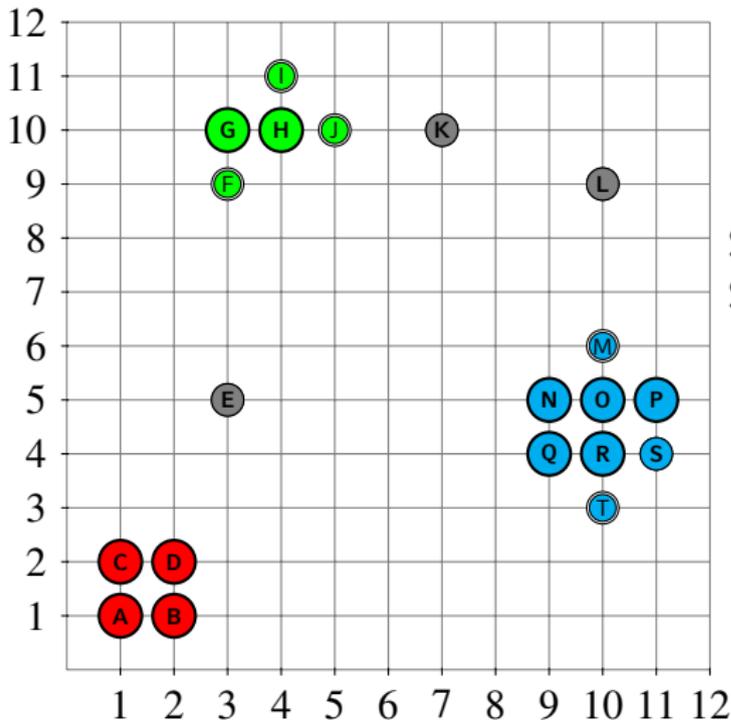
 $\epsilon = 1.1$ $\text{minPts} = 3$ Seed list:
NPS

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NPS

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PS

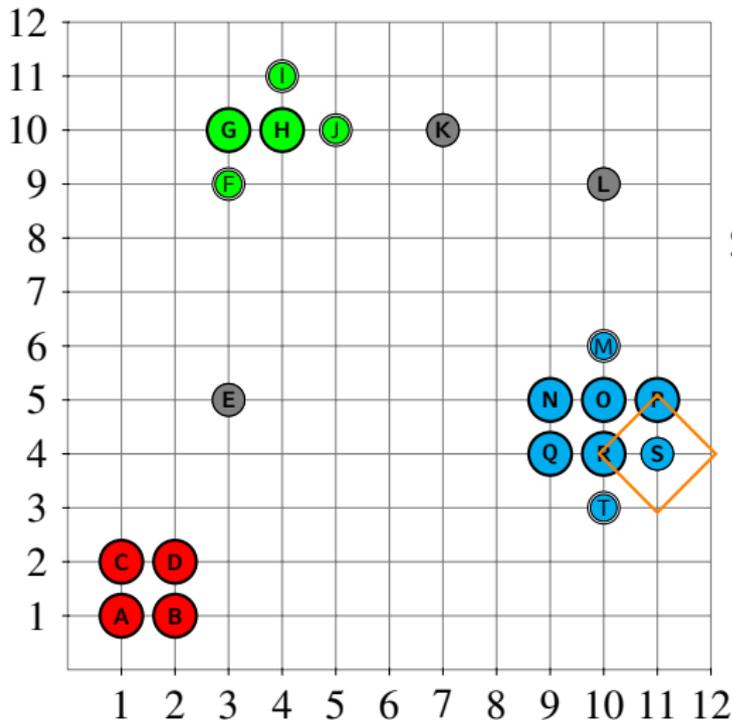
 $\epsilon = 1.1$ $\text{minPts} = 3$ Seed list:
PS

 $\epsilon = 1.1$ $\text{minPts} = 3$ Seed list:
S

 $\epsilon = 1.1$ $\text{minPts} = 3$

Seed list:

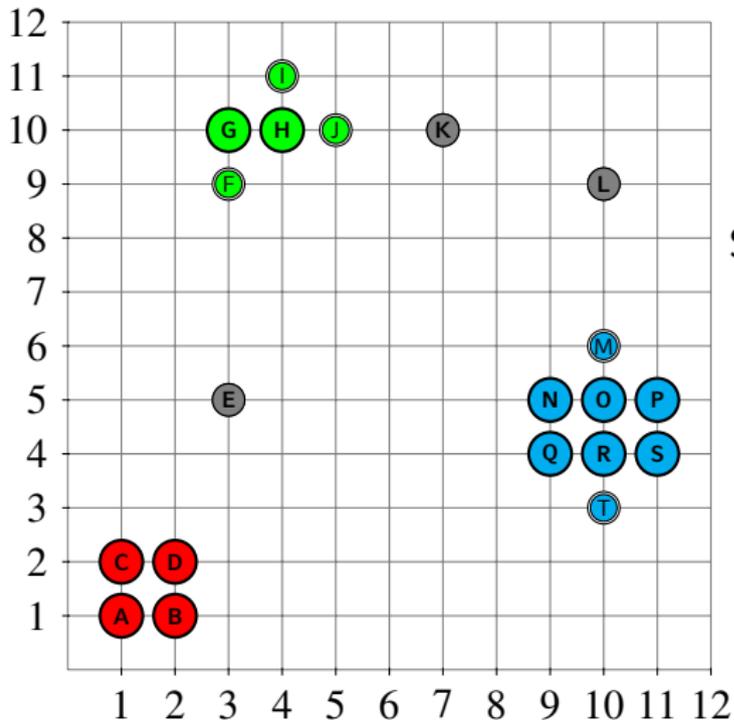
S



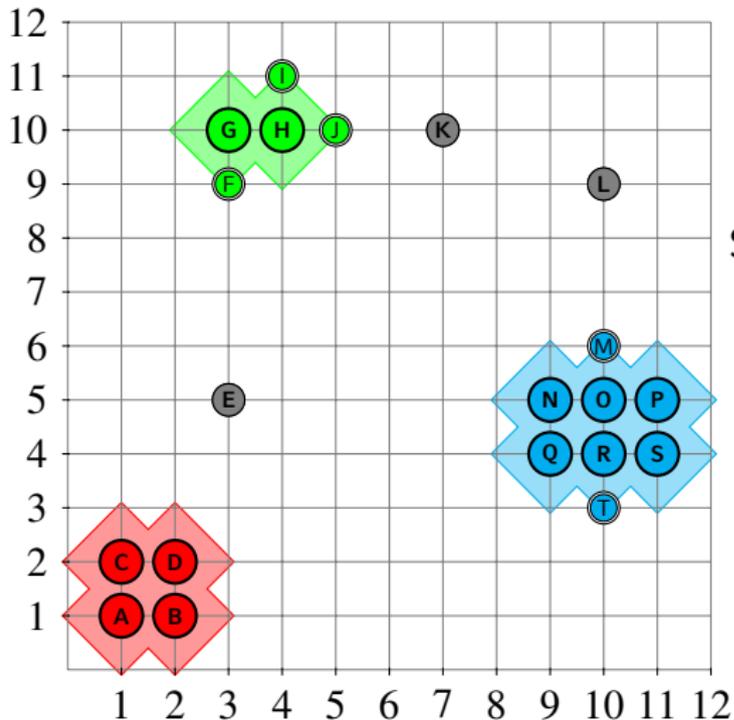
$$\epsilon = 1.1$$

$$\text{minPts} = 3$$

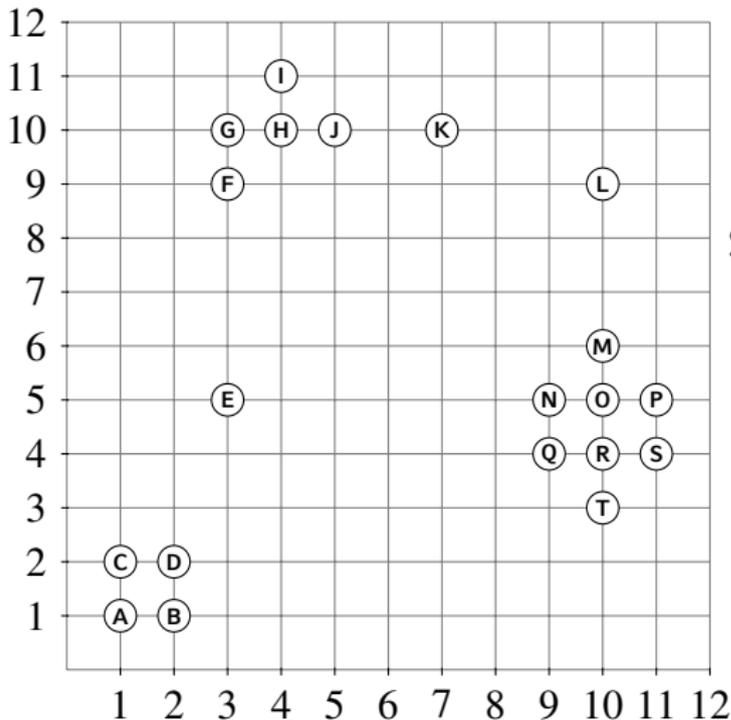
Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 3$

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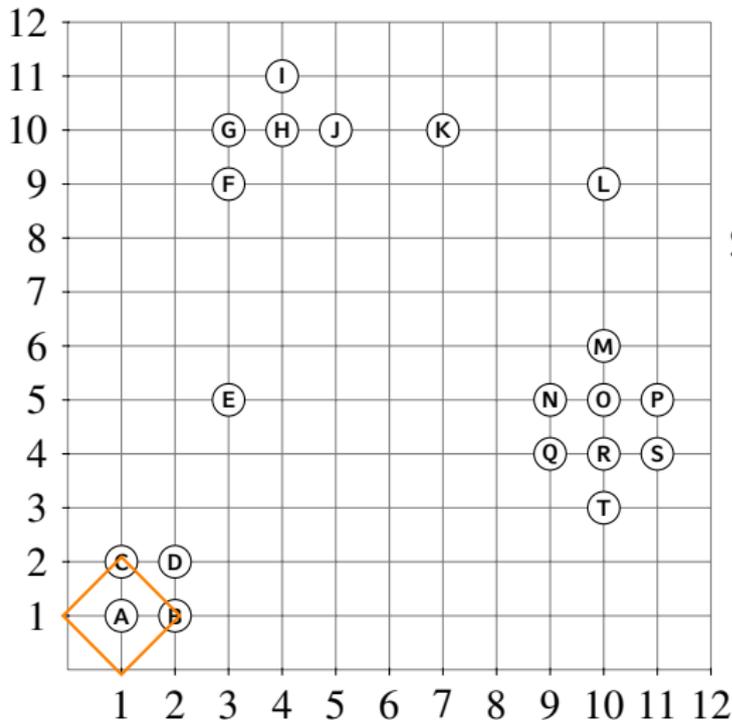
Seed list:



$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

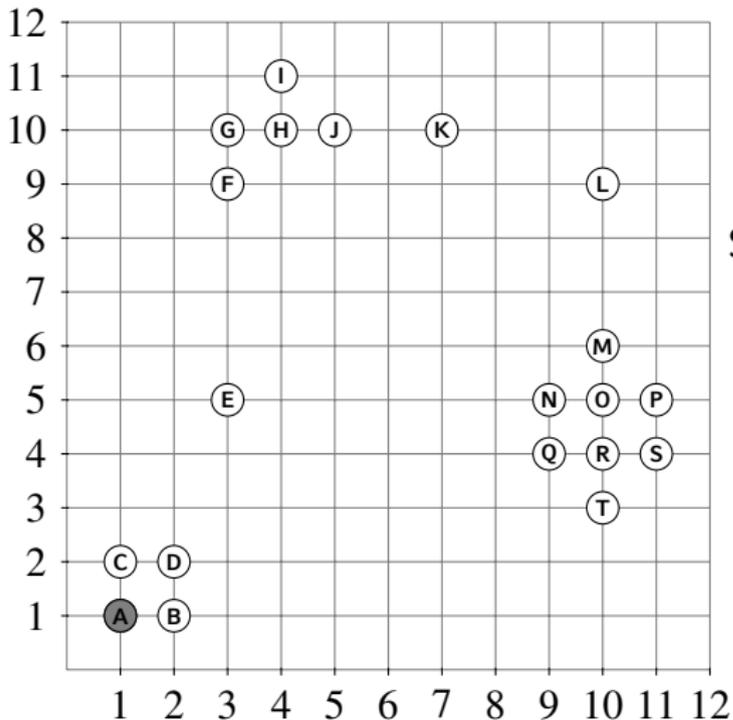
Seed list:



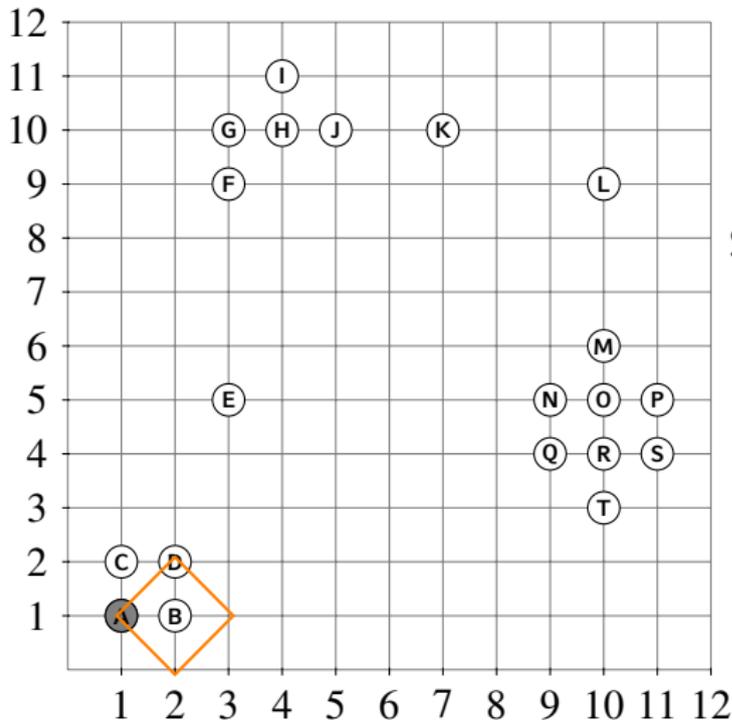
$\epsilon = 1.1$

$\text{minPts} = 4$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 4$

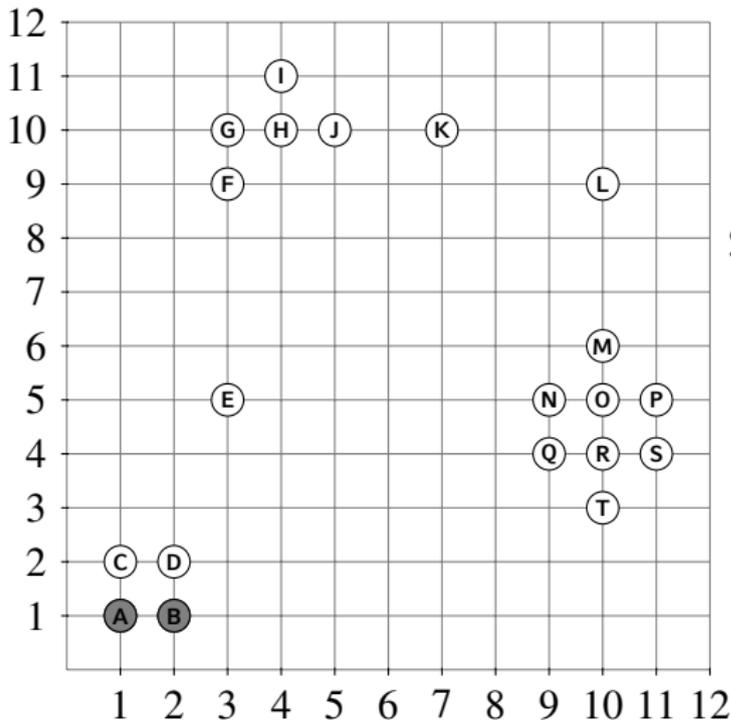
Seed list:



$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

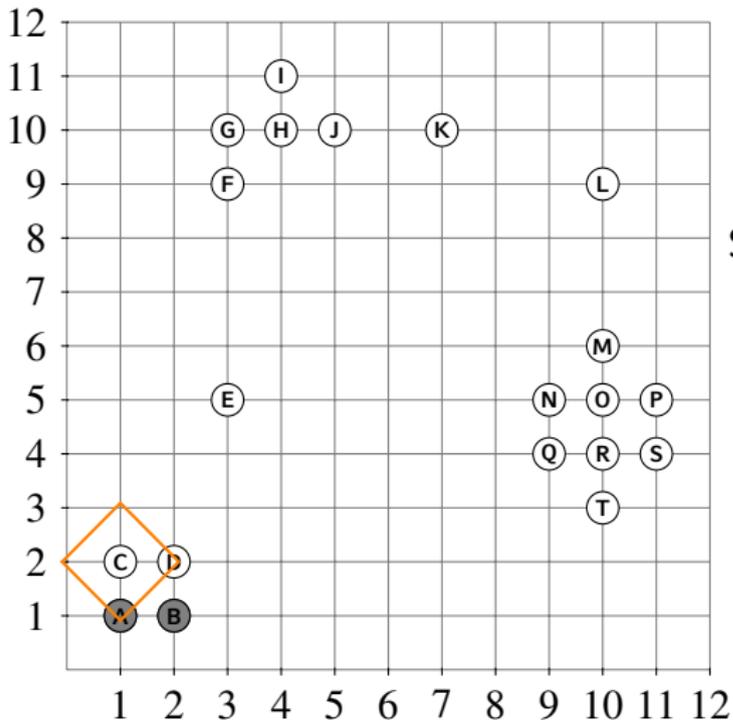
Seed list:



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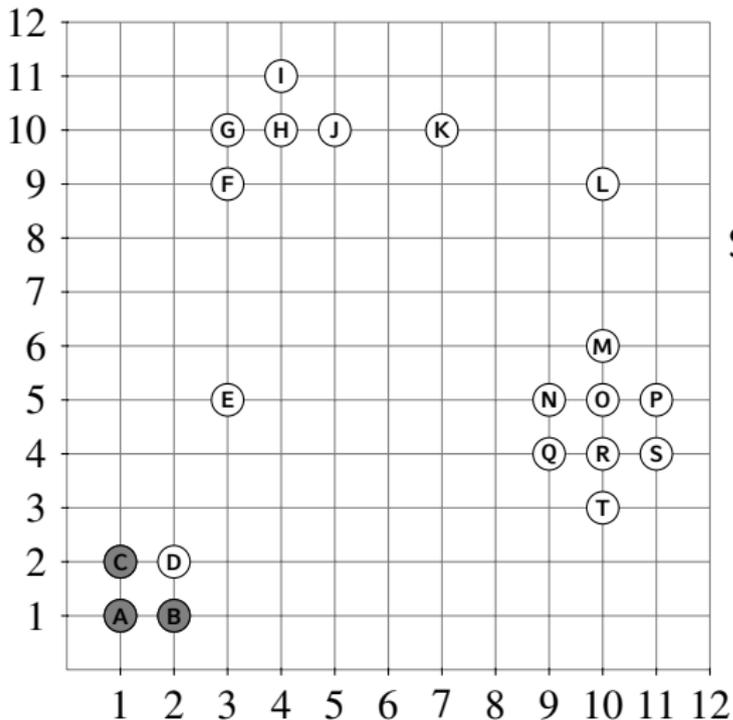
Seed list:



$\epsilon = 1.1$

$\text{minPts} = 4$

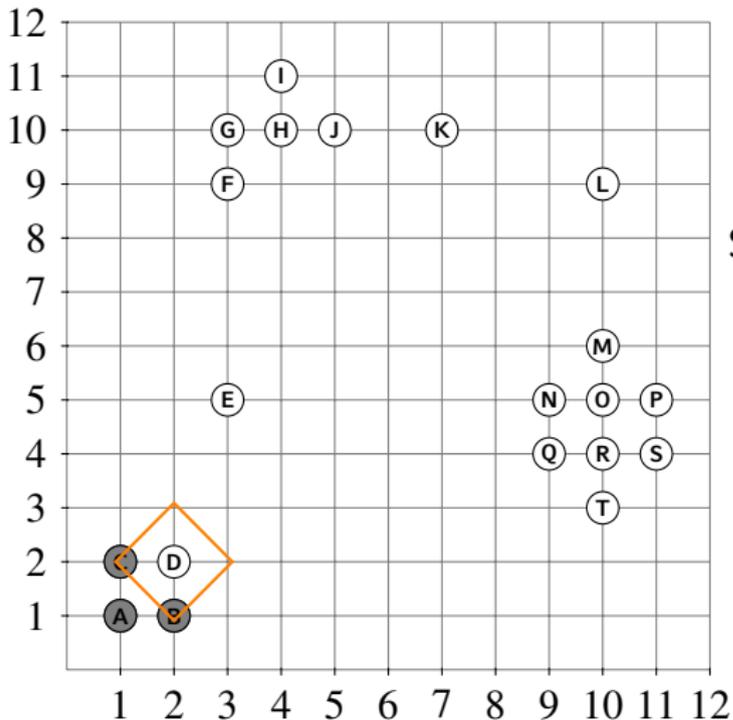
Seed list:



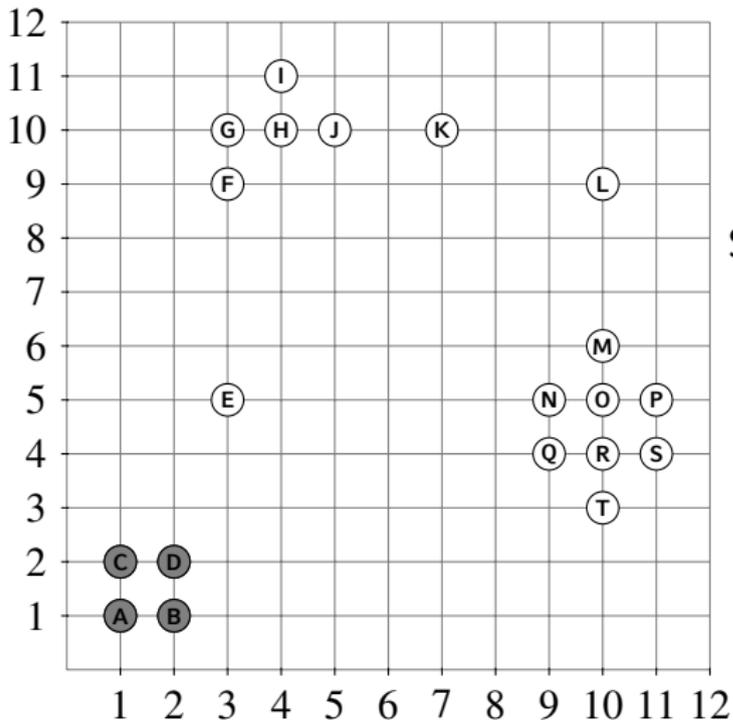
$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 4$

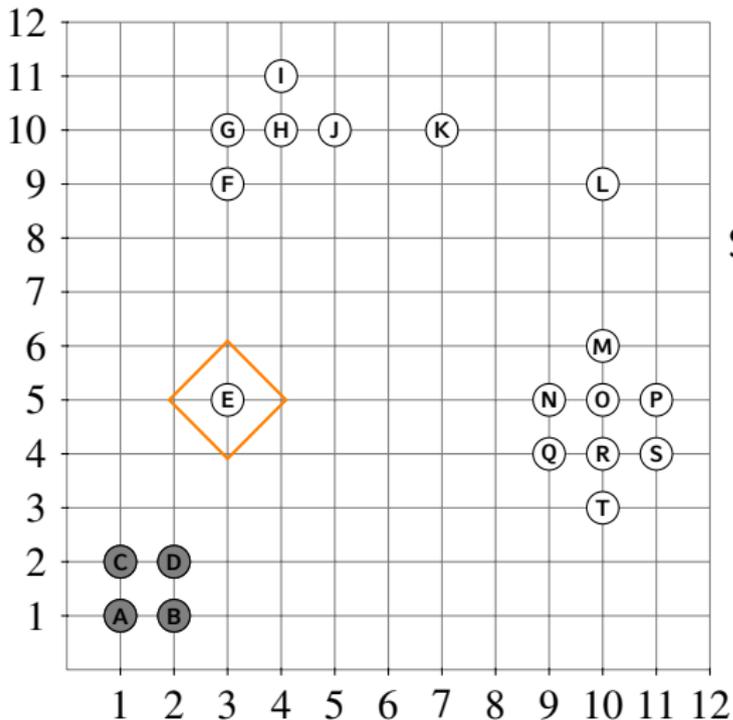
Seed list:



$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

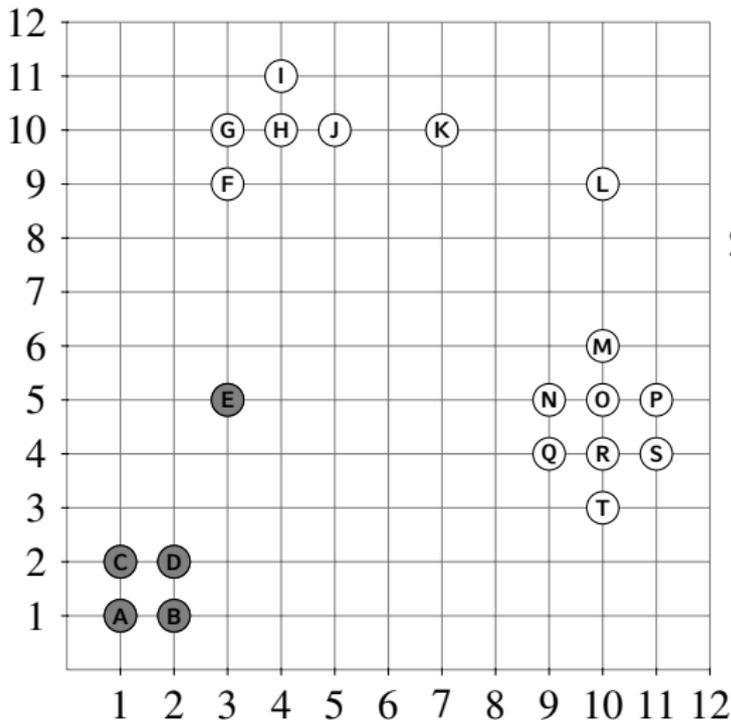
Seed list:



$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

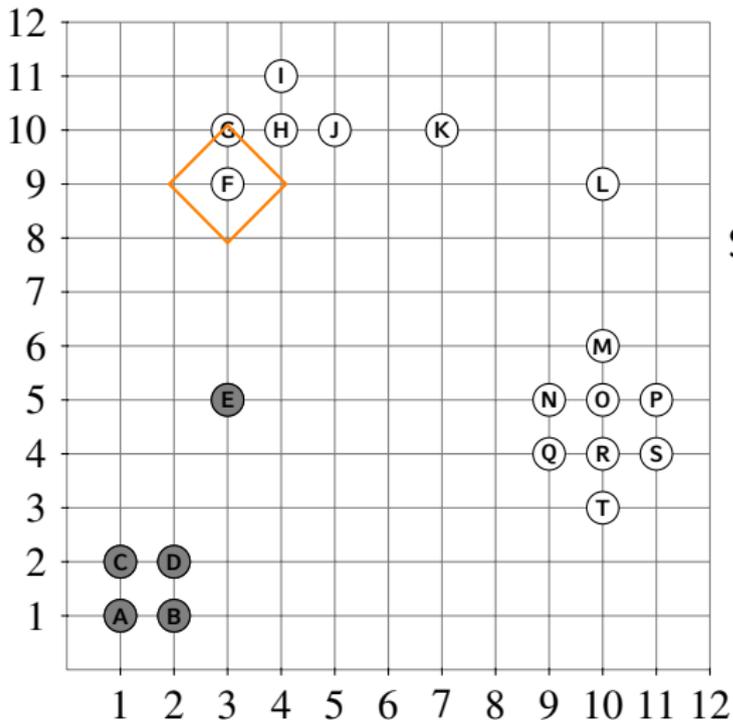
Seed list:



$$\epsilon = 1.1$$

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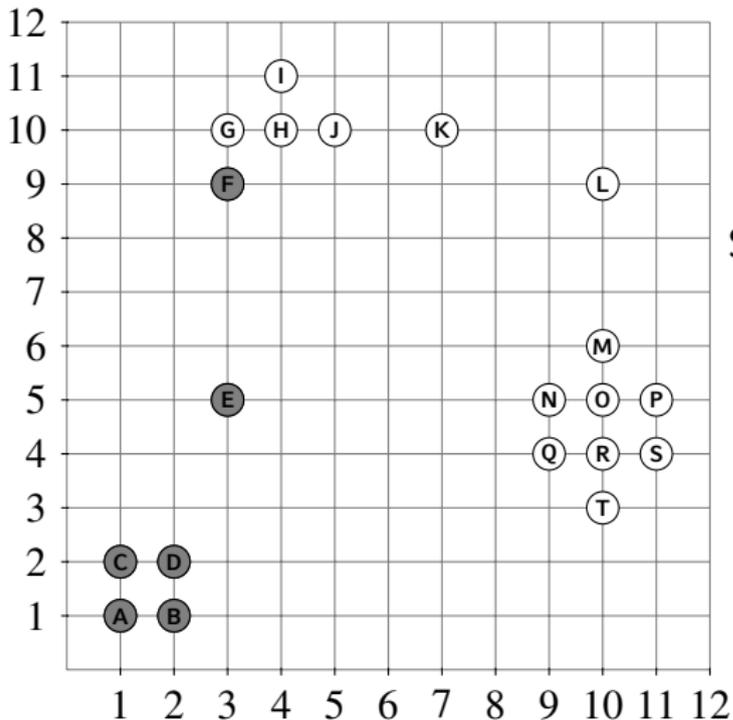
Seed list:



$$\epsilon = 1.1$$

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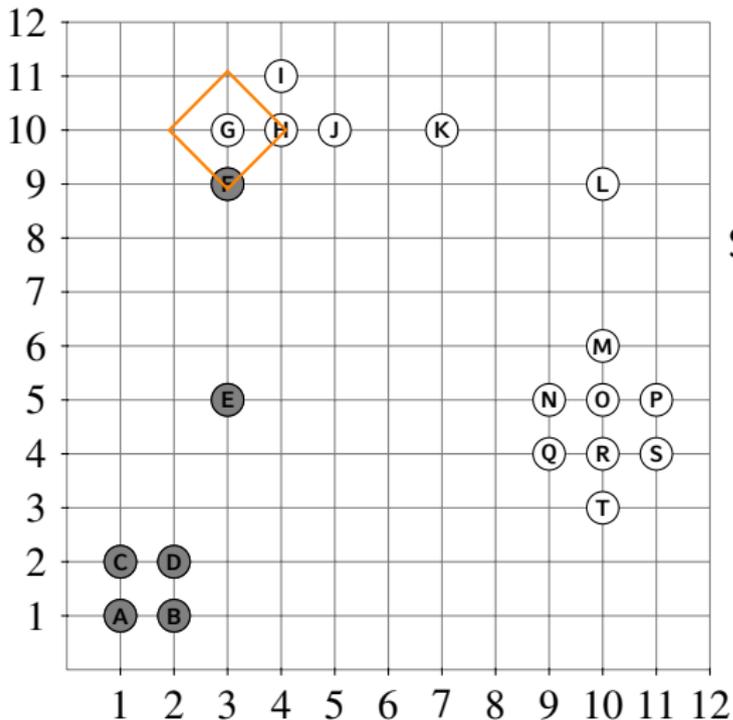
Seed list:



$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

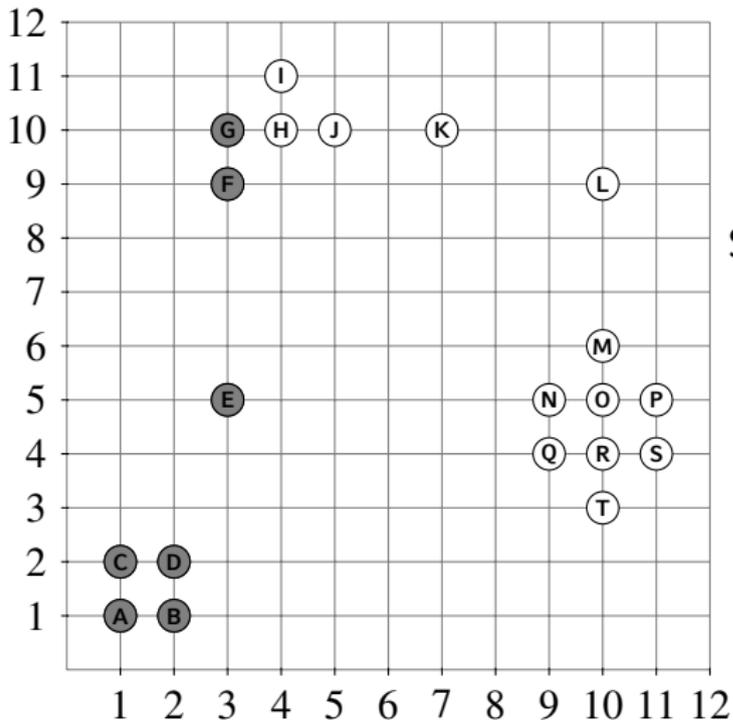
Seed list:



$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

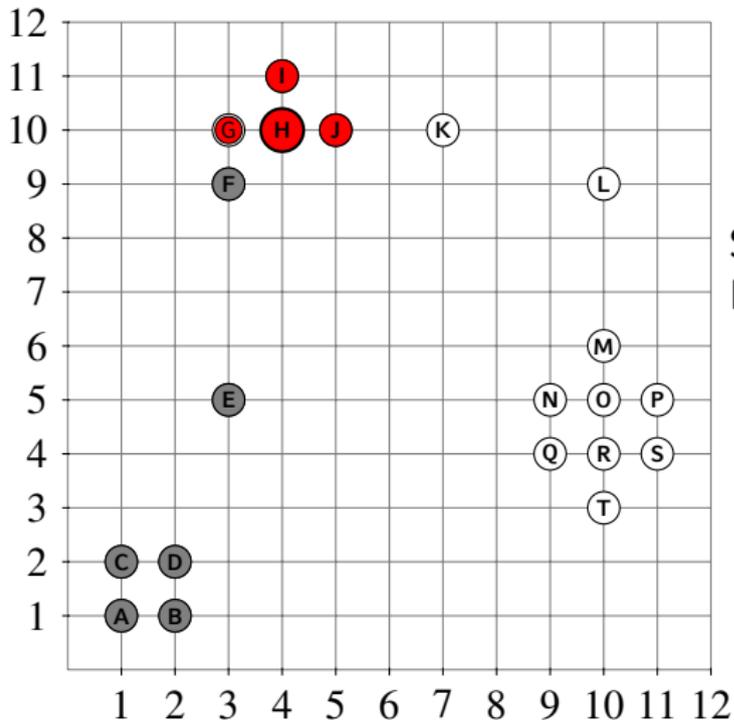
Seed list:



$$\epsilon = 1.1$$

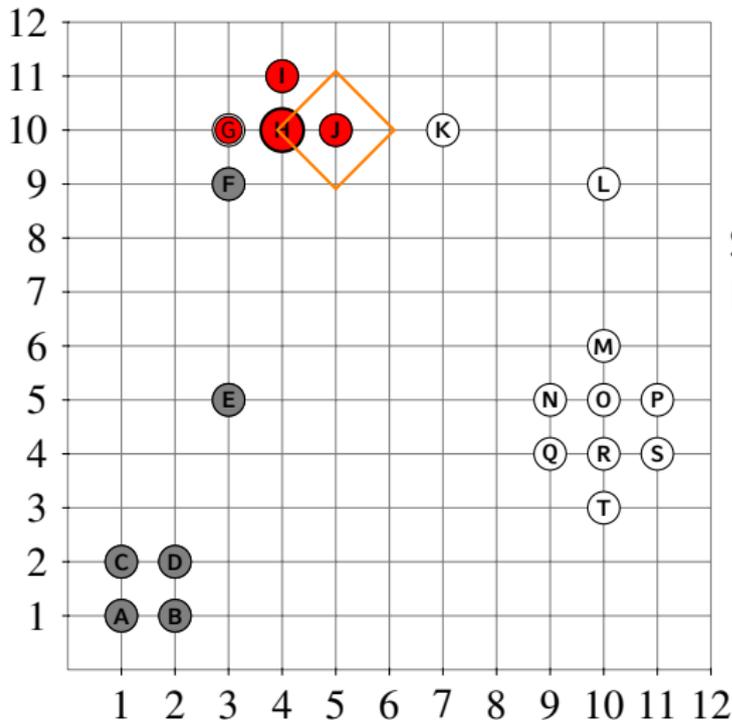
$$\text{minPts} = 4$$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 4$

Seed list:

IJ

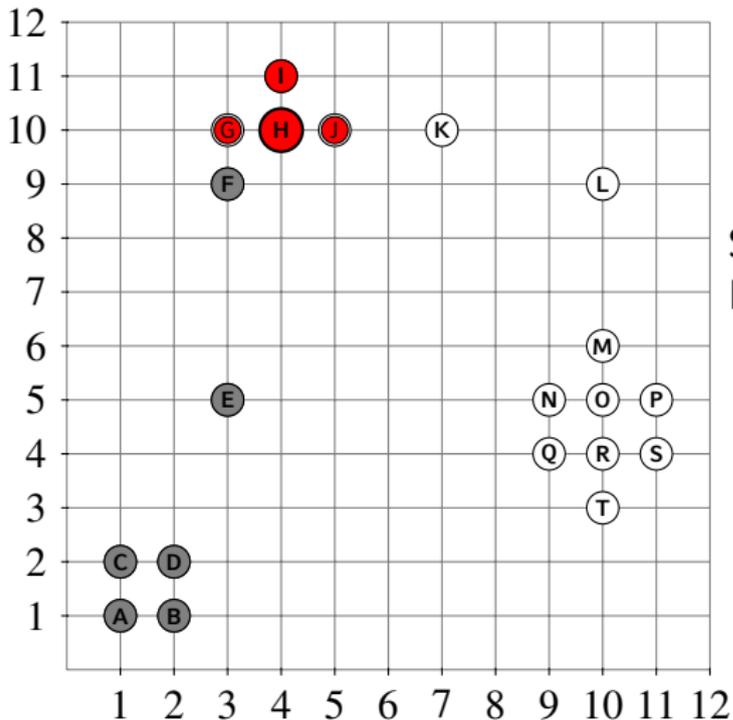


$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

Seed list:

I

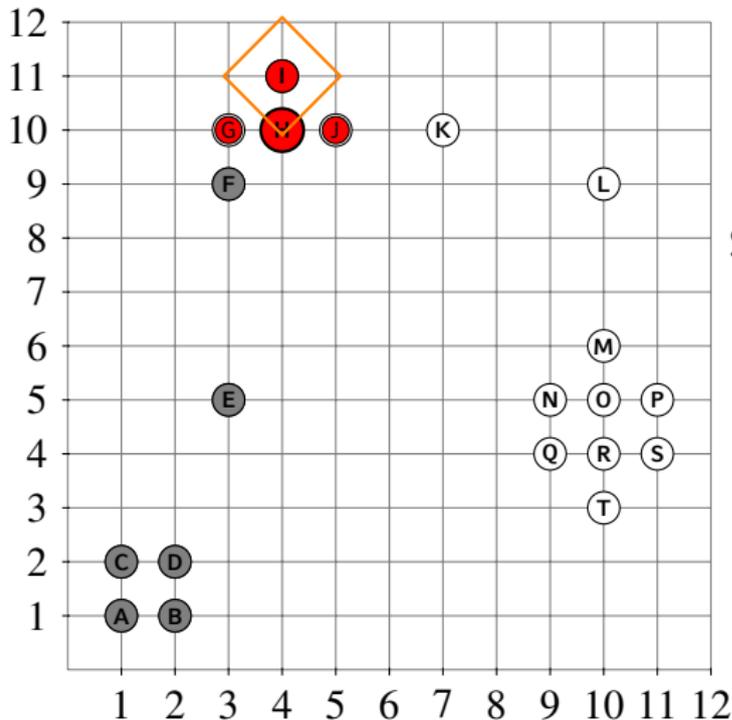


$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

Seed list:

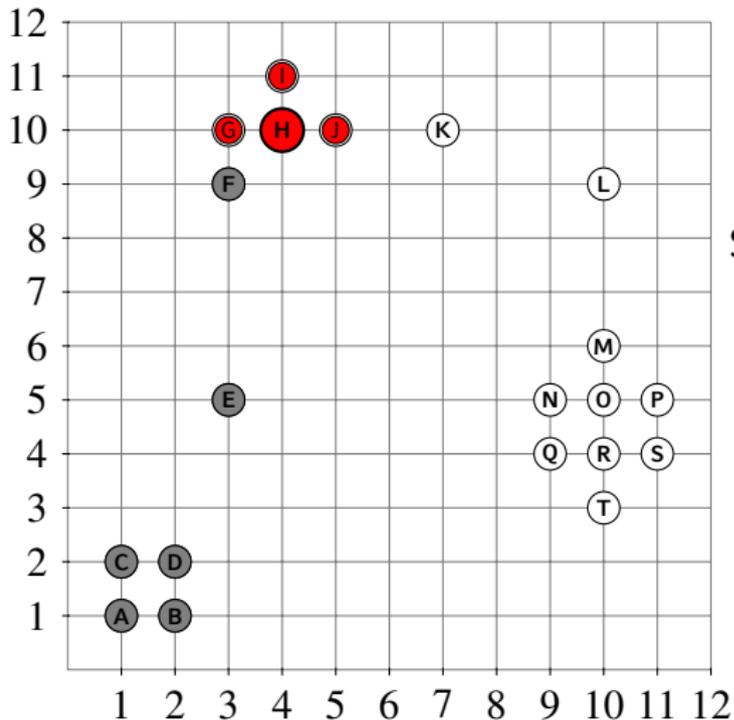
I



$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

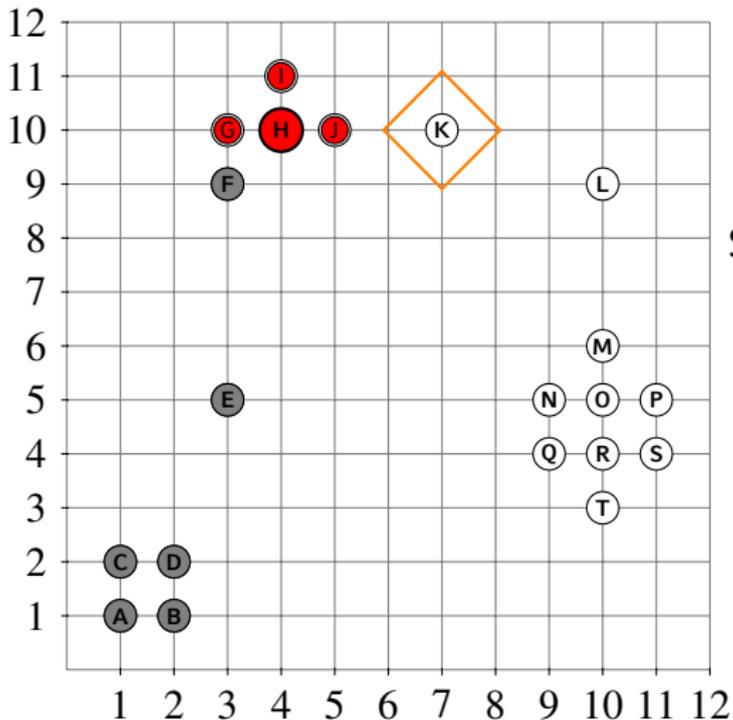
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$$\epsilon = 1.1$$

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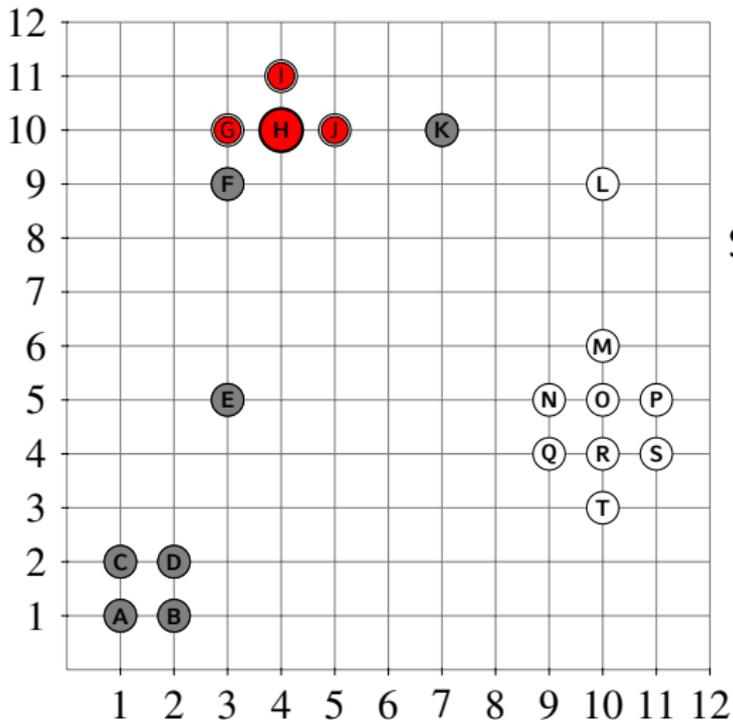
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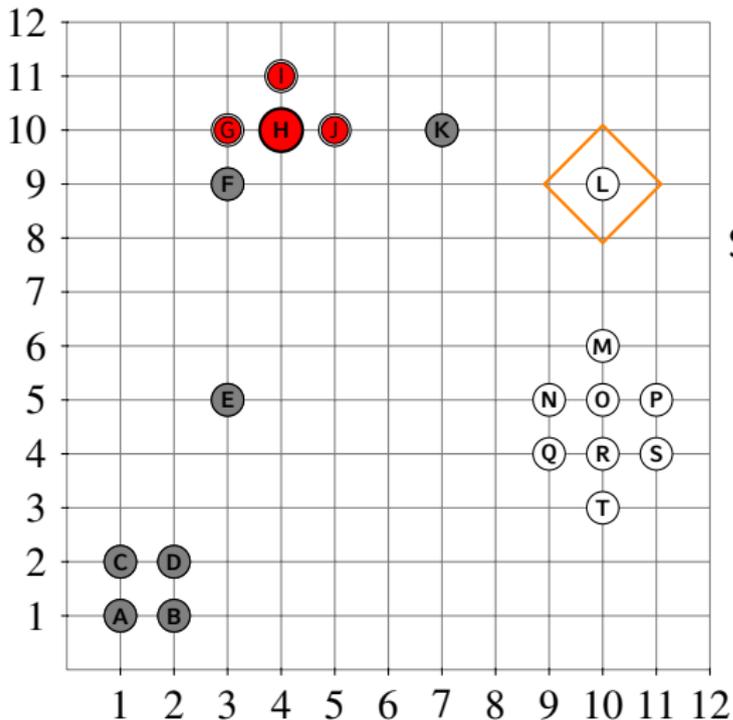
Seed list:



$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

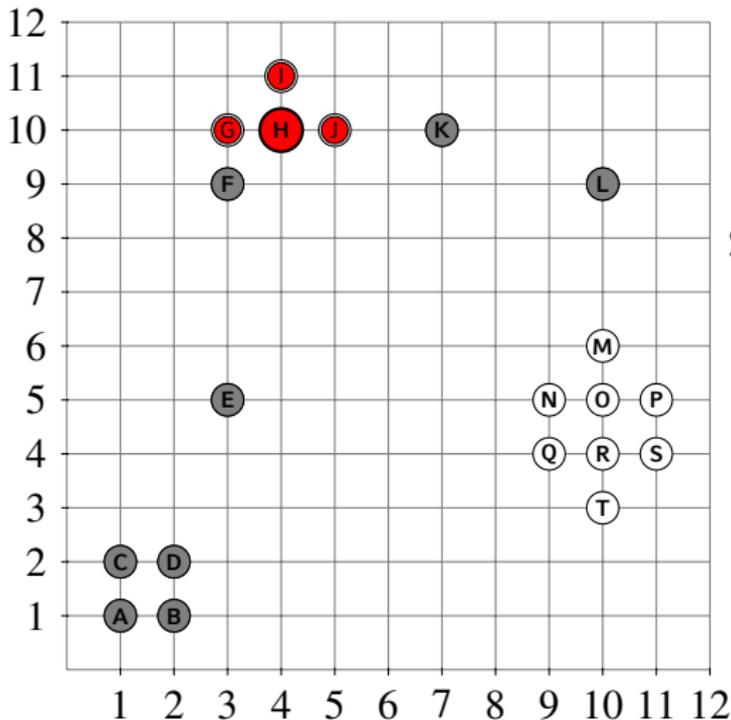
Seed list:



$$\epsilon = 1.1$$

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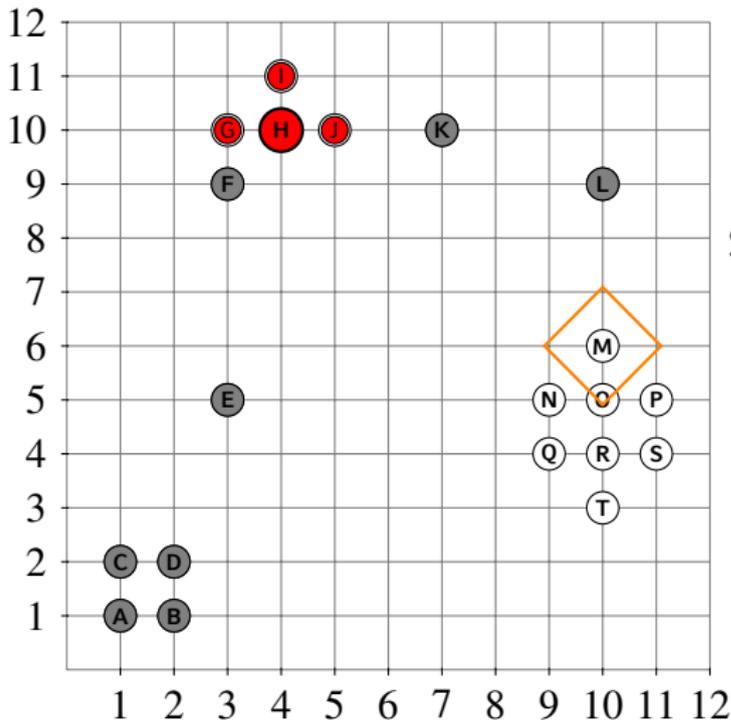
Seed list:



$\epsilon = 1.1$

$\text{minPts} = 4$

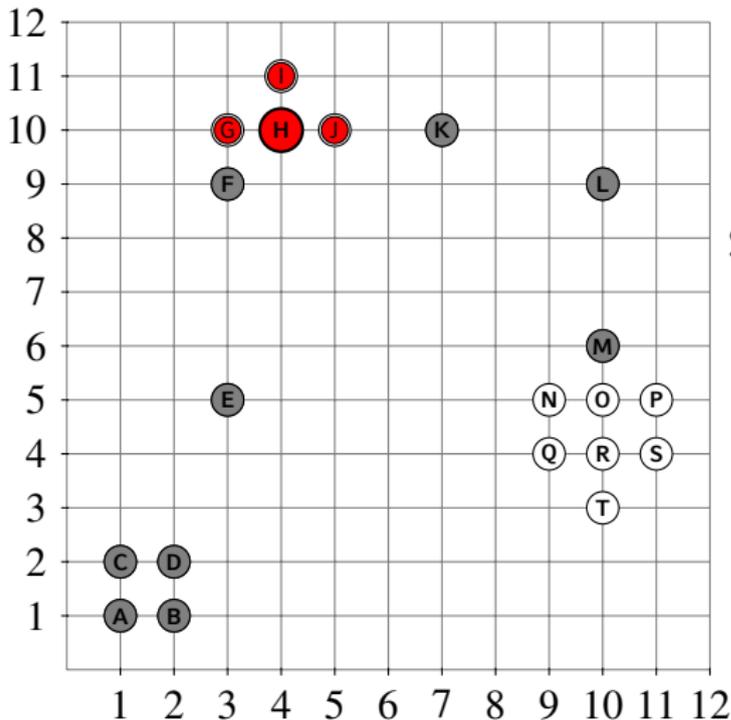
Seed list:



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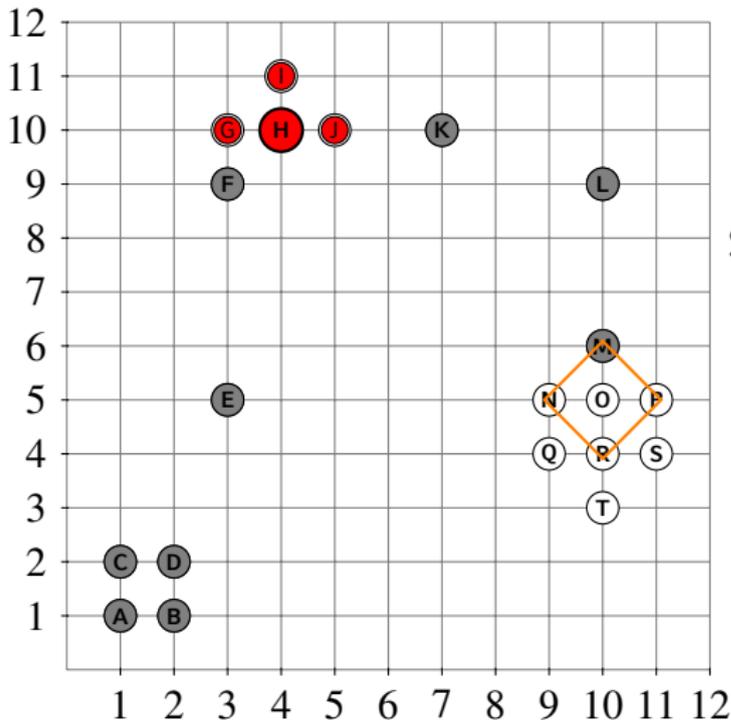
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$\epsilon = 1.1$

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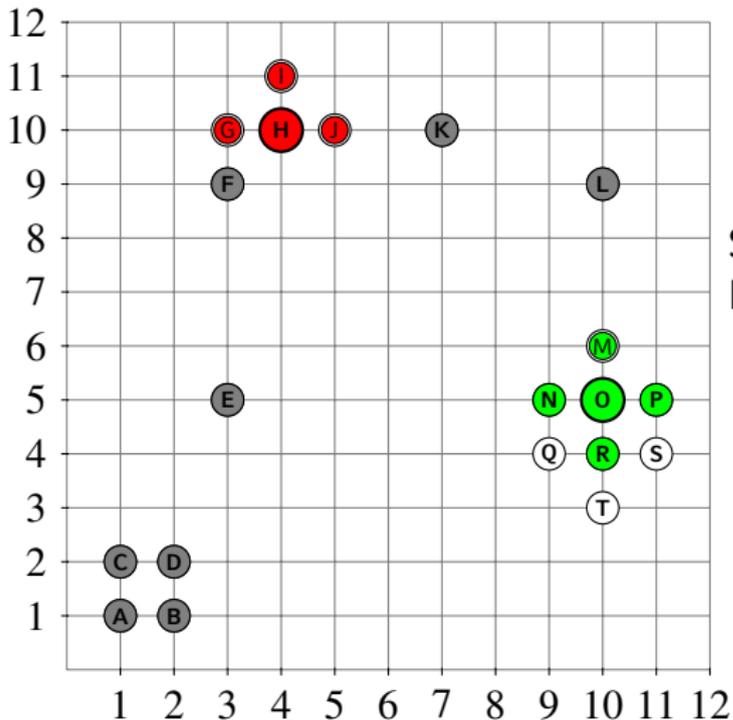
Seed list:



$\epsilon = 1.1$

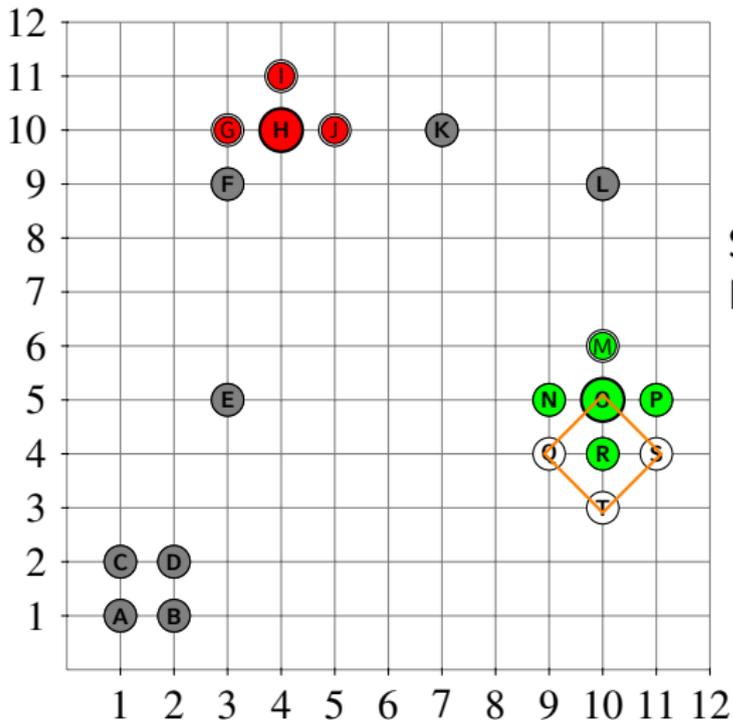
$minPts = 4$

Seed list:

 $\epsilon = 1.1$ $\text{minPts} = 4$

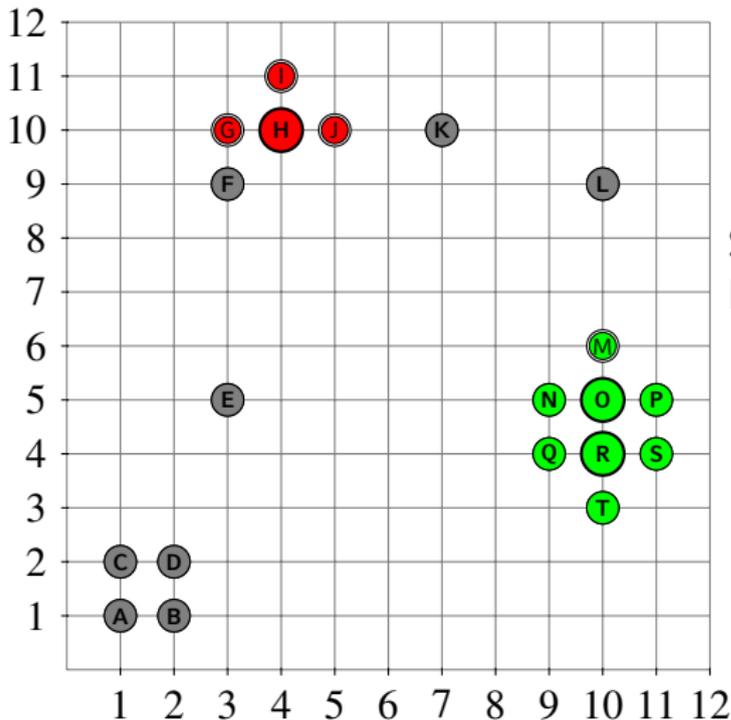
Seed list:

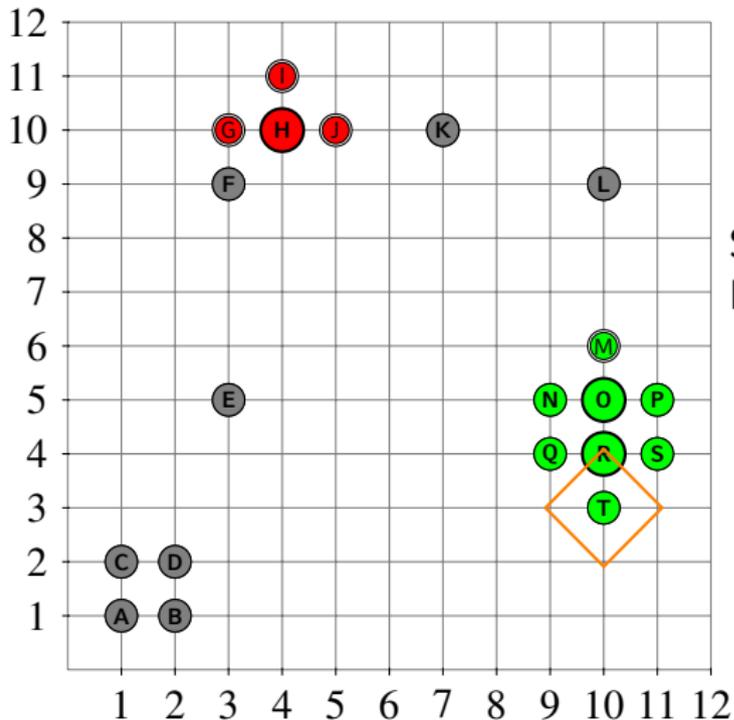
NPR

 $\epsilon = 1.1$ $\text{minPts} = 4$

Seed list:

NP

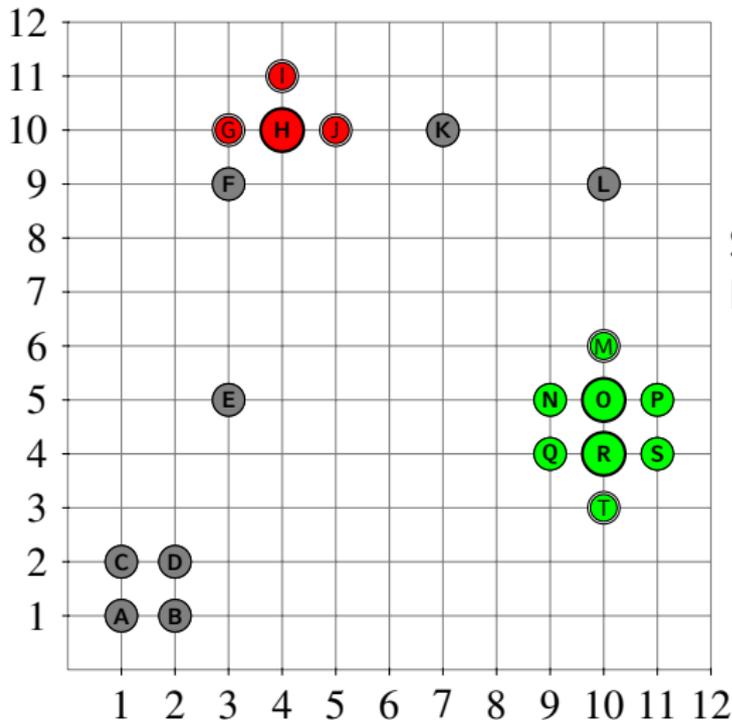
 $\epsilon = 1.1$ $\text{minPts} = 4$ Seed list:
NPQST

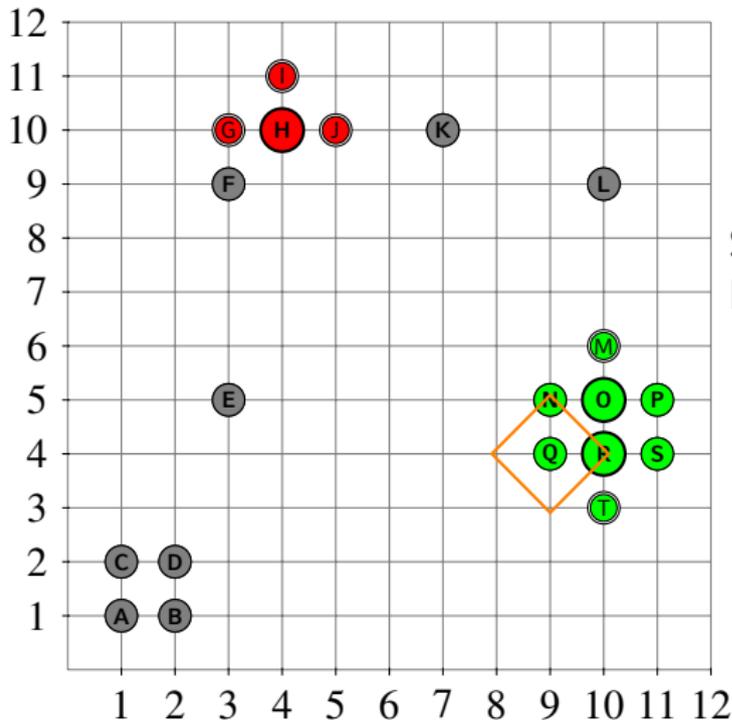


$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

Seed list:
NPQS

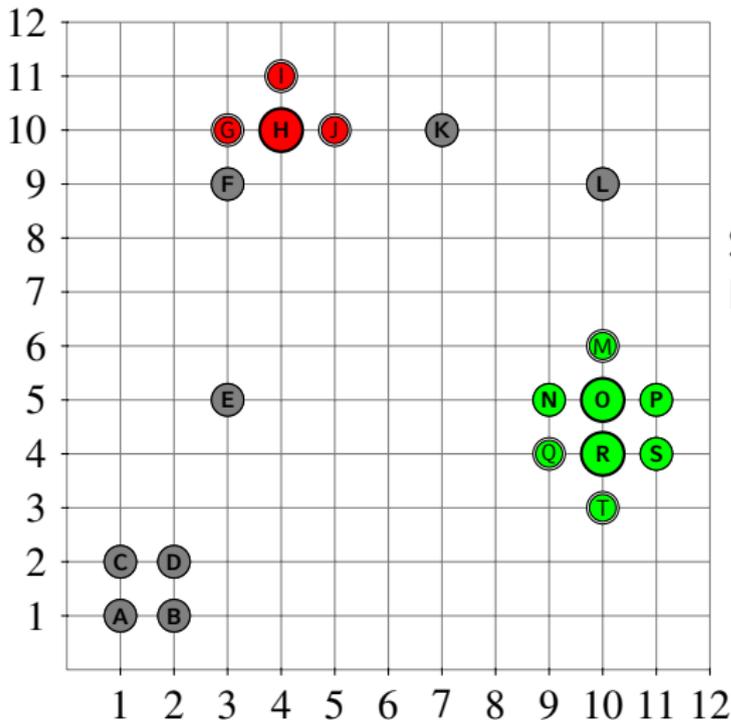
 $\epsilon = 1.1$ $\text{minPts} = 4$ Seed list:
NPQS



$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

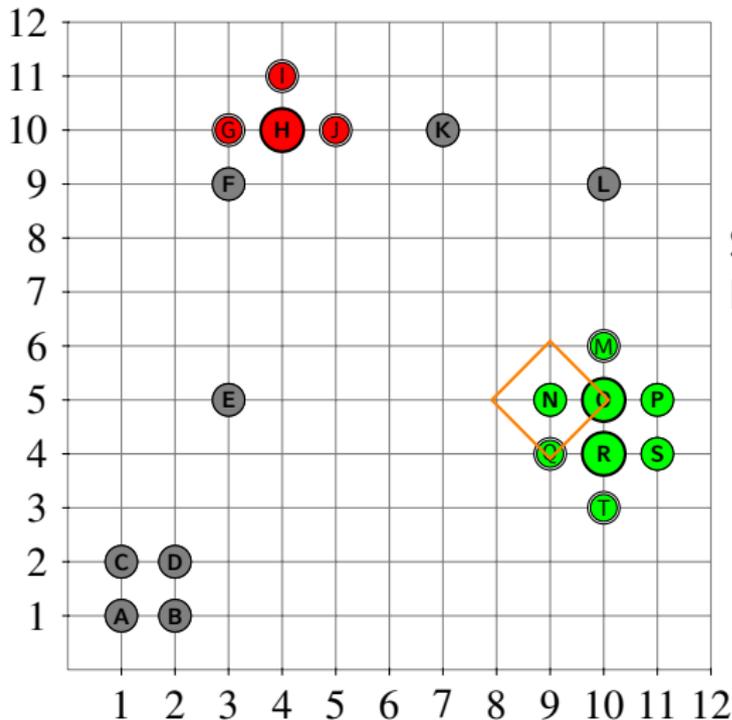
Seed list:
NPS



$\epsilon = 1.1$

$minPts = 4$

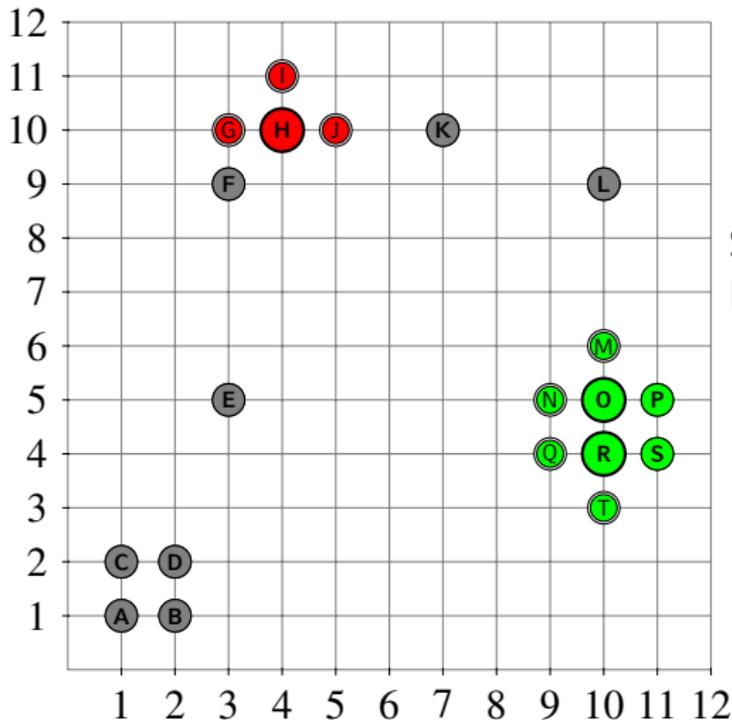
Seed list:
NPS

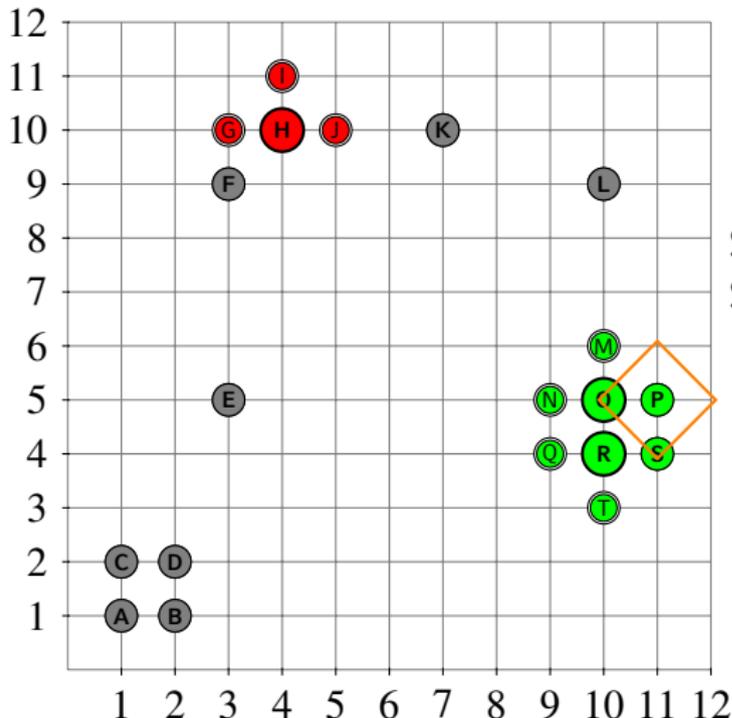


$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

Seed list:
PS

 $\epsilon = 1.1$ $\text{minPts} = 4$ Seed list:
PS

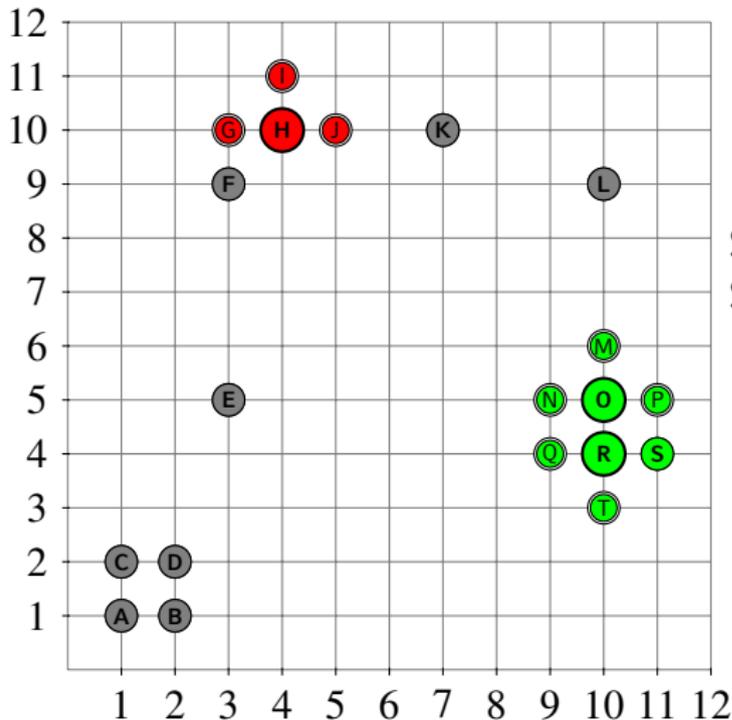


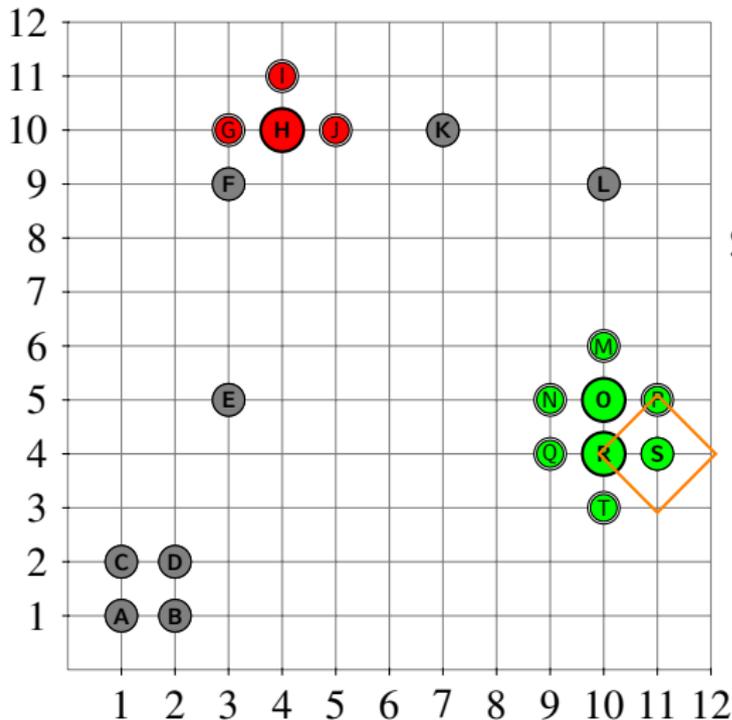
$\epsilon = 1.1$

$minPts = 4$

Seed list:

S

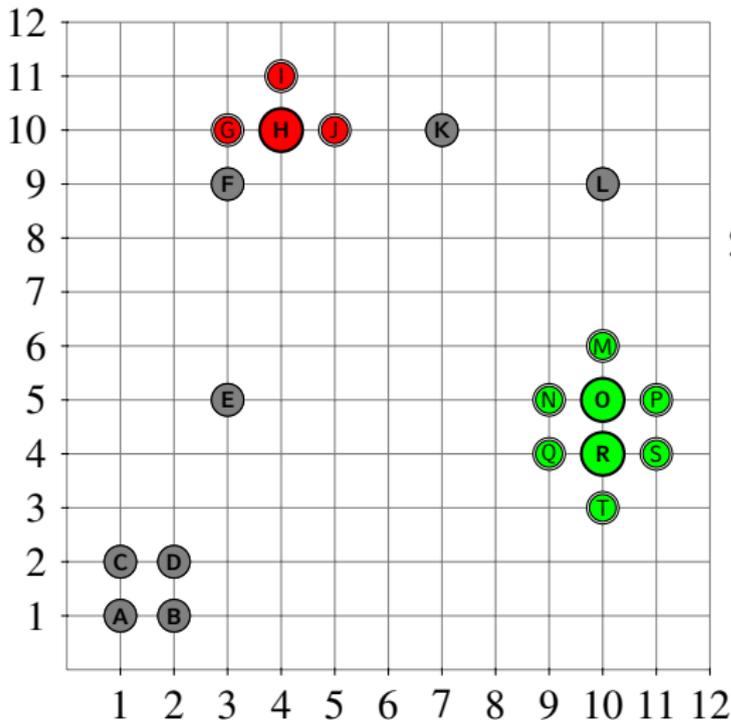
 $\epsilon = 1.1$ $\text{minPts} = 4$ Seed list:
S



$\epsilon = 1.1$

$minPts = 4$

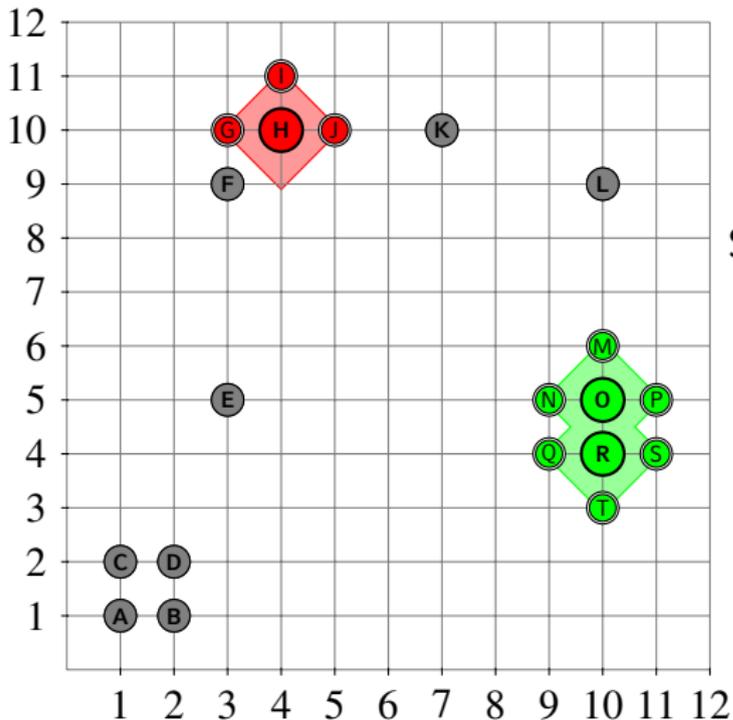
Seed list:



$\epsilon = 1.1$

$minPts = 4$

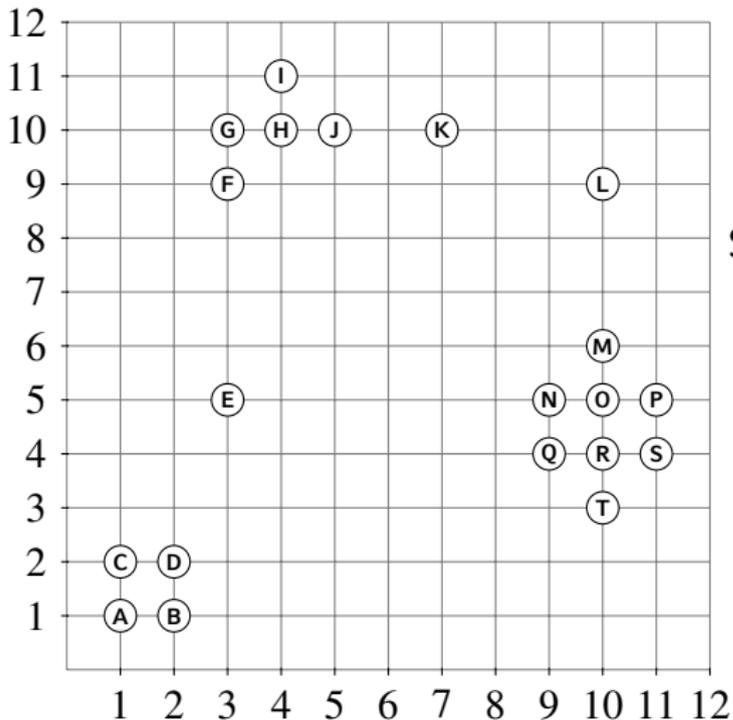
Seed list:



$$\epsilon = 1.1$$

$$\text{minPts} = 4$$

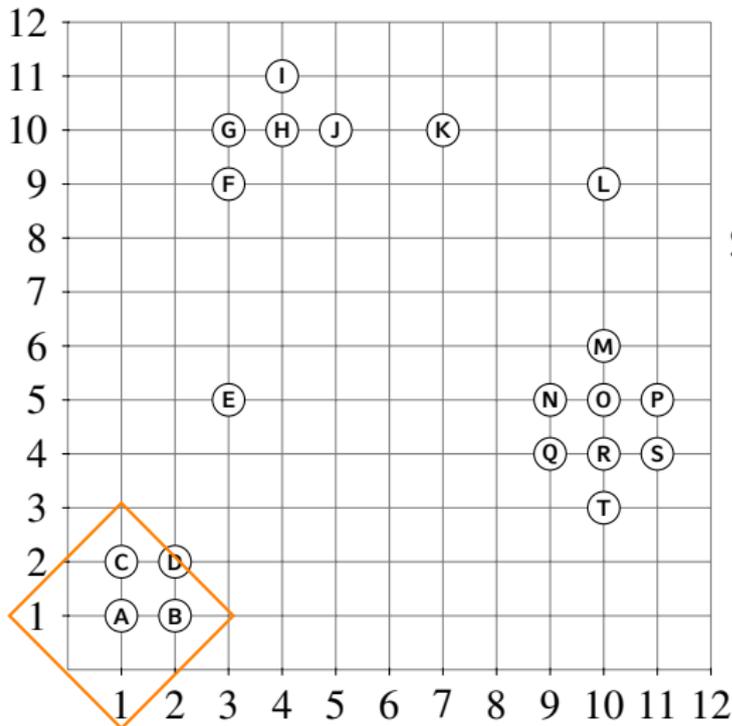
Seed list:



$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

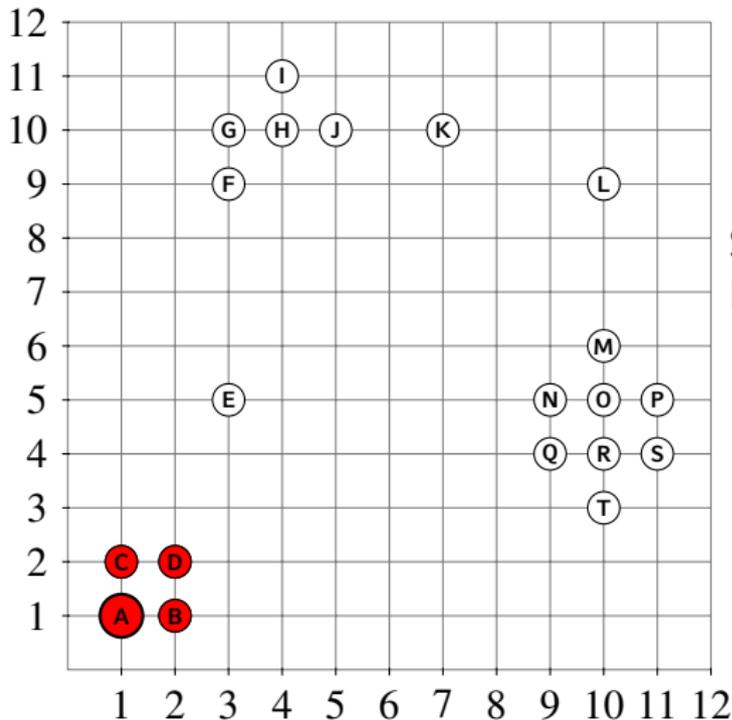
Seed list:



$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

Seed list:

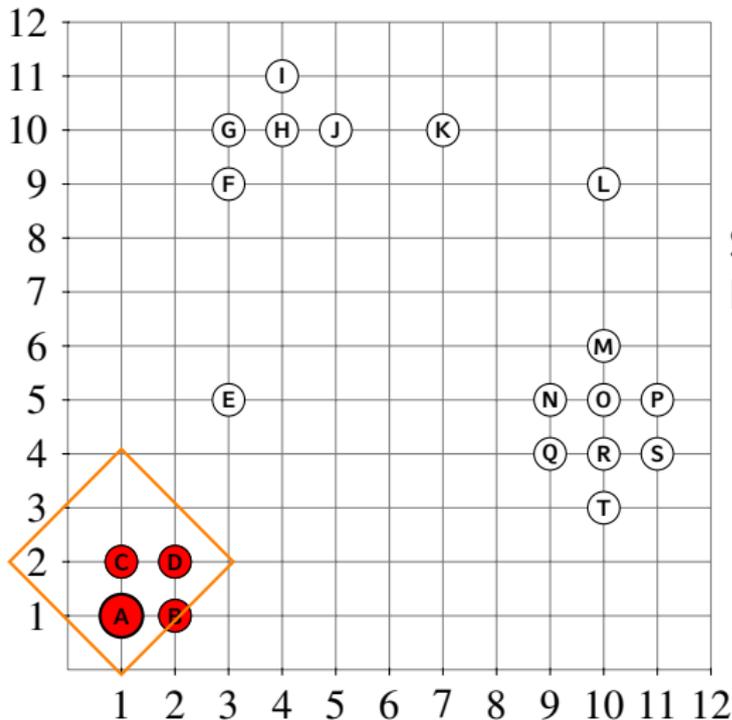


$\epsilon = 2.1$

$minPts = 4$

Seed list:

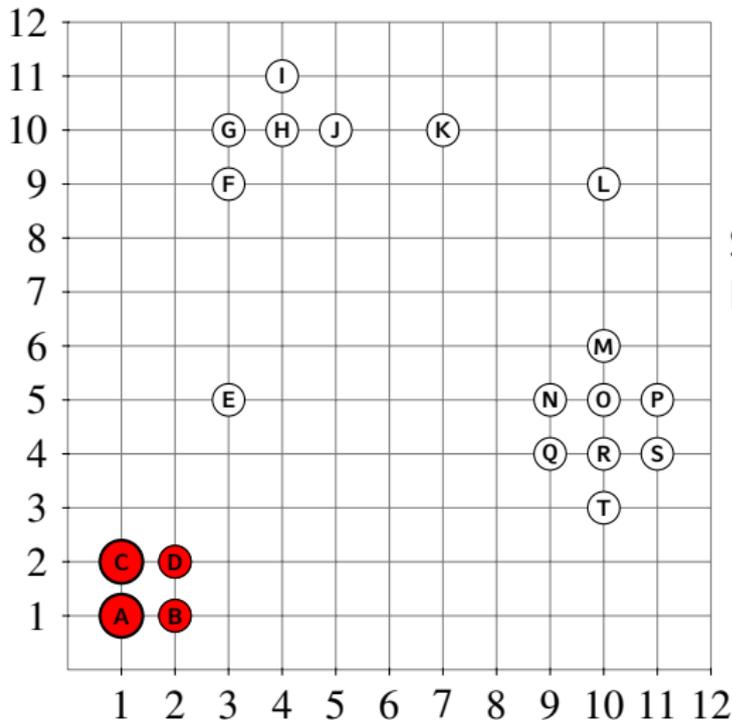
BCD



$$\epsilon = 2.1$$

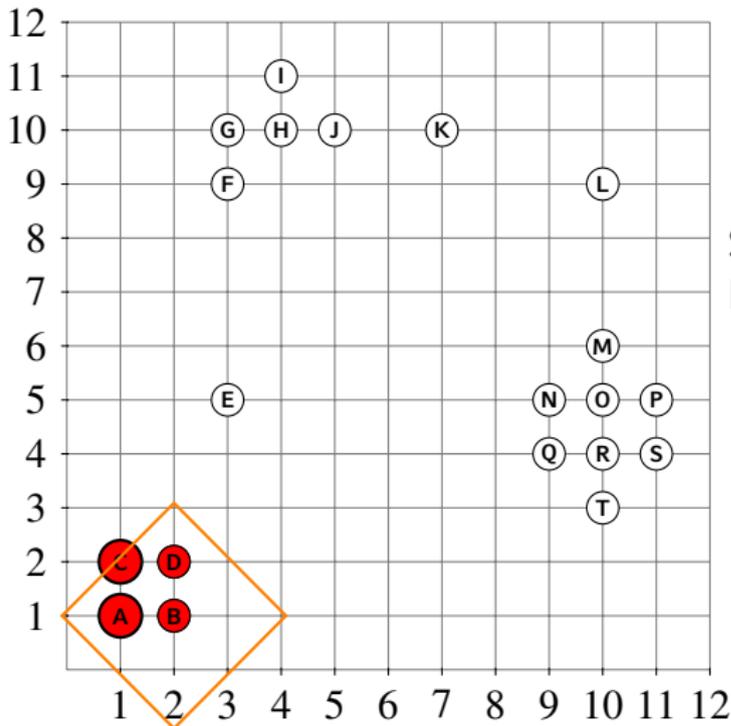
$$\text{minPts} = 4$$

Seed list:
BD

 $\epsilon = 2.1$ $\text{minPts} = 4$

Seed list:

BD

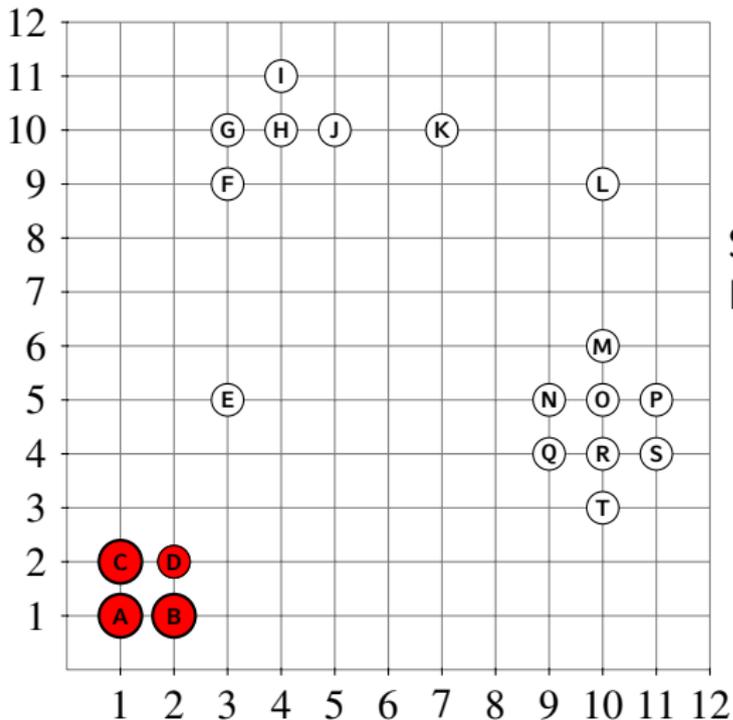


$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

Seed list:

D

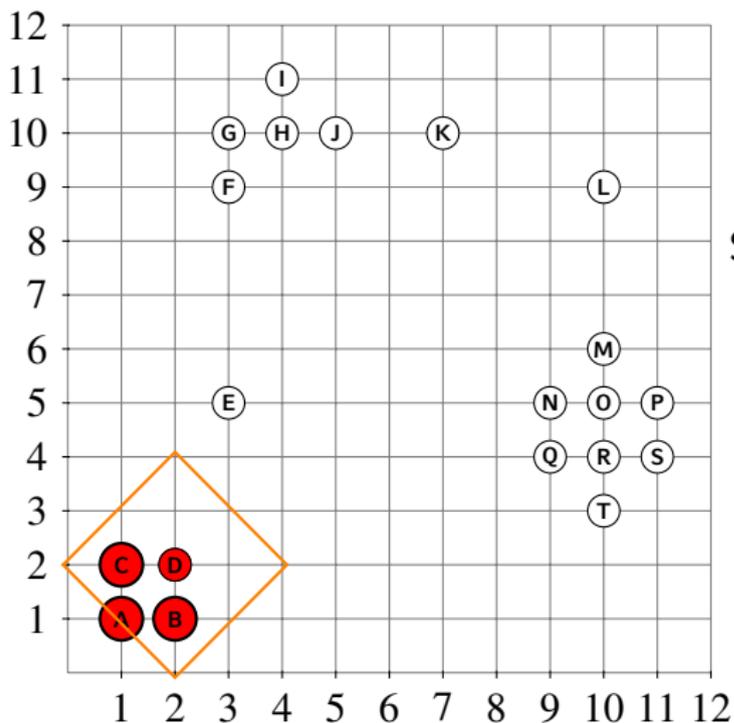


$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

Seed list:

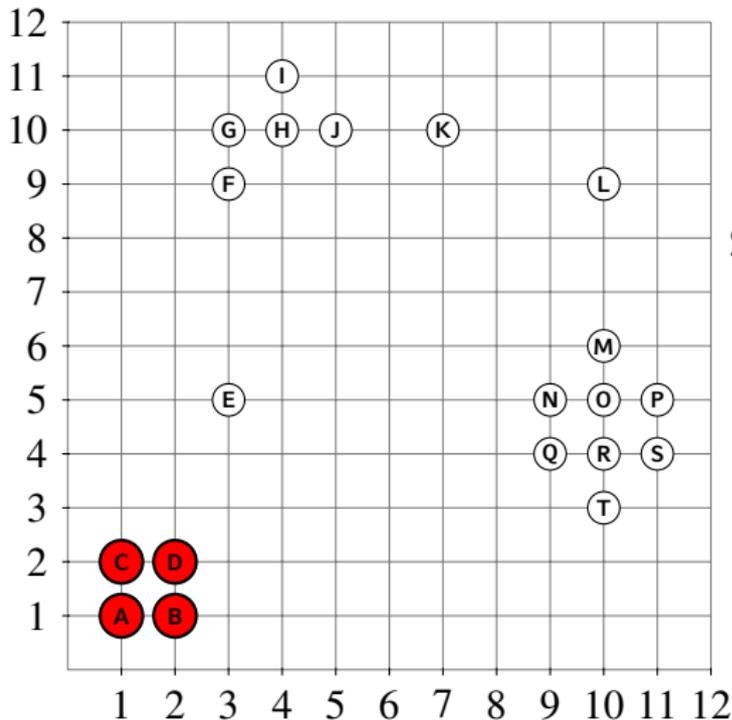
D



$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

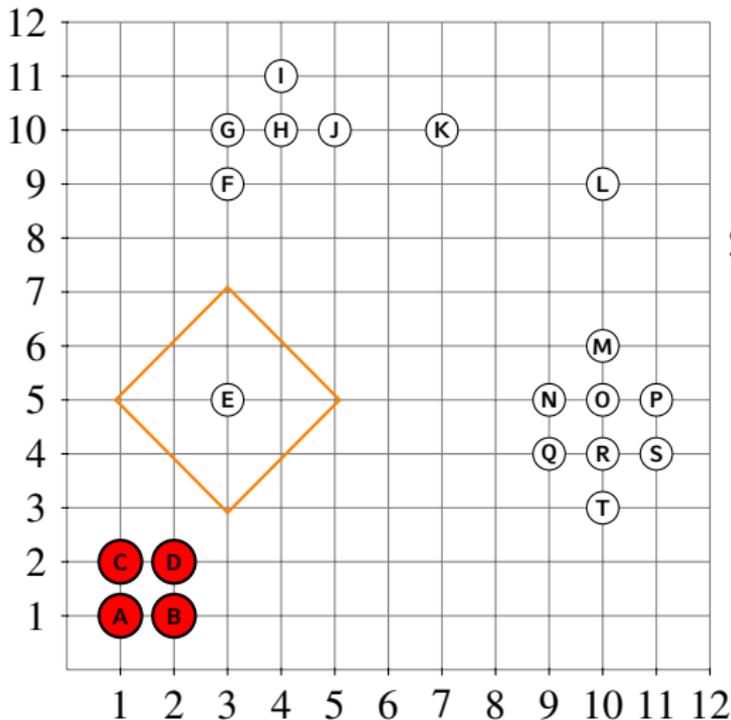
Seed list:



$\epsilon = 2.1$

$minPts = 4$

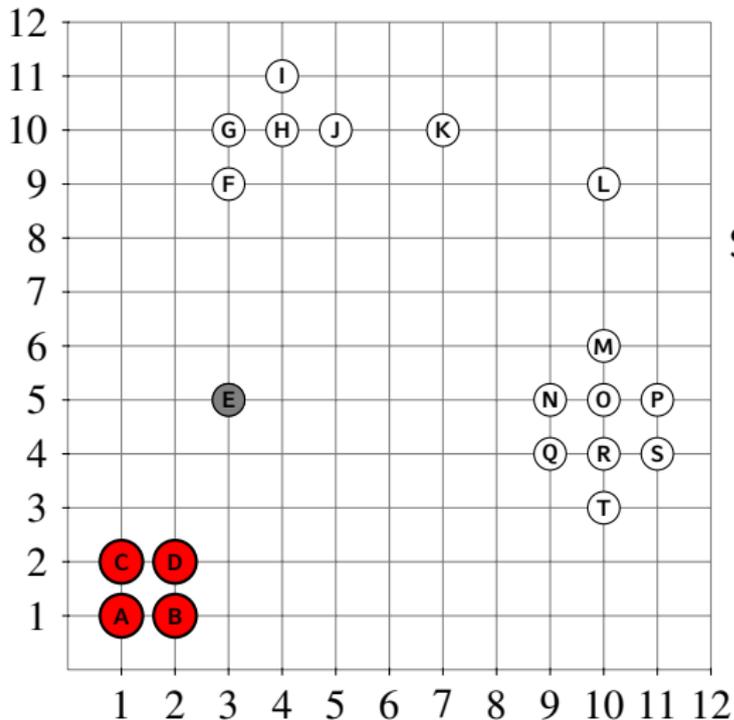
Seed list:

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 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$ 

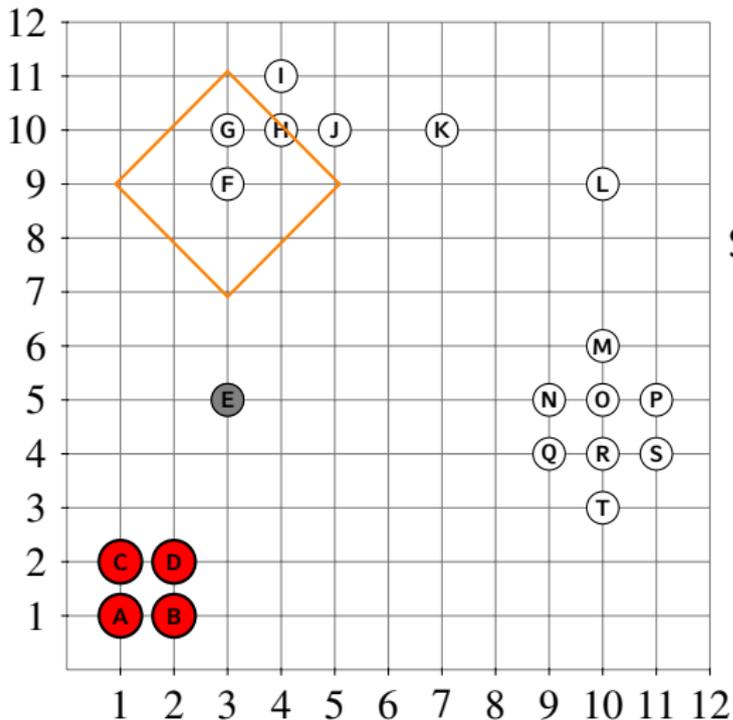
$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

Seed list:

 $\epsilon = 2.1$ $\text{minPts} = 4$

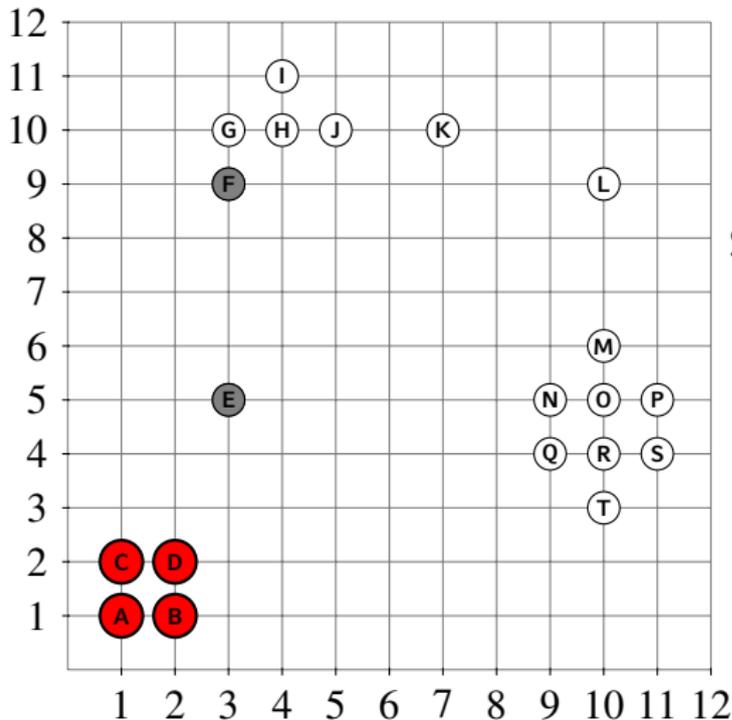
Seed list:



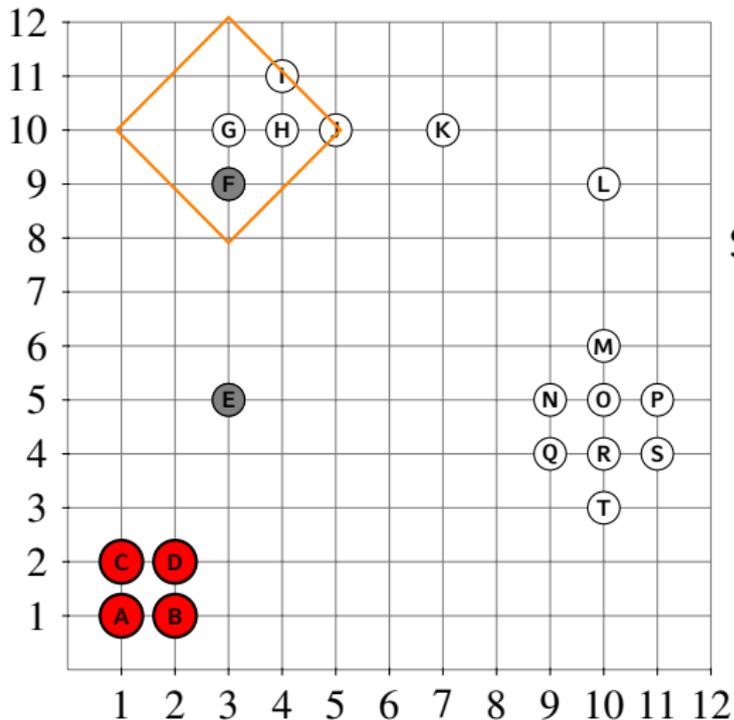
$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

Seed list:

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 2.1$ $\text{minPts} = 4$

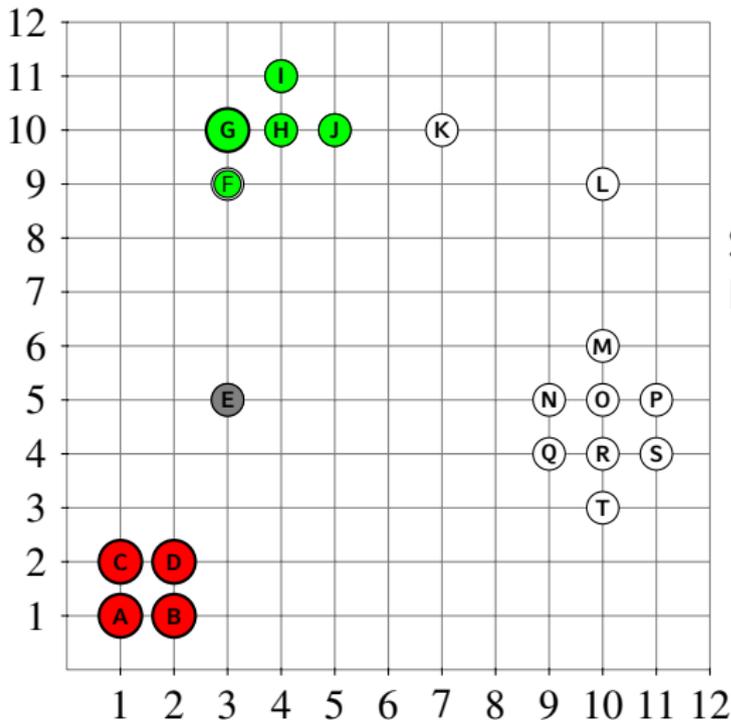
Seed list:



$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

Seed list:

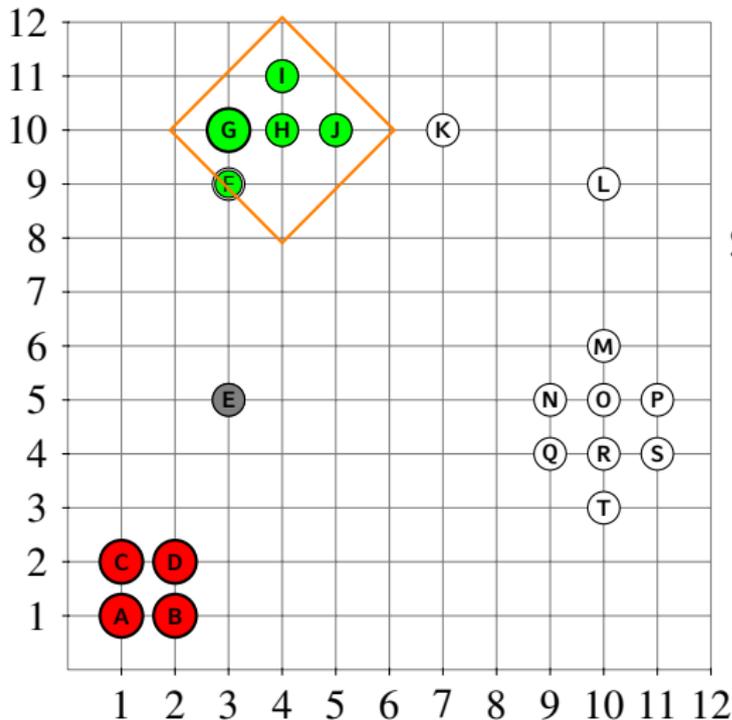


$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

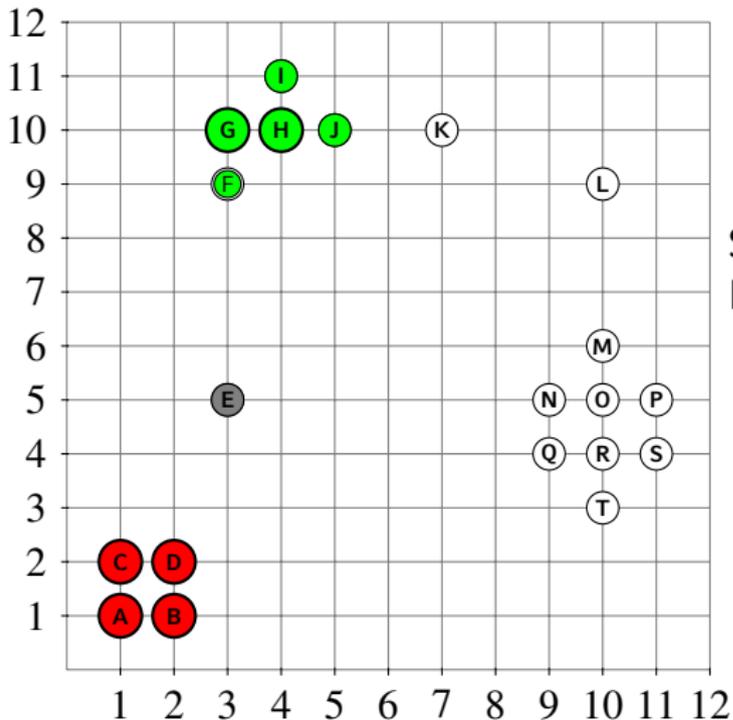
Seed list:

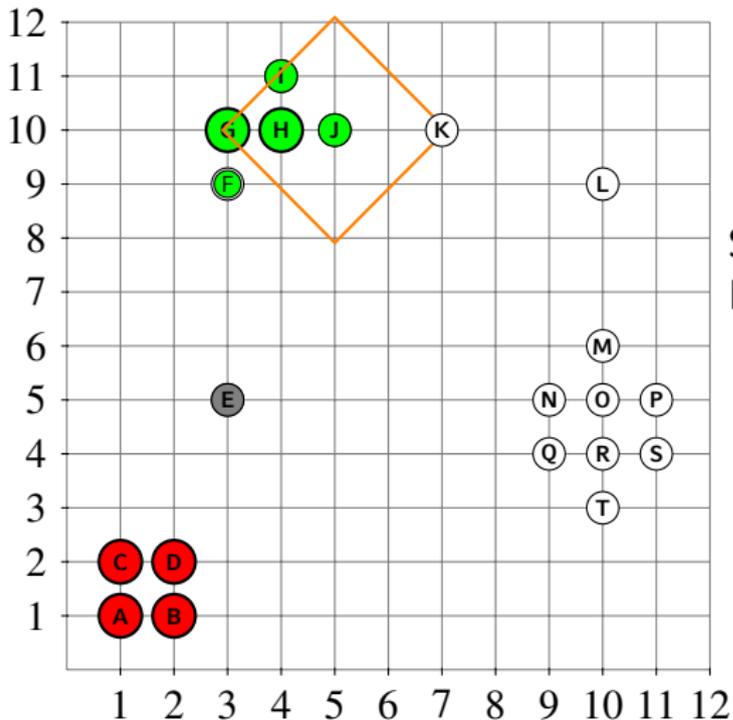
HIJ

 $\epsilon = 2.1$ $\text{minPts} = 4$

Seed list:

IJ



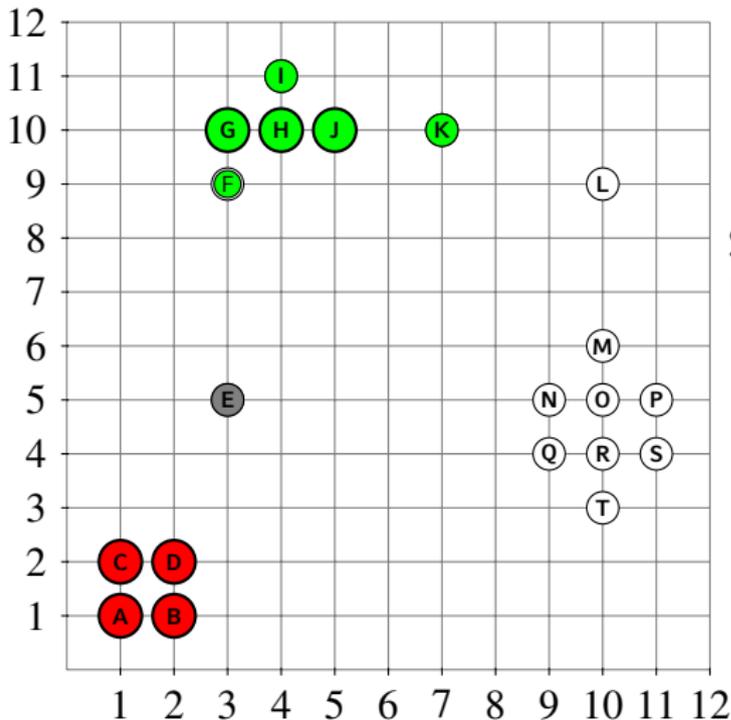


$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

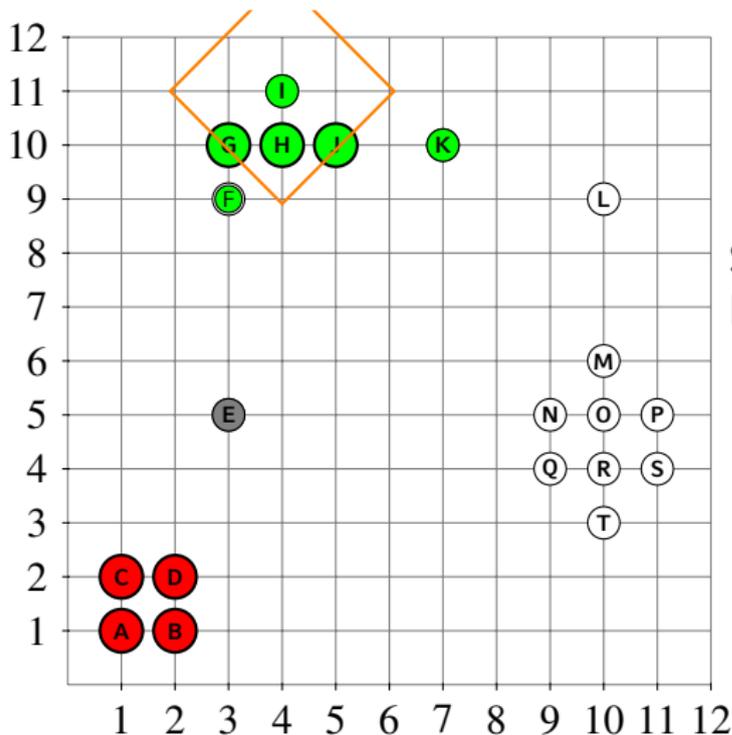
Seed list:

I

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 2.1$ $\text{minPts} = 4$

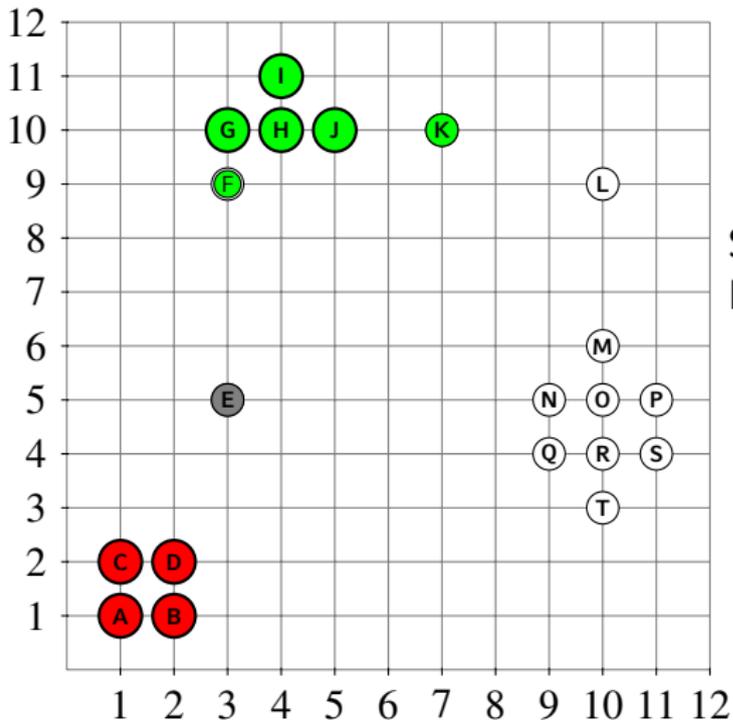
Seed list:

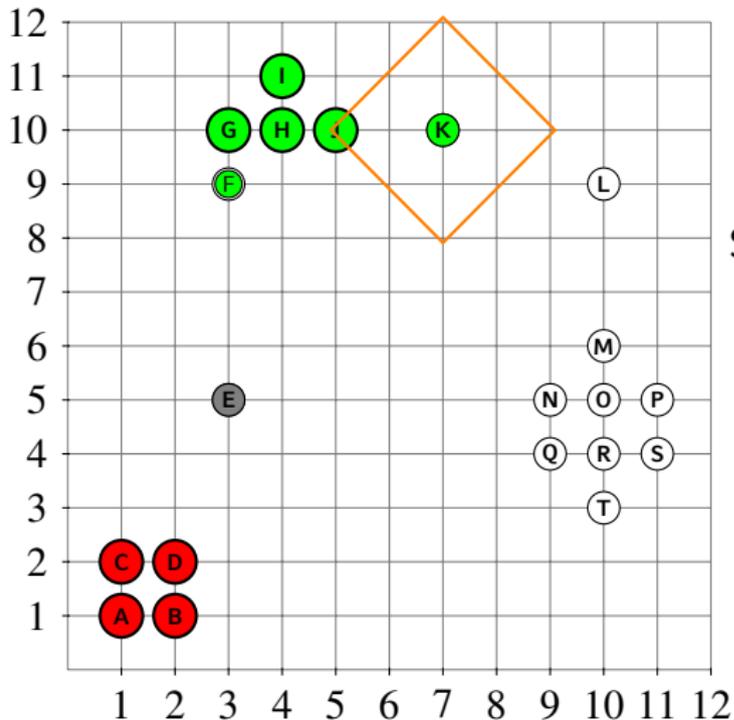
IK

 $\epsilon = 2.1$ $\text{minPts} = 4$

Seed list:

K

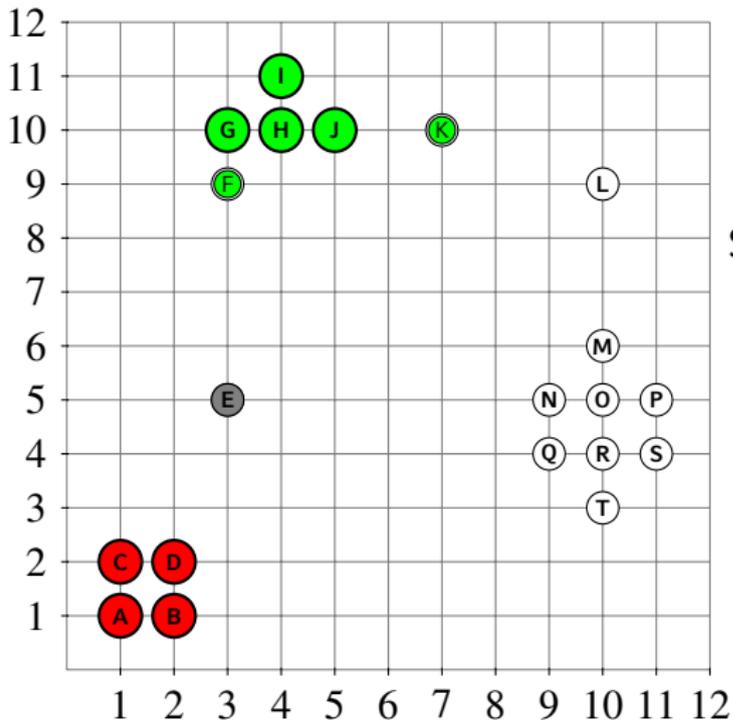
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 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 2.1$ $\text{minPts} = 4$ Seed list:
K

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$ 

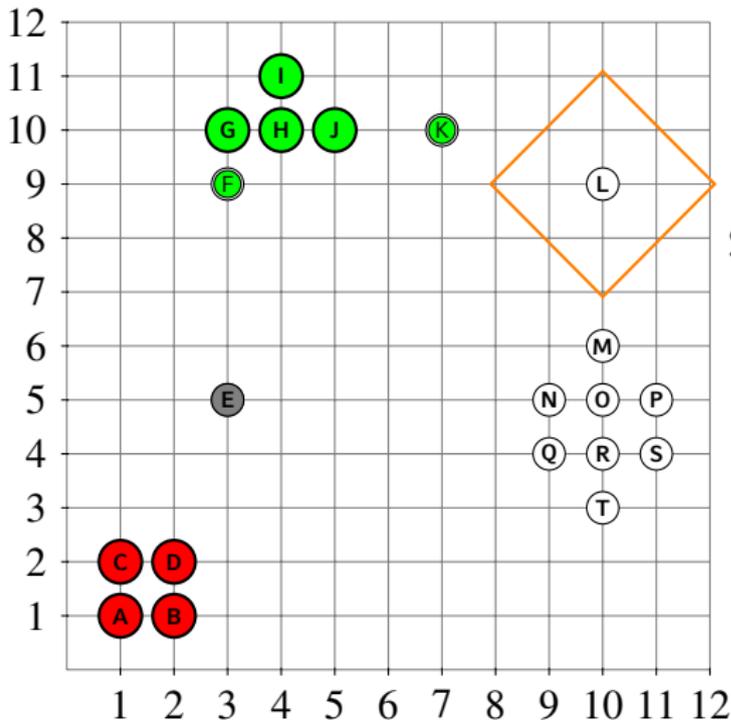
$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

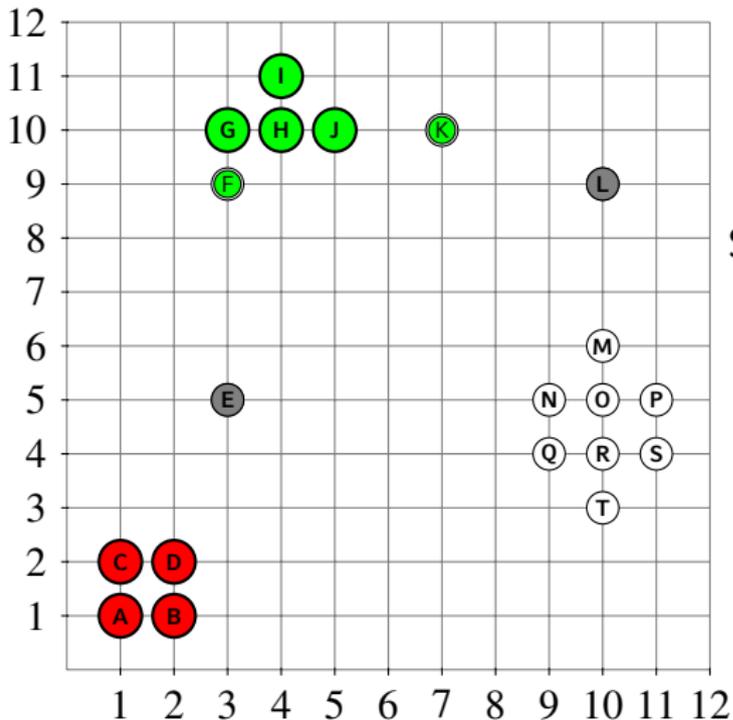
Seed list:

$\epsilon = 1.1$
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 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 2.1$ $\text{minPts} = 4$

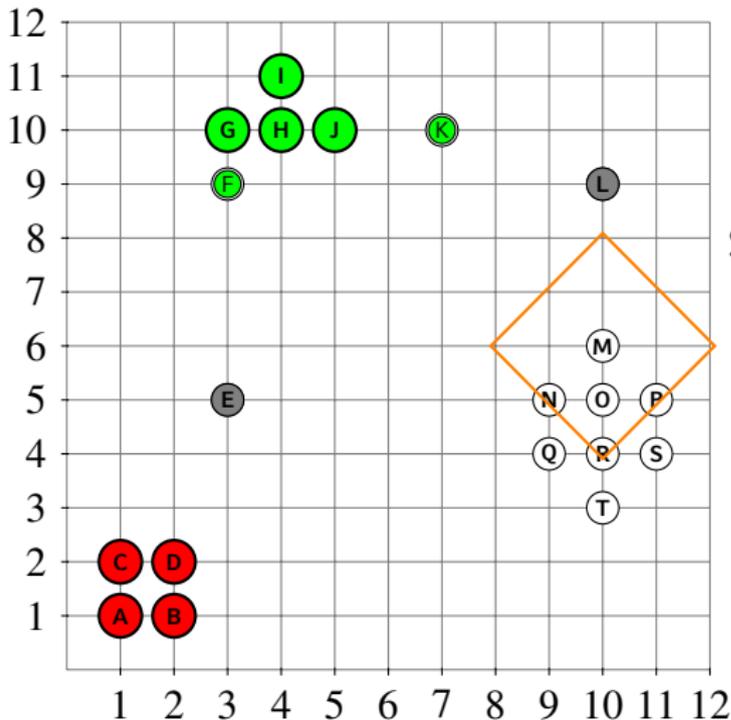
Seed list:

 $\epsilon = 2.1$ $\text{minPts} = 4$

Seed list:

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 2.1$ $\text{minPts} = 4$

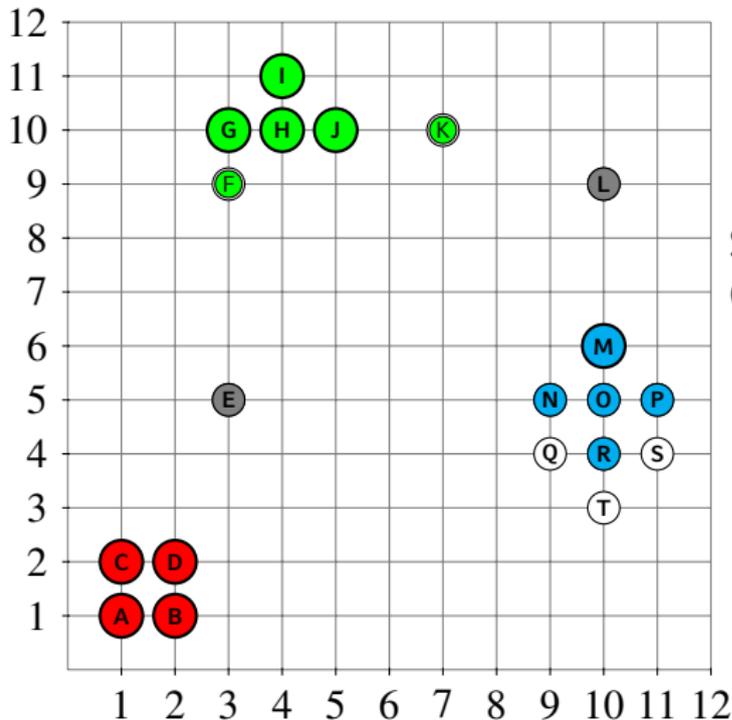
Seed list:

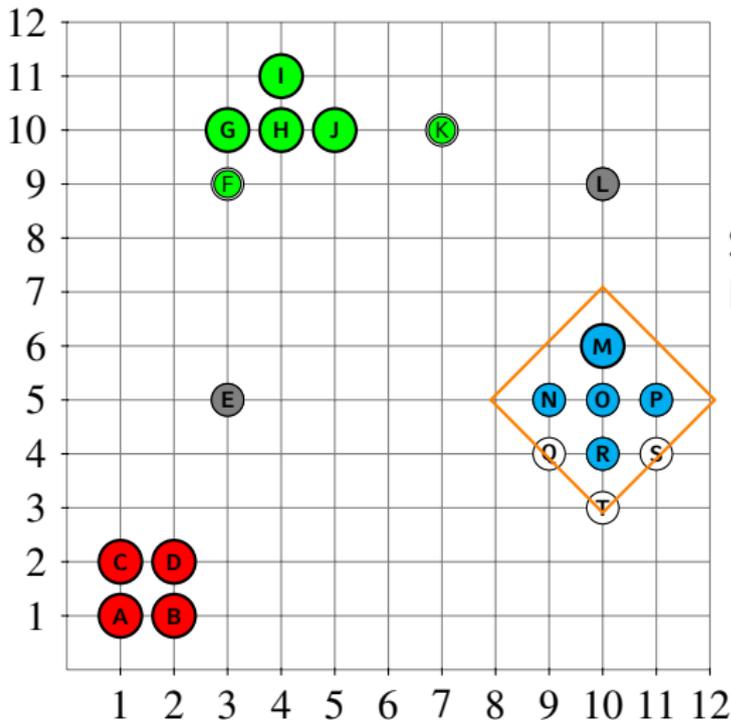


$\epsilon = 2.1$

$minPts = 4$

Seed list:

 $\epsilon = 2.1$ $\text{minPts} = 4$ Seed list:
ONPR

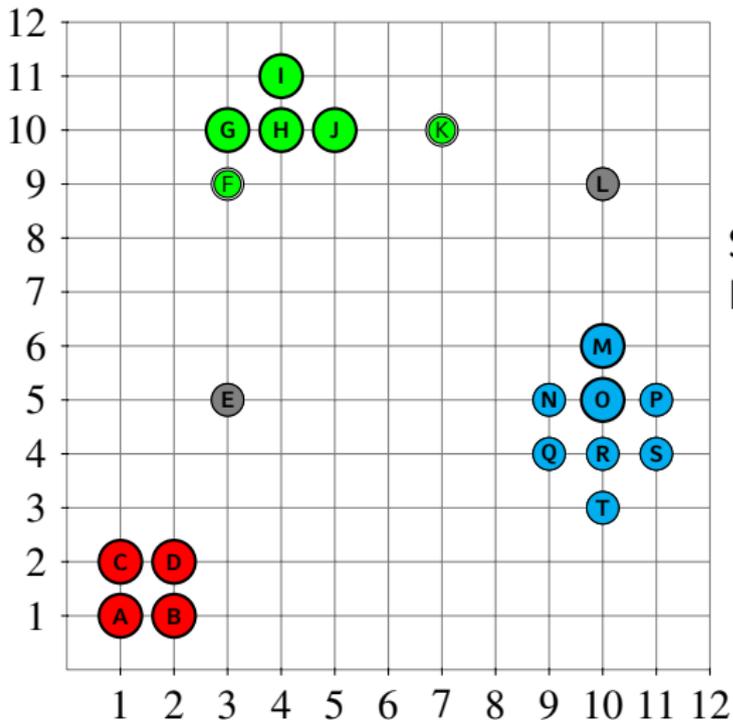


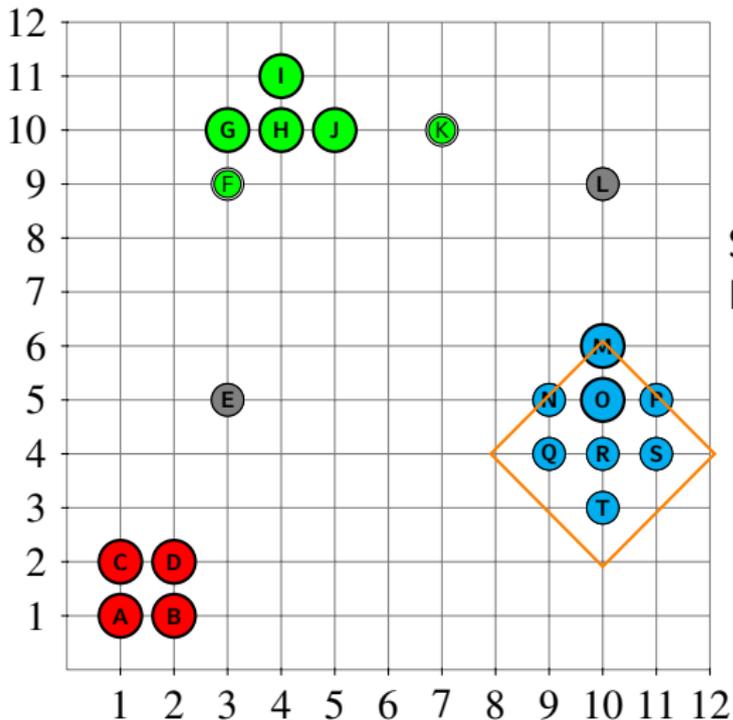
$\epsilon = 2.1$

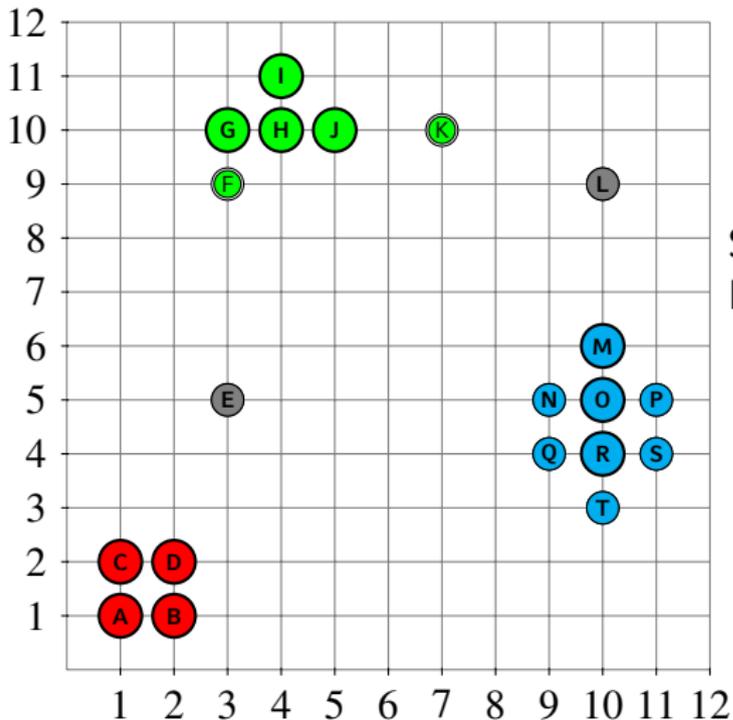
$minPts = 4$

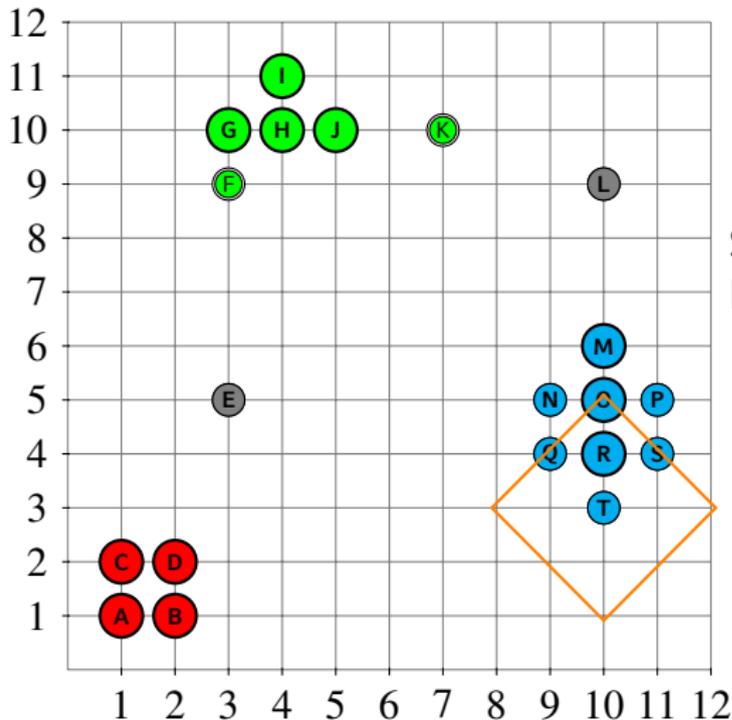
Seed list:

NPR

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 2.1$ $\text{minPts} = 4$ Seed list:
NPRQST

 $\epsilon = 2.1$ $\text{minPts} = 4$ Seed list:
NPQST

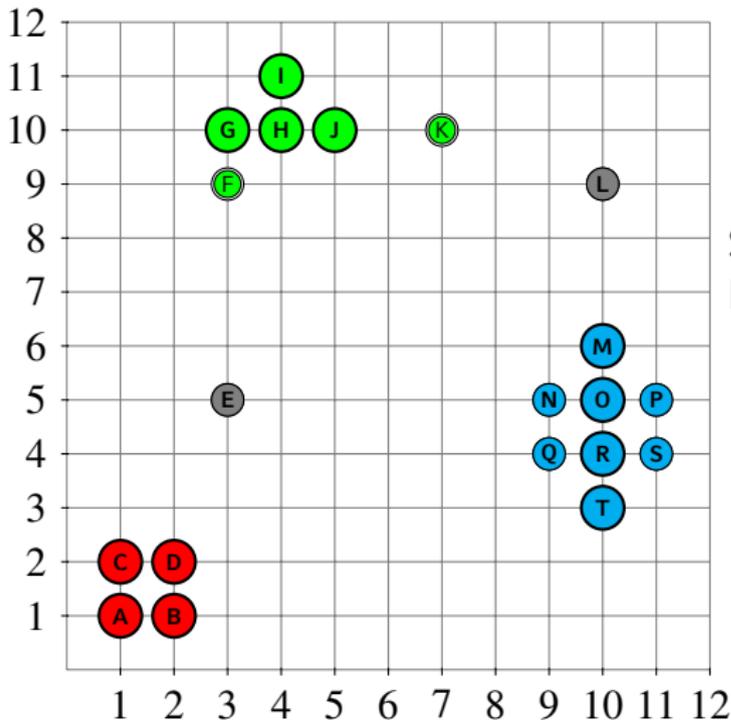
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NPQST

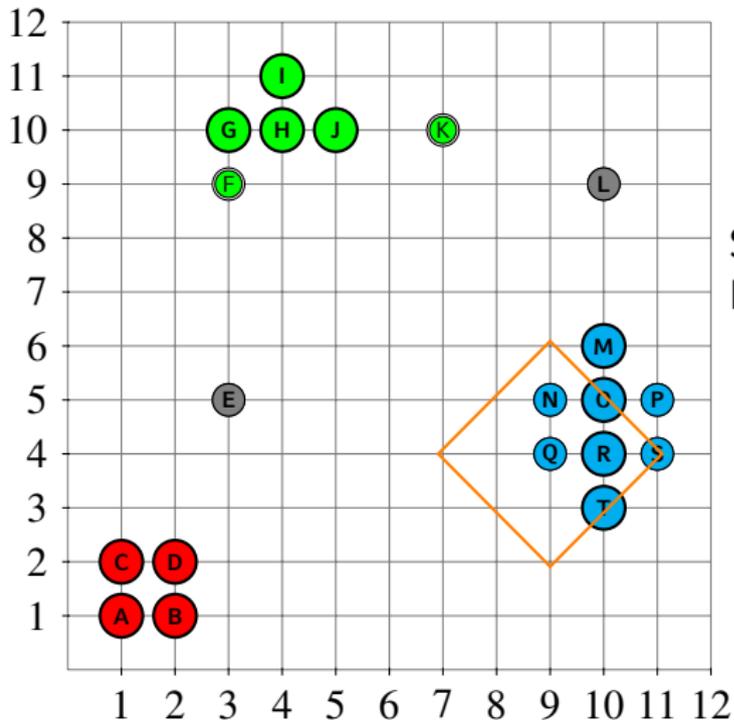


$\epsilon = 2.1$

$minPts = 4$

Seed list:
NPQS

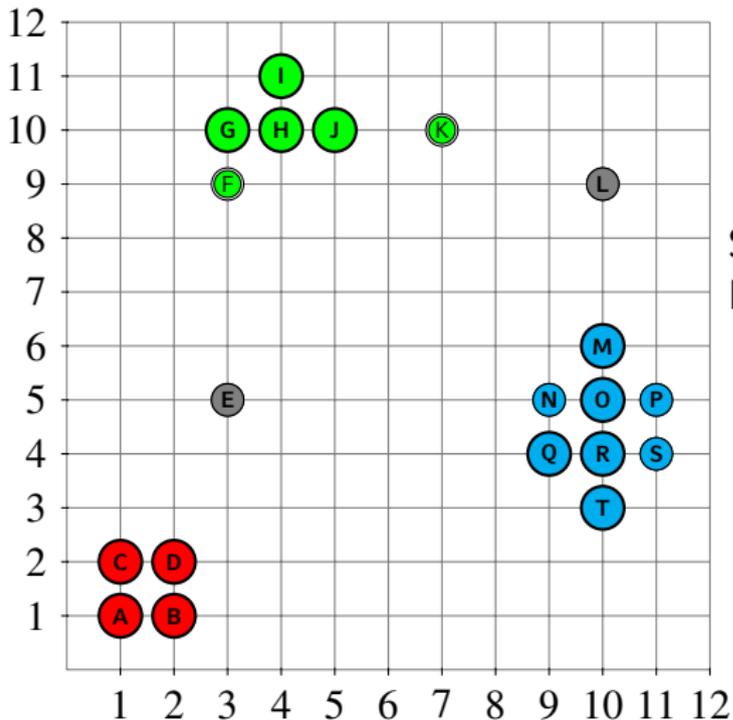
$\epsilon = 1.1$
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 $\text{minPts} = 4$ $\epsilon = 2.1$
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 $\text{minPts} = 4$  $\epsilon = 2.1$ $\text{minPts} = 4$ Seed list:
NPQS

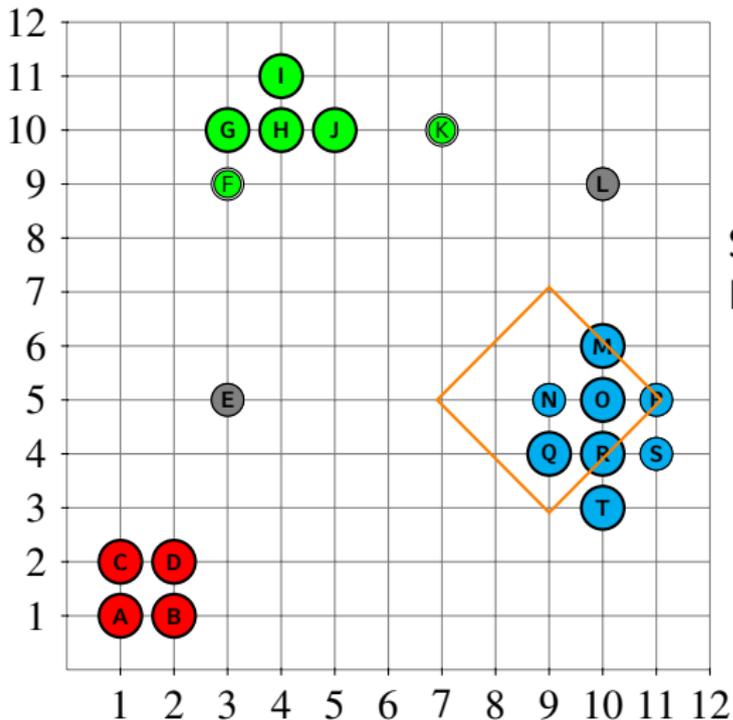


$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

Seed list:
NPS

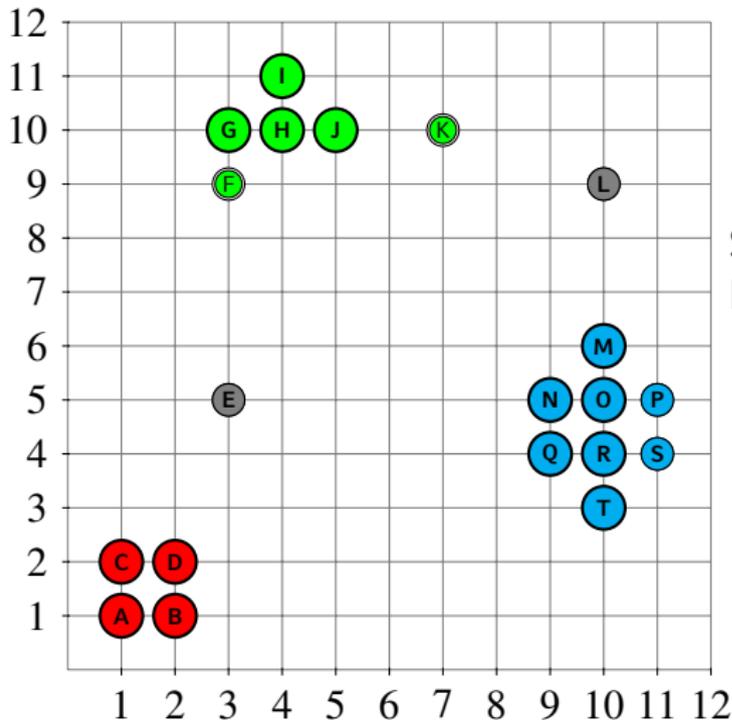
$\epsilon = 1.1$
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 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 2.1$ $\text{minPts} = 4$ Seed list:
NPS



$$\epsilon = 2.1$$

$$\text{minPts} = 4$$

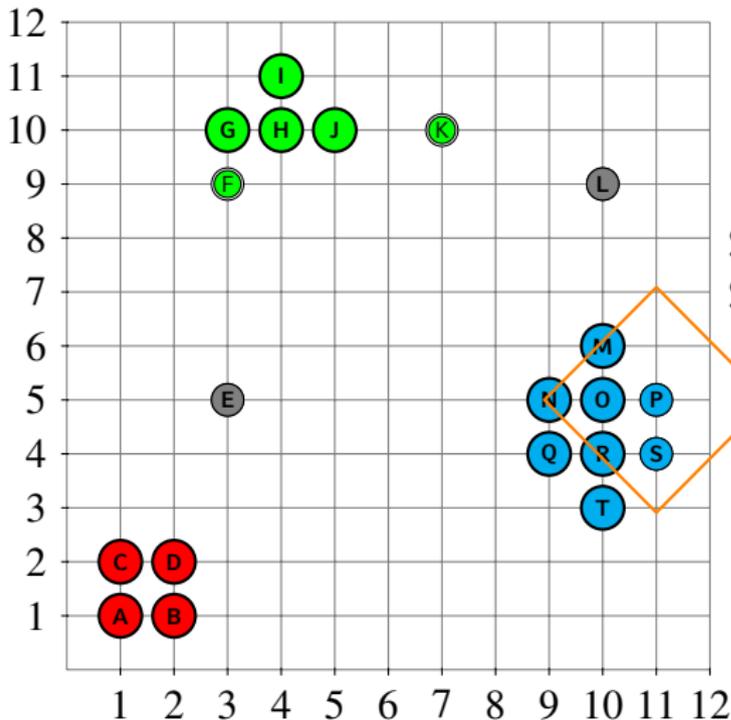
Seed list:
PS



$\epsilon = 2.1$

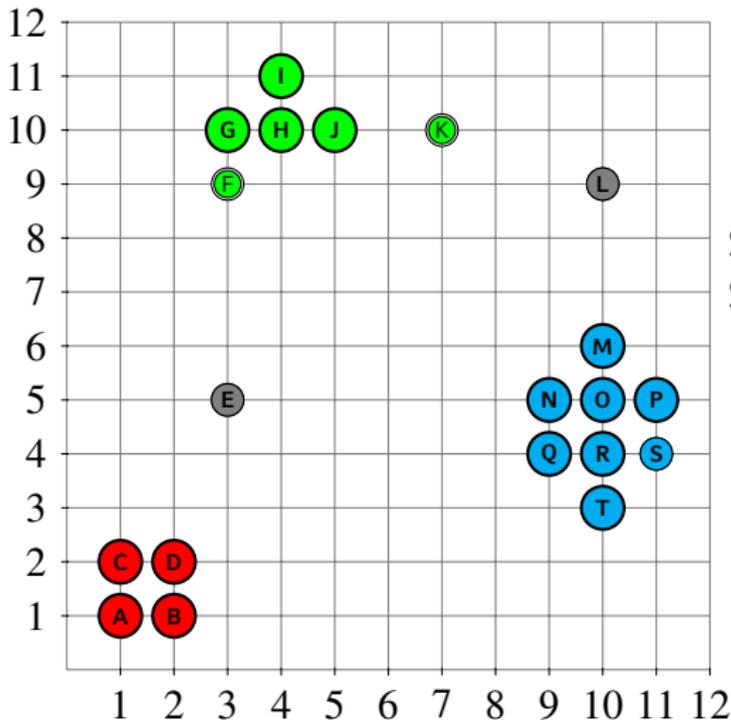
$minPts = 4$

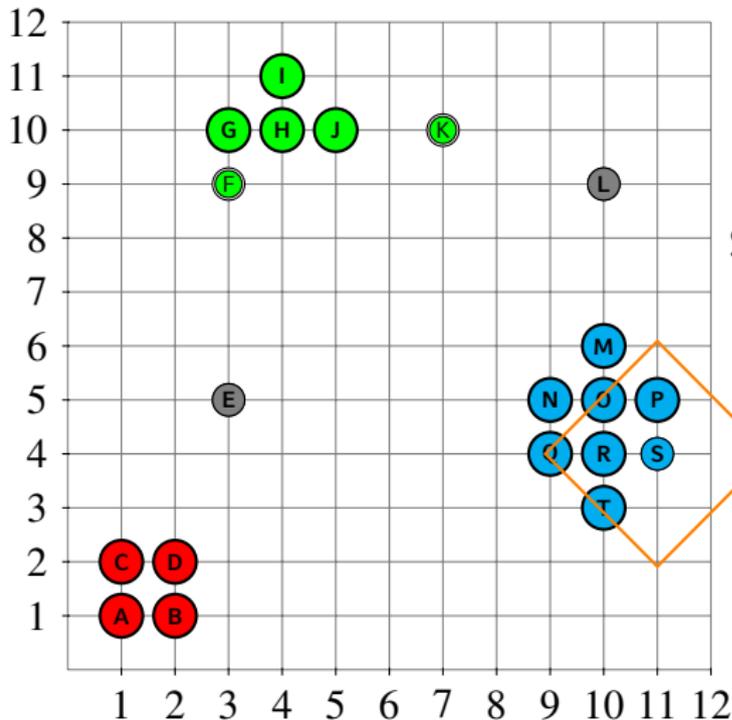
Seed list:
PS

 $\epsilon = 2.1$ $\text{minPts} = 4$

Seed list:

S

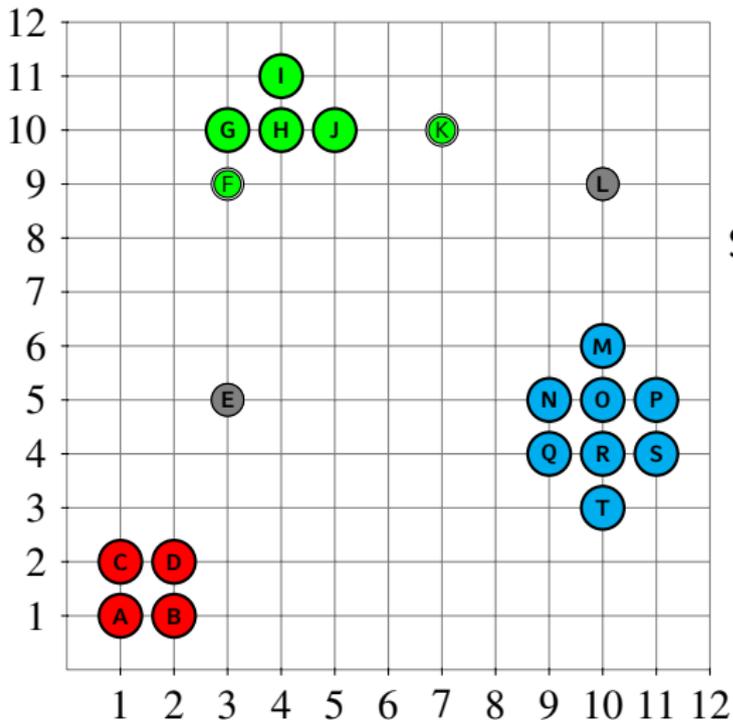
$\epsilon = 1.1$
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 $\text{minPts} = 4$ $\epsilon = 2.1$
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 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 2.1$ $\text{minPts} = 4$ Seed list:
S



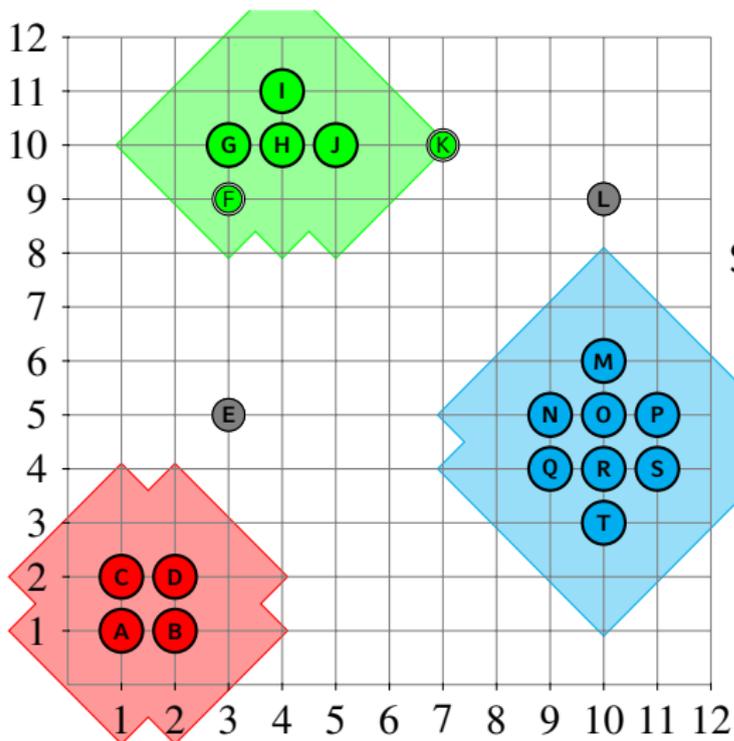
$\epsilon = 2.1$

$minPts = 4$

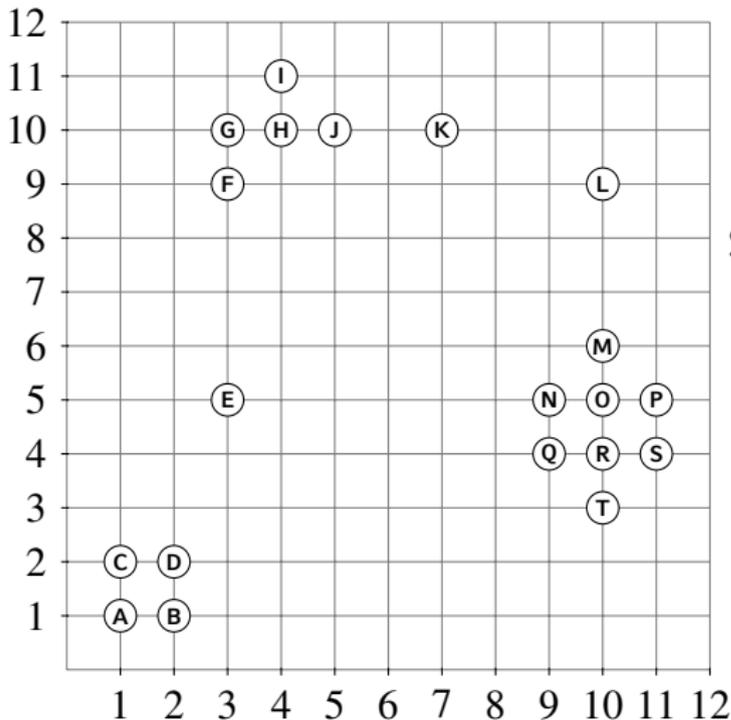
Seed list:

$\epsilon = 1.1$
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 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 2.1$ $\text{minPts} = 4$

Seed list:

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
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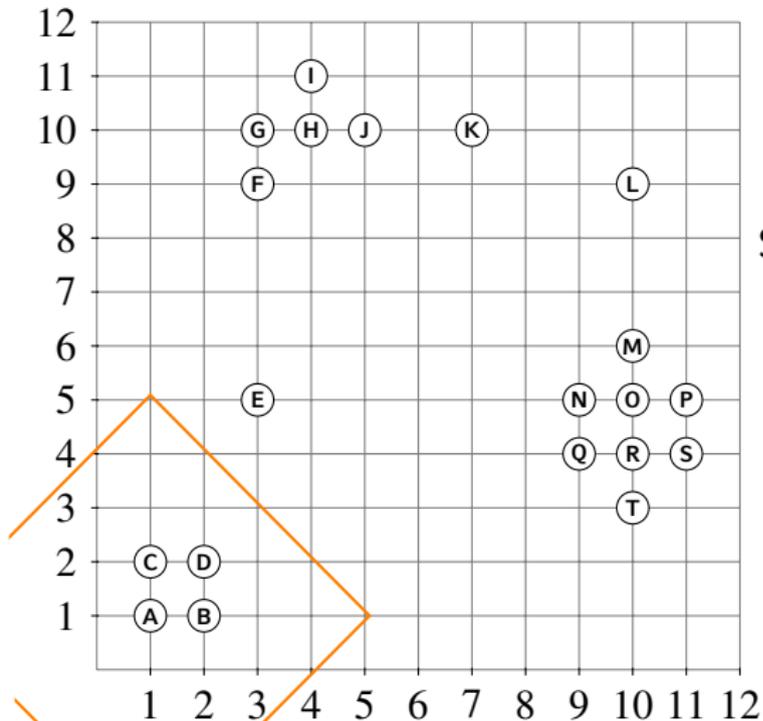
Seed list:



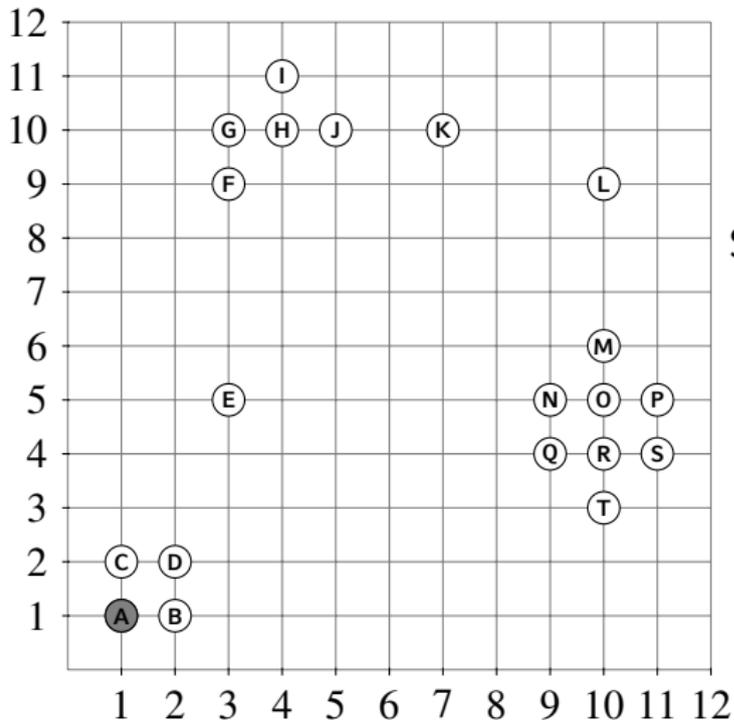
$\epsilon = 4.1$

$\text{minPts} = 5$

Seed list:

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 5$

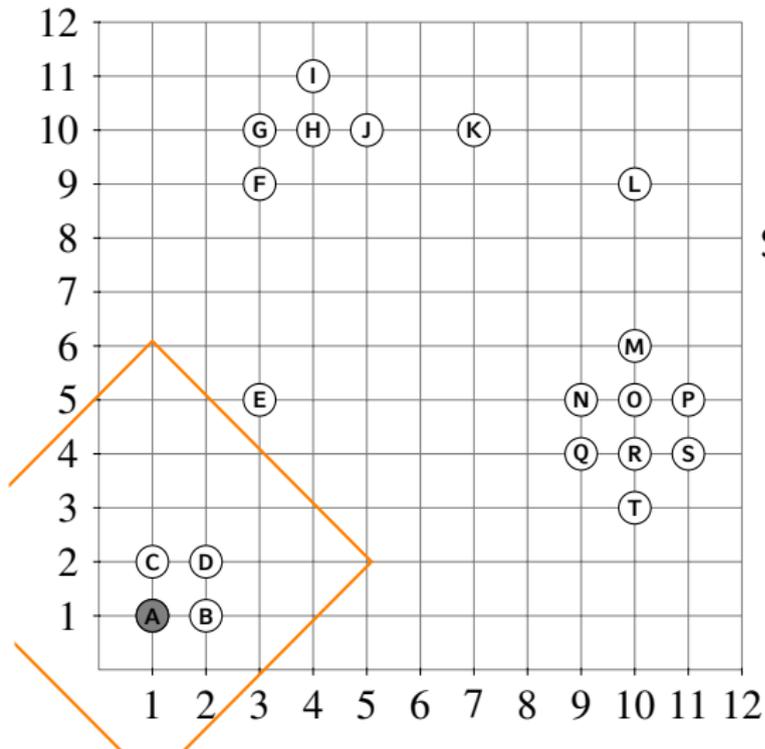
Seed list:



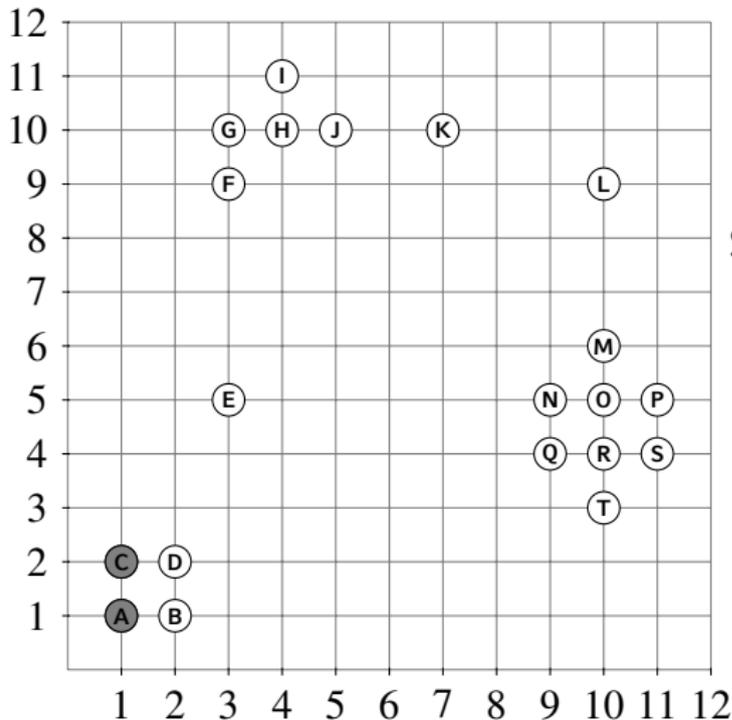
$$\epsilon = 4.1$$

$$\text{minPts} = 5$$

Seed list:

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 5$

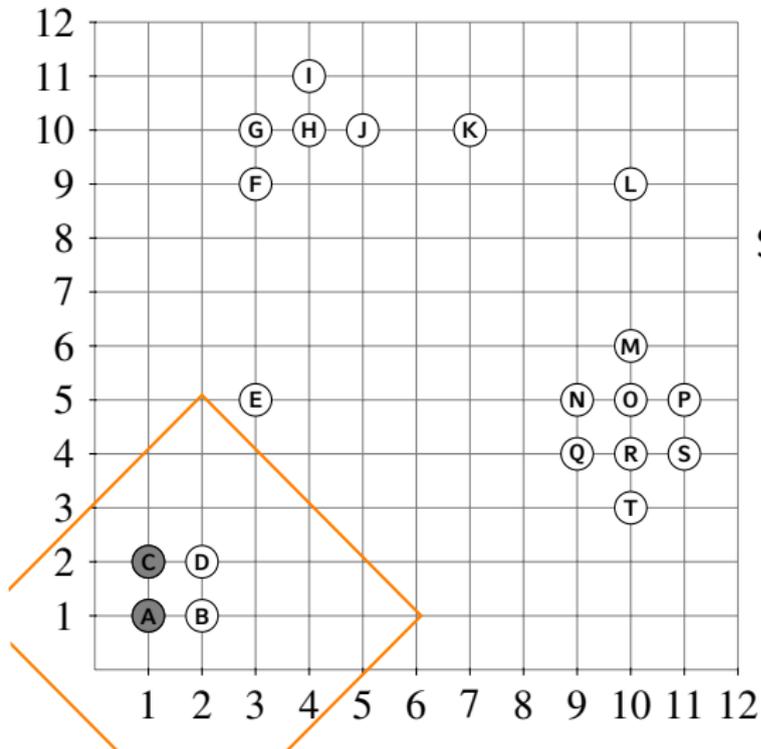
Seed list:



$$\epsilon = 4.1$$

$$\text{minPts} = 5$$

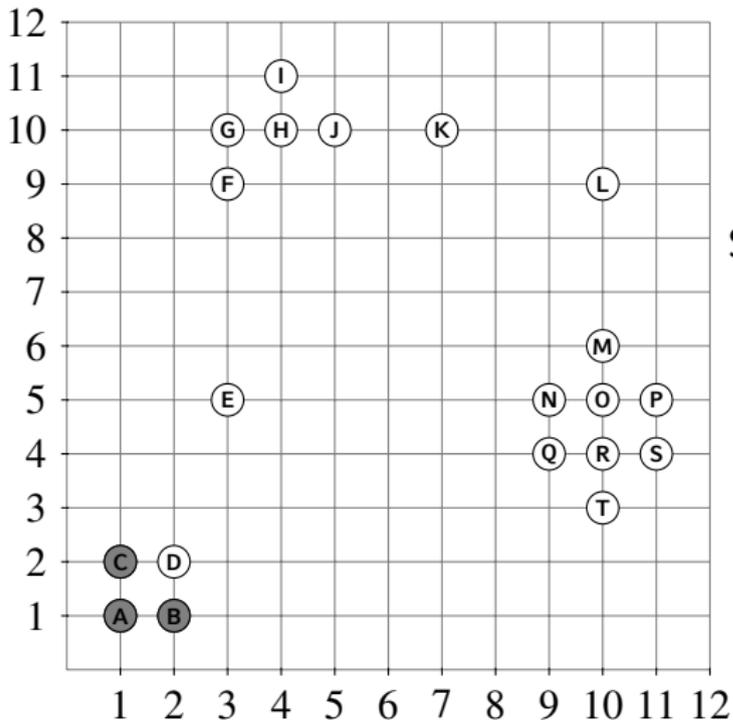
Seed list:



$$\epsilon = 4.1$$

$$\text{minPts} = 5$$

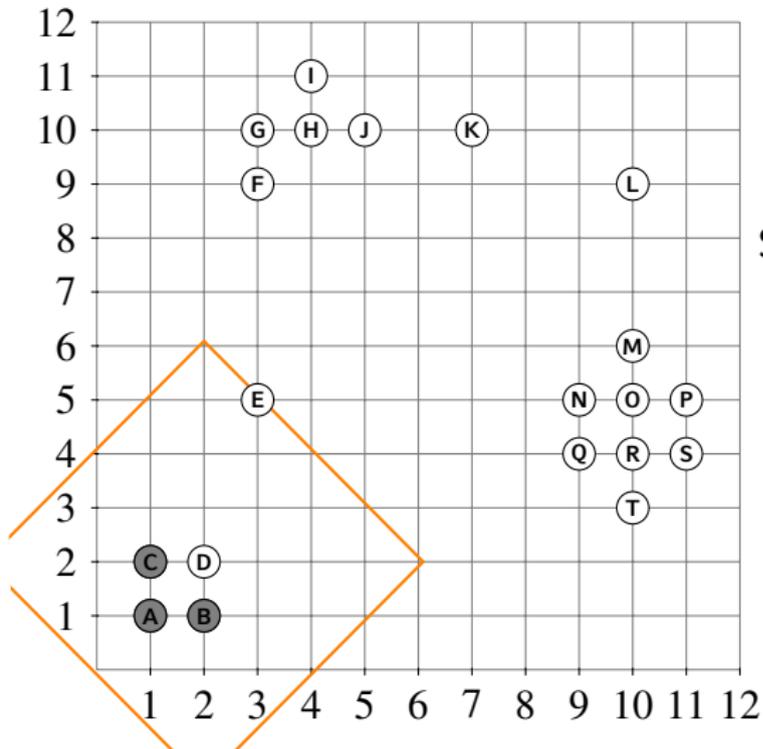
Seed list:



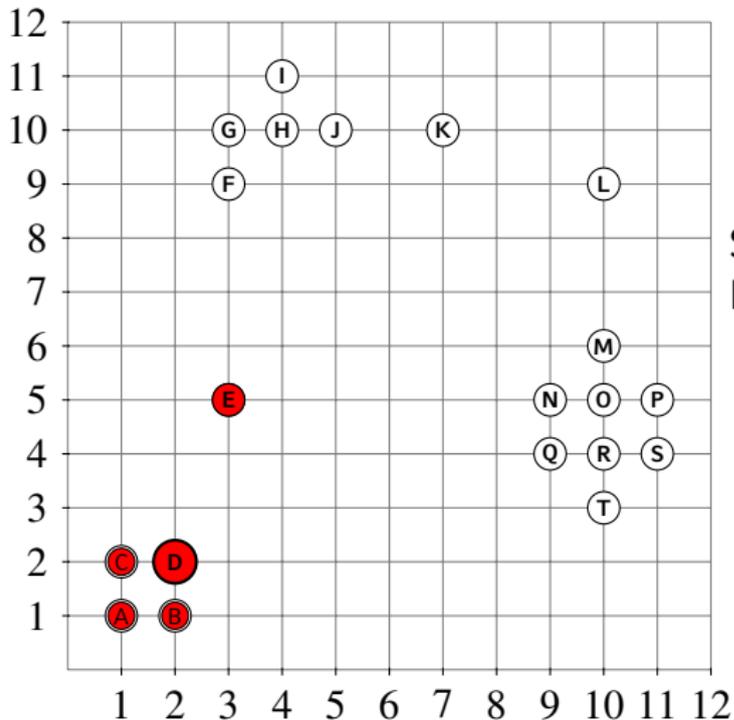
$$\epsilon = 4.1$$

$$\text{minPts} = 5$$

Seed list:

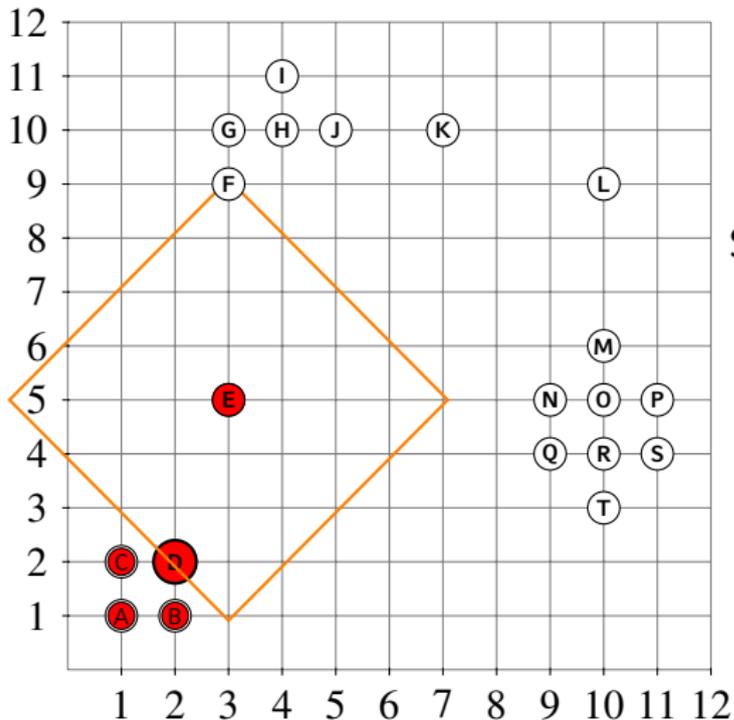
$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
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 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

 $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

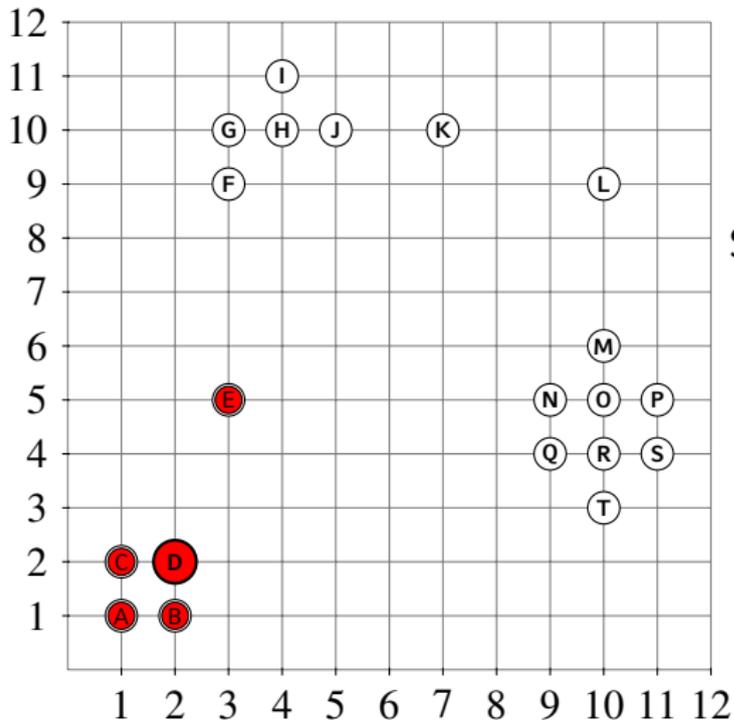
E



$$\epsilon = 4.1$$

$$\text{minPts} = 5$$

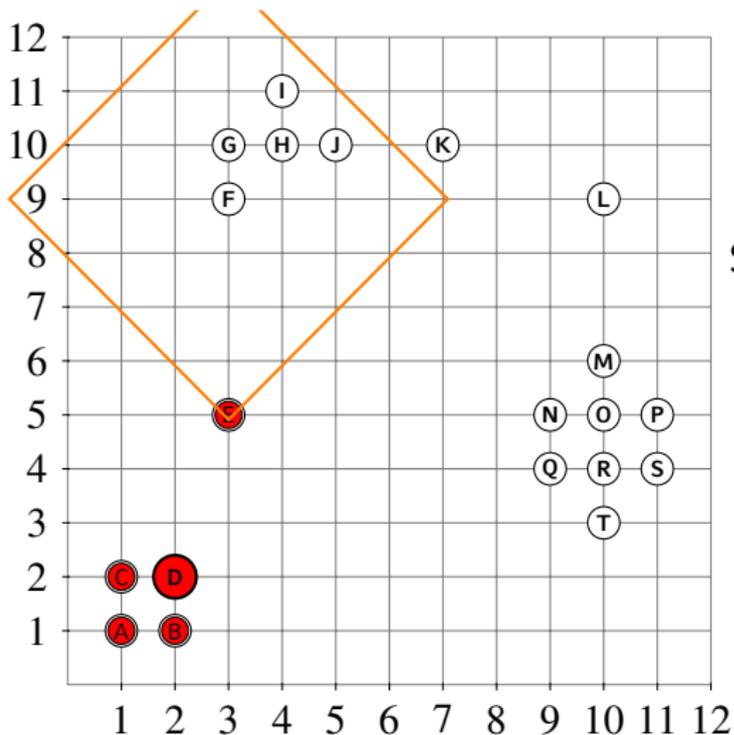
Seed list:



$$\epsilon = 4.1$$

$$\text{minPts} = 5$$

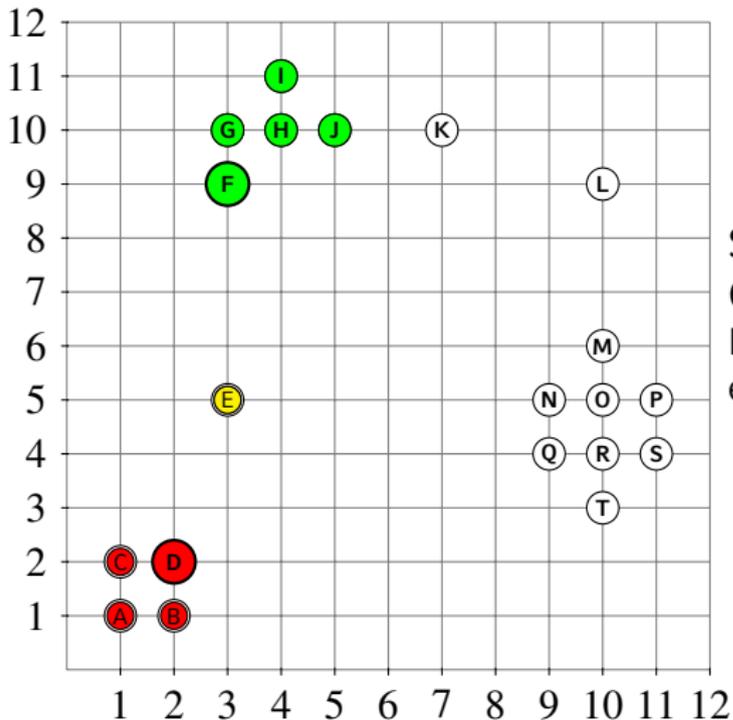
Seed list:



$$\epsilon = 4.1$$

$$\text{minPts} = 5$$

Seed list:



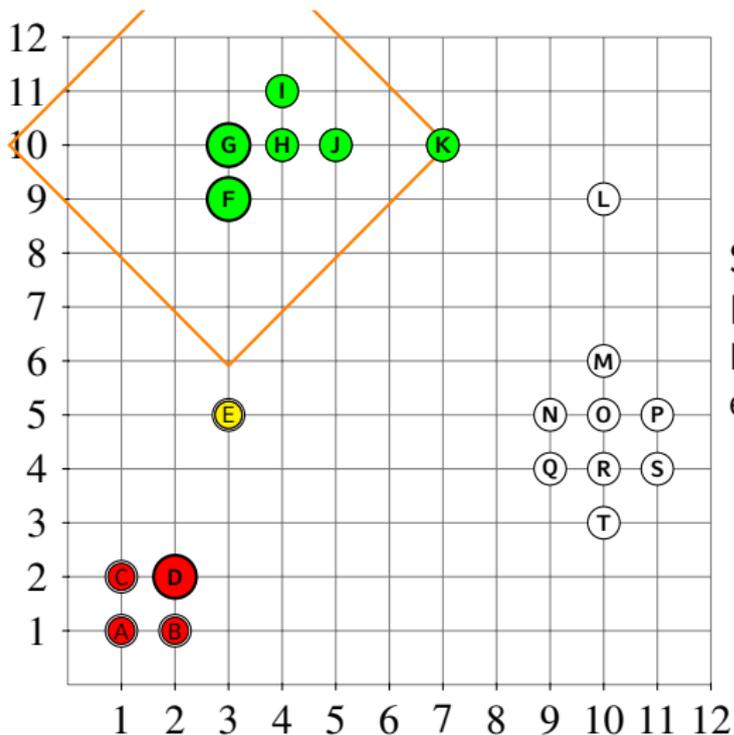
$$\epsilon = 4.1$$

$$\text{minPts} = 5$$

Seed list:

GHIJ

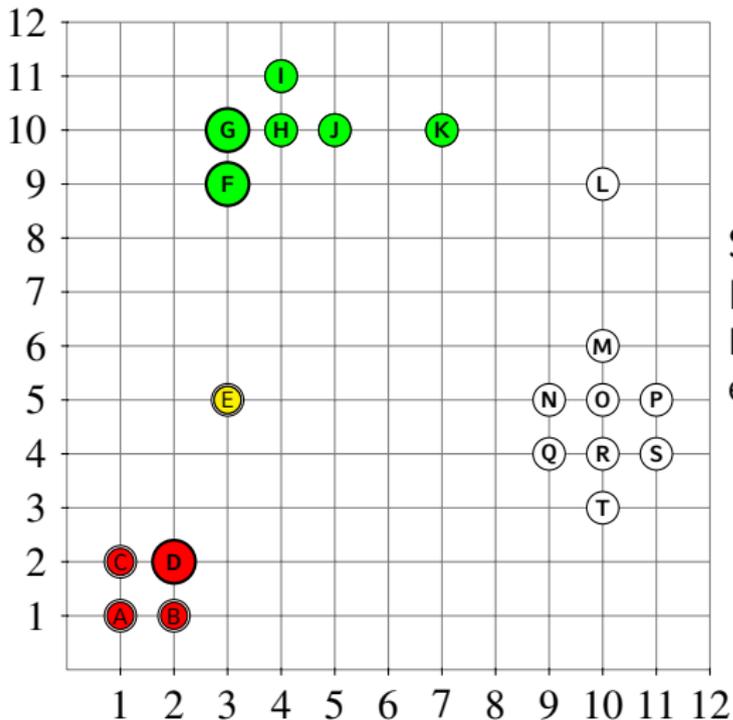
E nicht
eindeutig!

 $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

HIJ

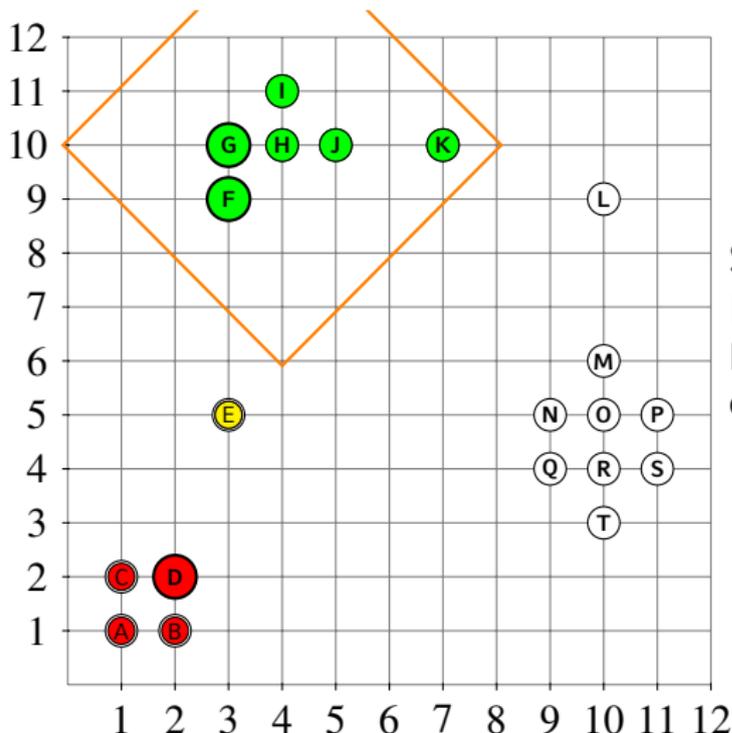
E nicht
eindeutig!

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

HIJK

E nicht
eindeutig!



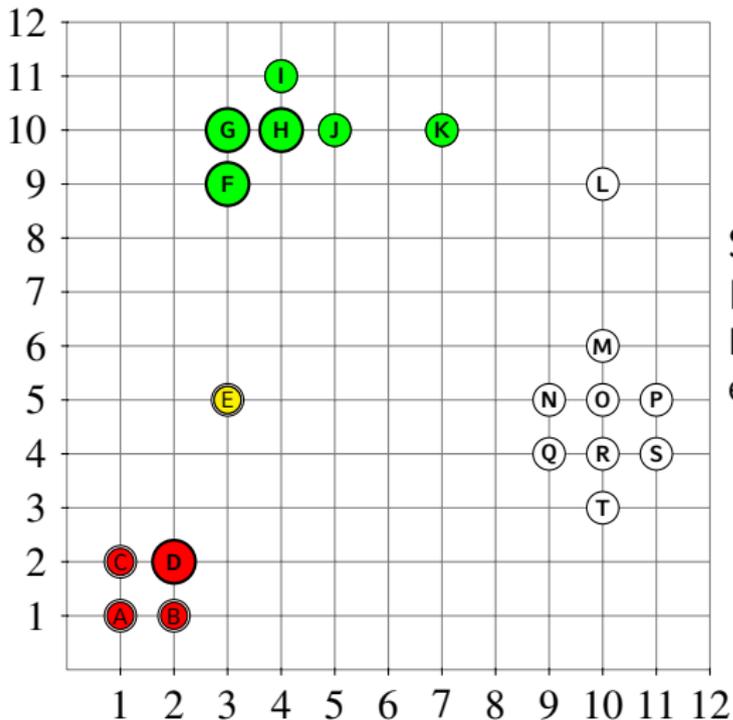
$\epsilon = 4.1$

$\text{minPts} = 5$

Seed list:

IJK

E nicht
eindeutig!

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

IJK

E nicht
eindeutig!

$\epsilon = 1.1$
 $minPts = 2$

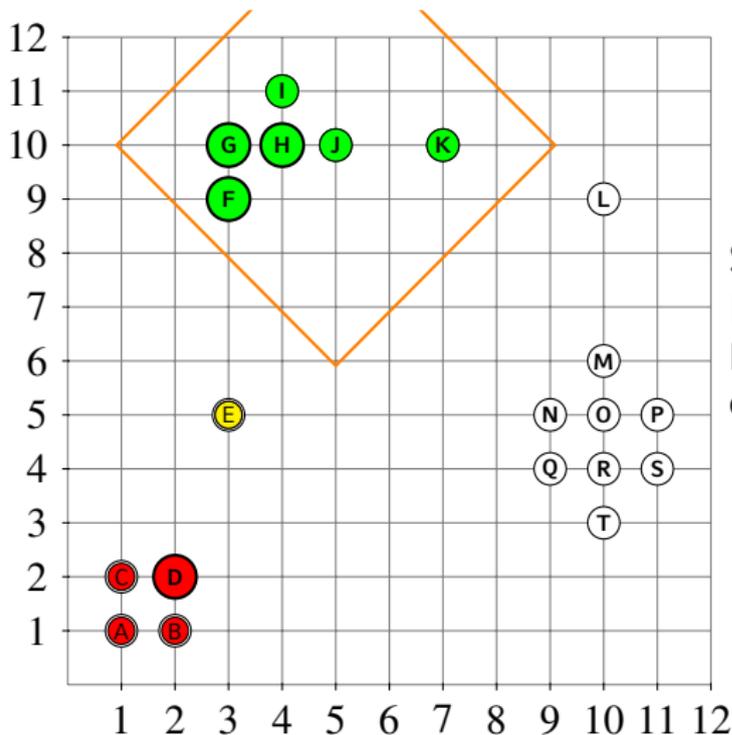
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 $minPts = 3$

$\epsilon = 1.1$
 $minPts = 4$

$\epsilon = 2.1$
 $minPts = 4$

$\epsilon = 4.1$
 $minPts = 5$

$\epsilon = 4.1$
 $minPts = 4$



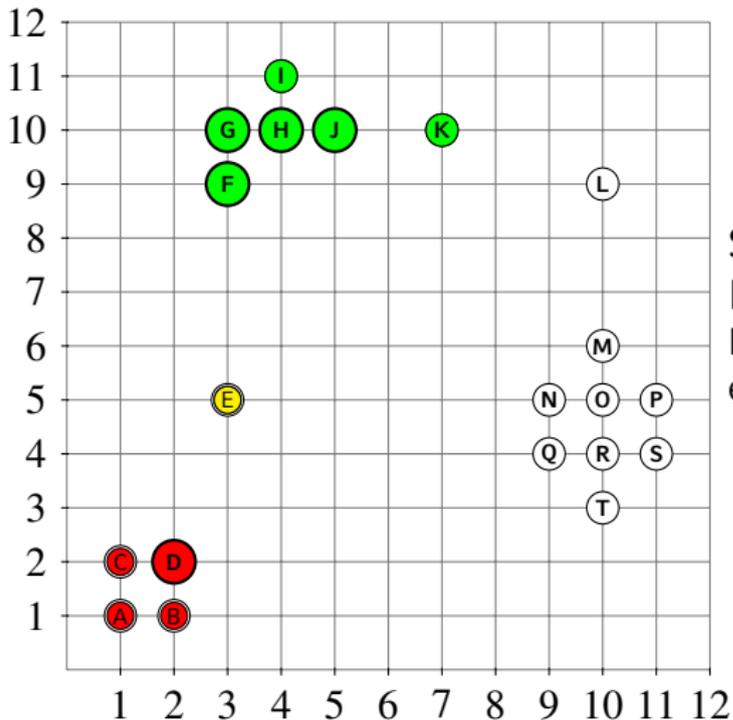
$\epsilon = 4.1$

$minPts = 5$

Seed list:

IK

E nicht
eindeutig!



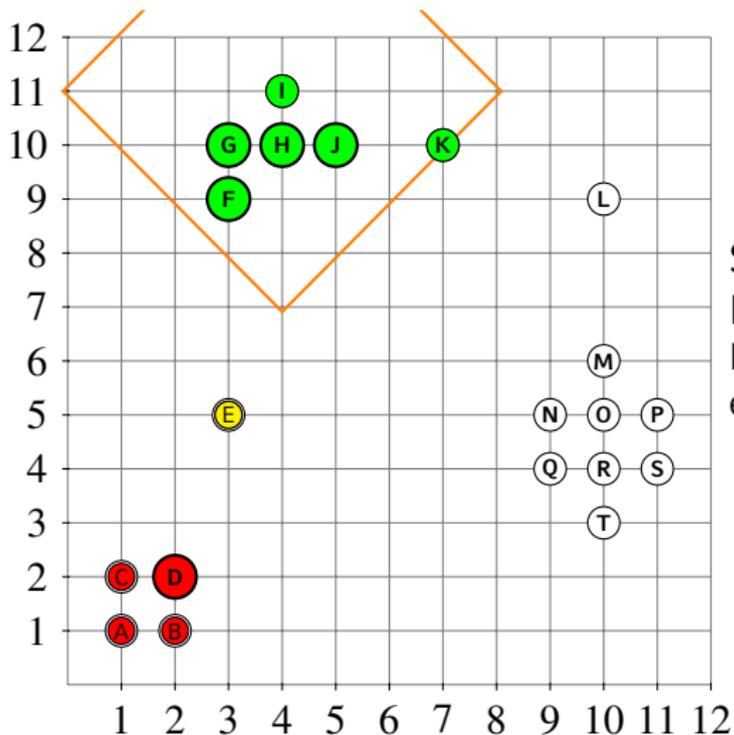
$\epsilon = 4.1$

$\text{minPts} = 5$

Seed list:

IK

E nicht
eindeutig!



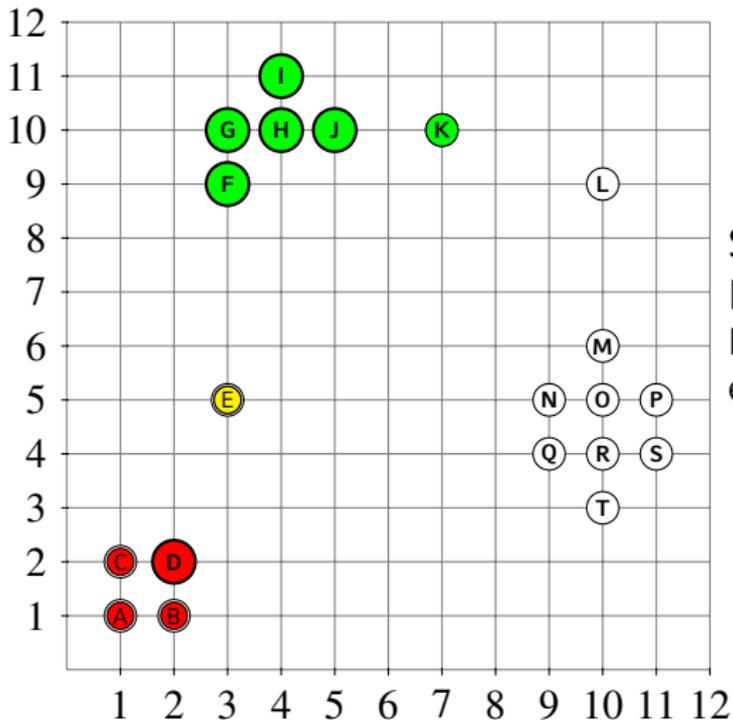
$$\epsilon = 4.1$$

$$\text{minPts} = 5$$

Seed list:

K

E nicht
eindeutig!

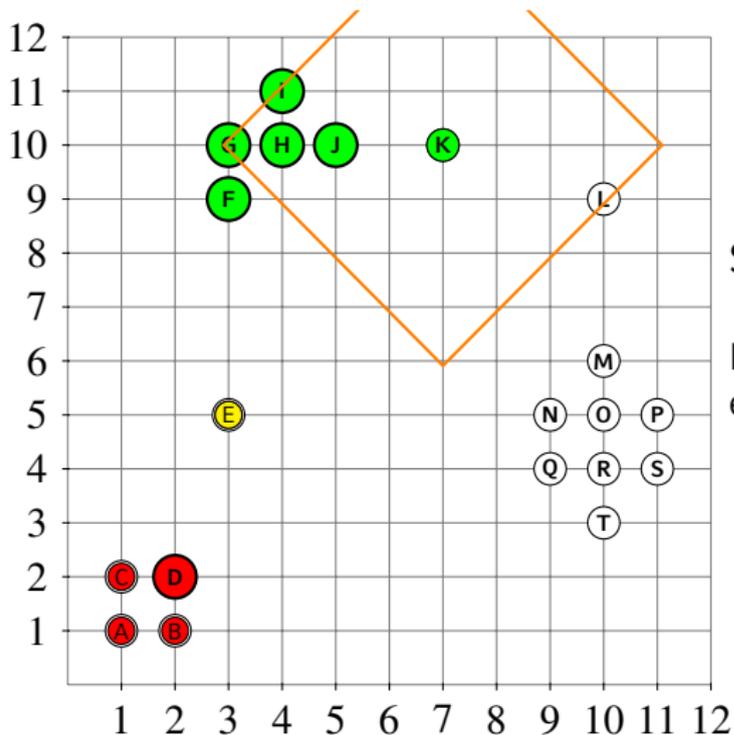
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Seed list:

K

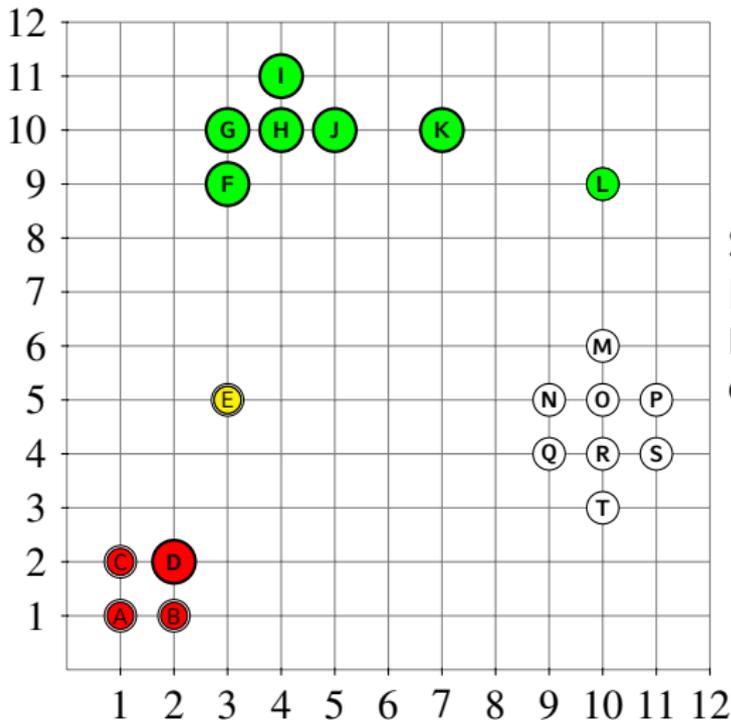
E nicht

eindeutig!

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 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

E nicht
eindeutig!



$\epsilon = 4.1$

$\text{minPts} = 5$

Seed list:

L

E nicht
eindeutig!

$\epsilon = 1.1$
 $\text{minPts} = 2$

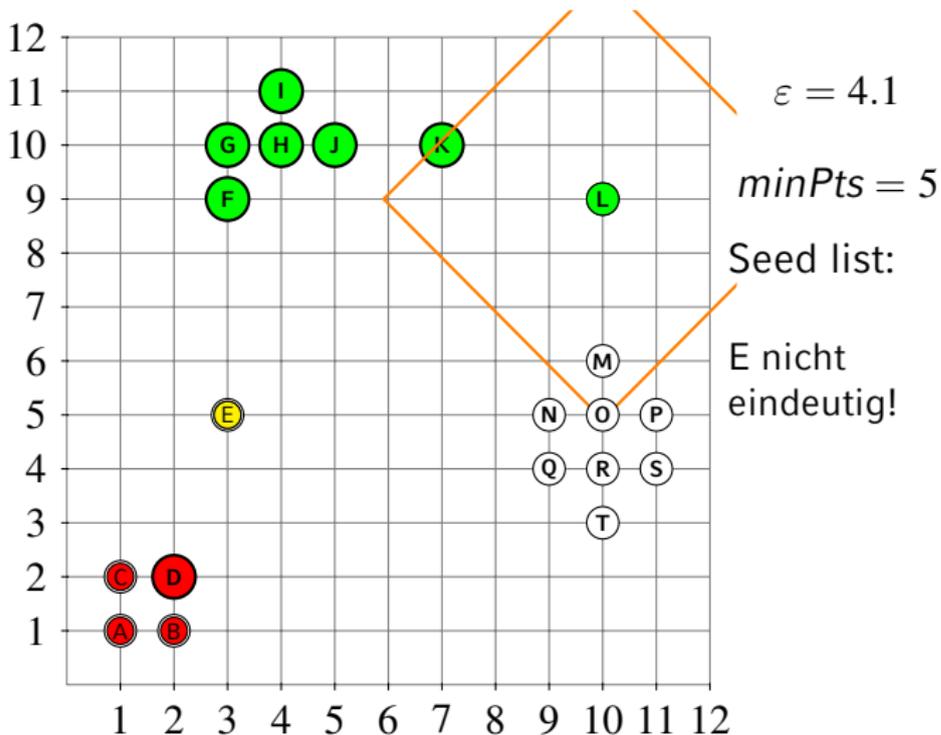
$\epsilon = 1.1$
 $\text{minPts} = 3$

$\epsilon = 1.1$
 $\text{minPts} = 4$

$\epsilon = 2.1$
 $\text{minPts} = 4$

$\epsilon = 4.1$
 $\text{minPts} = 5$

$\epsilon = 4.1$
 $\text{minPts} = 4$



$\epsilon = 1.1$
 $minPts = 2$

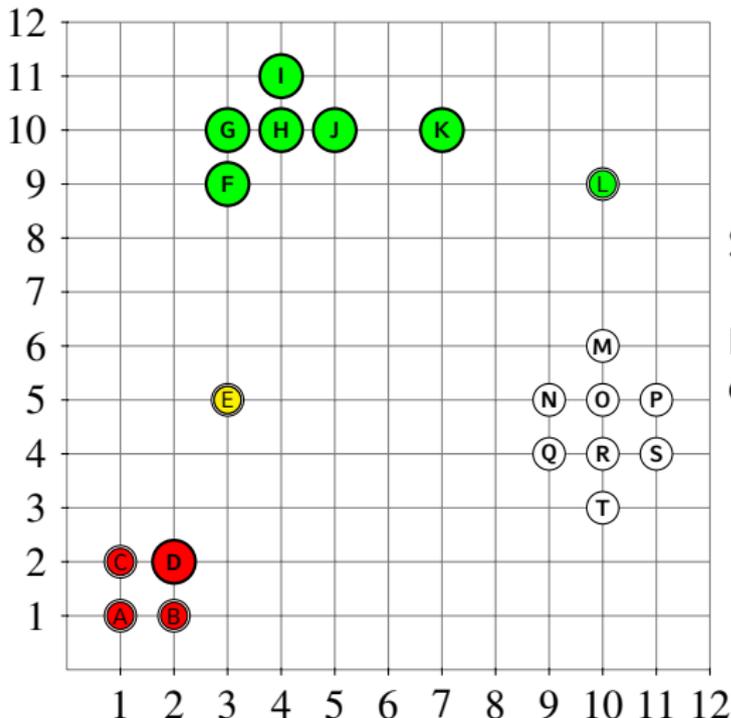
$\epsilon = 1.1$
 $minPts = 3$

$\epsilon = 1.1$
 $minPts = 4$

$\epsilon = 2.1$
 $minPts = 4$

$\epsilon = 4.1$
 $minPts = 5$

$\epsilon = 4.1$
 $minPts = 4$

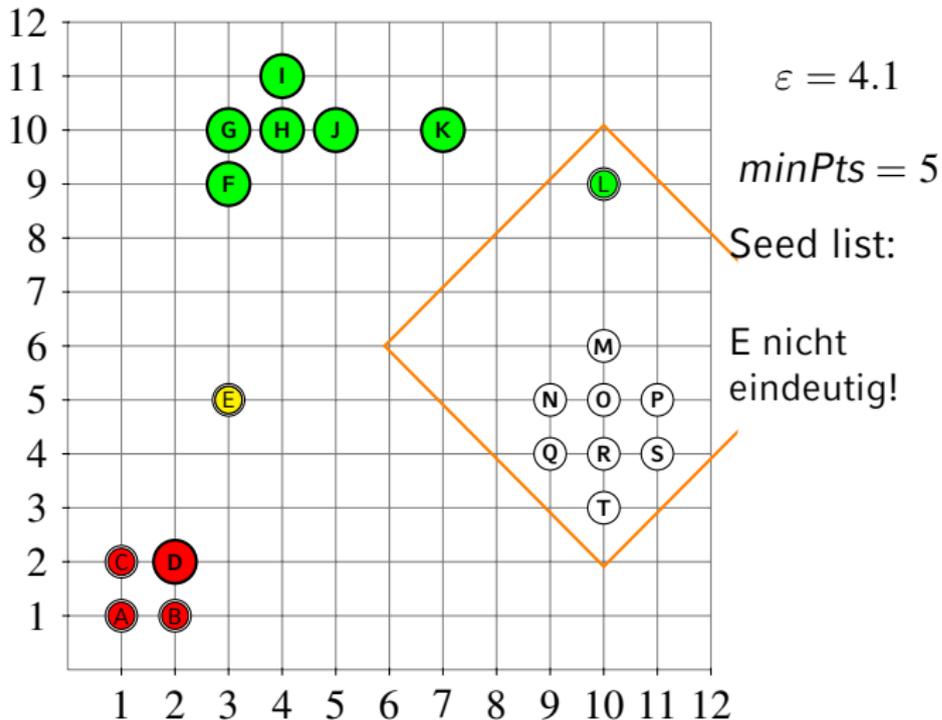


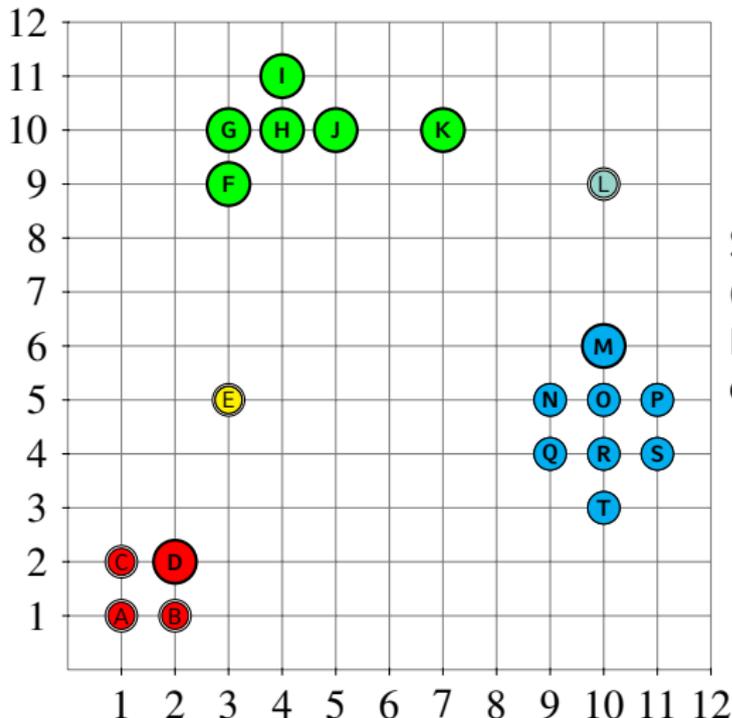
$\epsilon = 4.1$

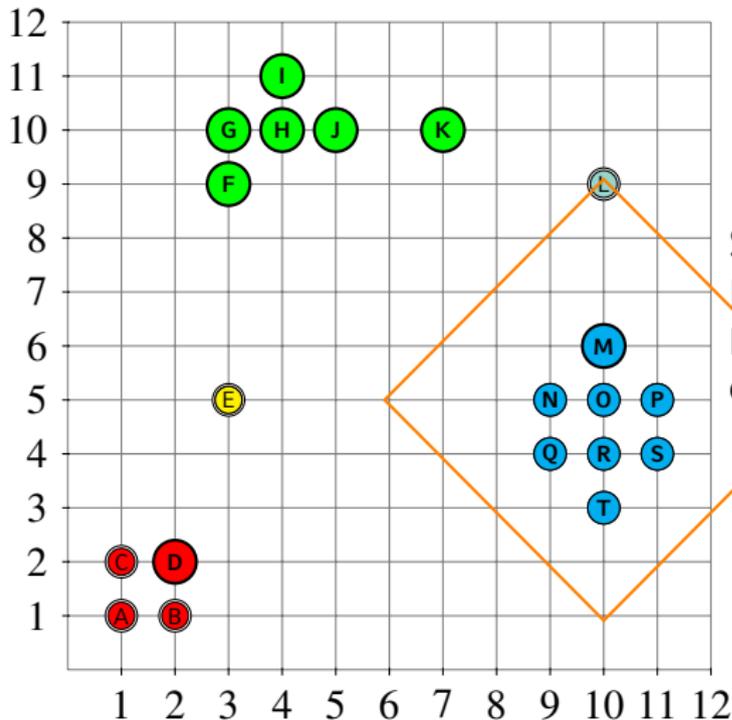
$minPts = 5$

Seed list:

E nicht
eindeutig!

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
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 $\text{minPts} = 4$ 

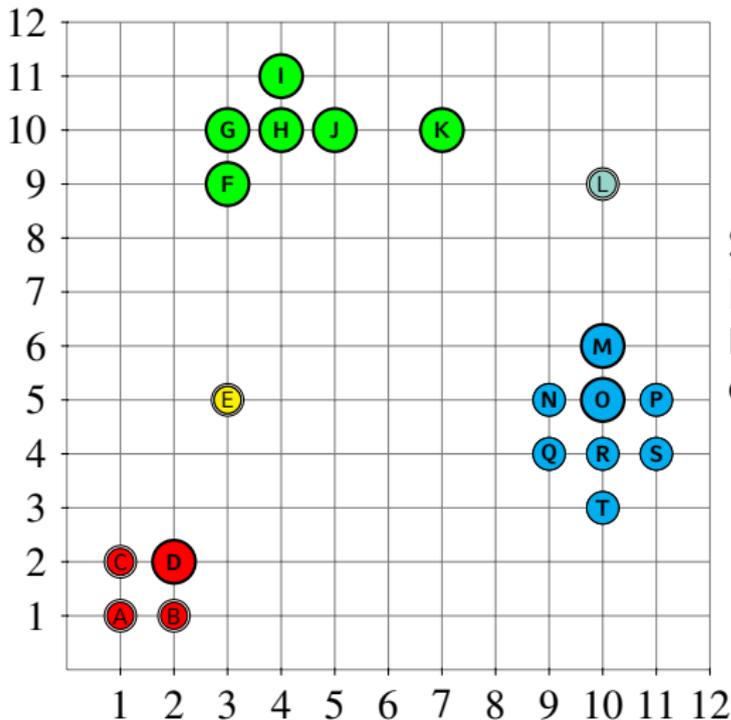
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 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 5$ Seed list:
ONPRQST
E und L nicht
eindeutig!

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

NPQST

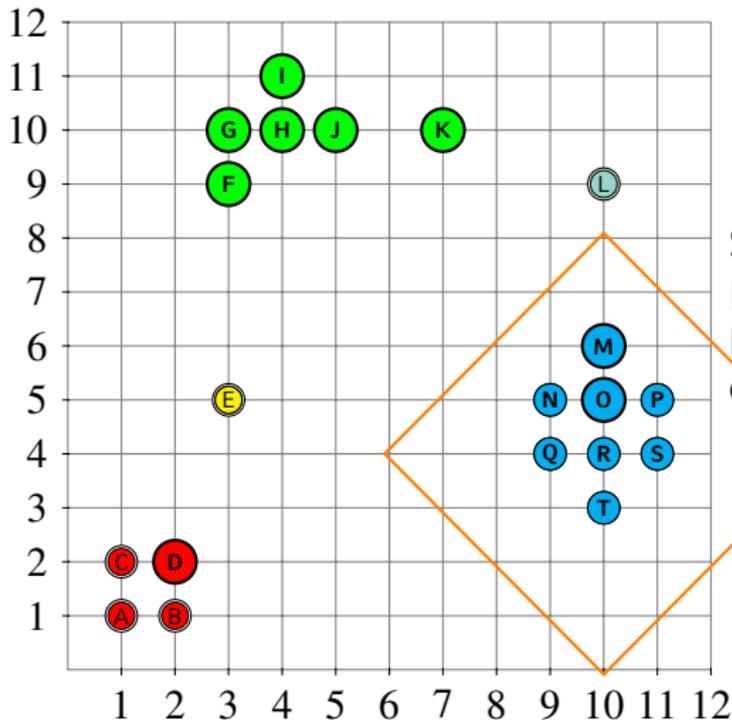
E und L
nicht
eindeutig!

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

NPQST

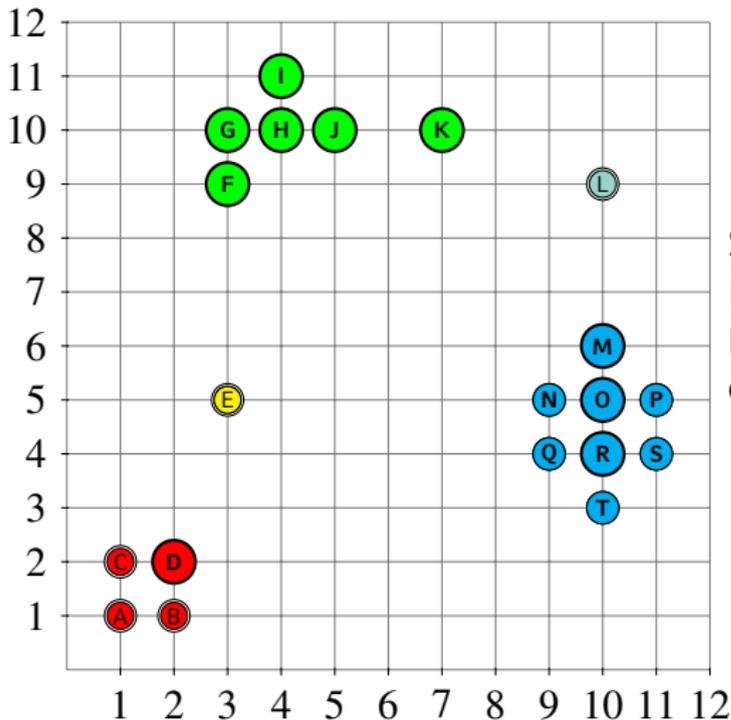
E und L nicht
eindeutig!

 $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

NPQST

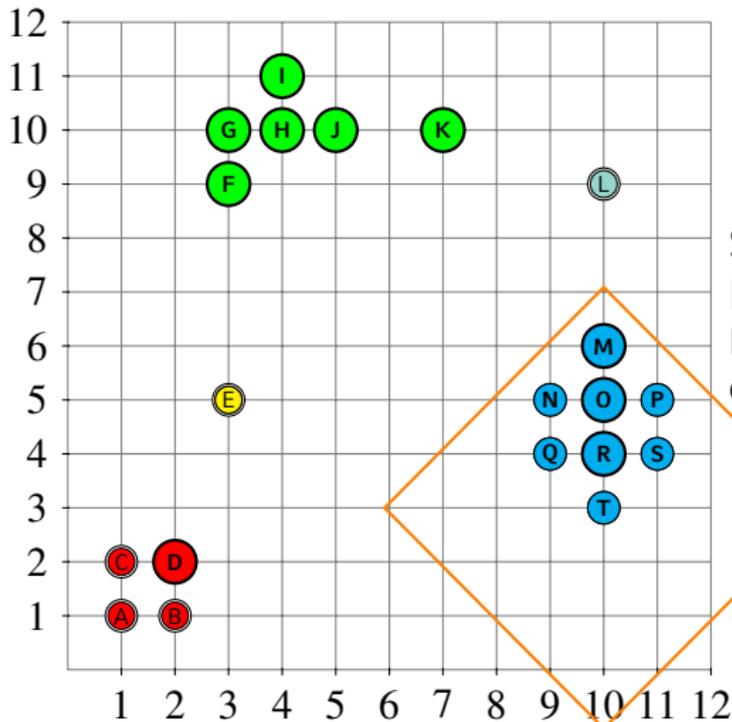
E und L nicht
eindeutig!

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

NPQST

E und L nicht
eindeutig!



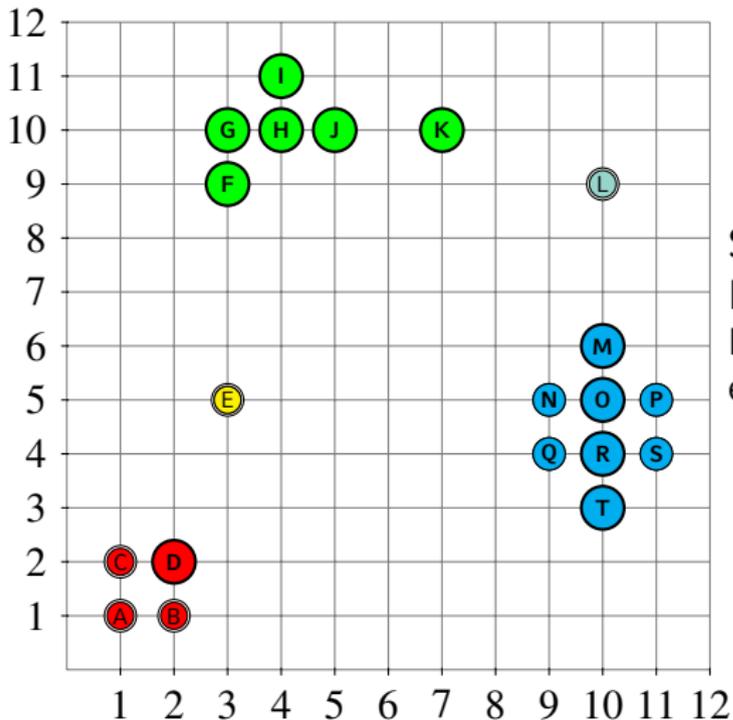
$\epsilon = 4.1$

$\text{minPts} = 5$

Seed list:

NPQS

E und L
eindeutig!



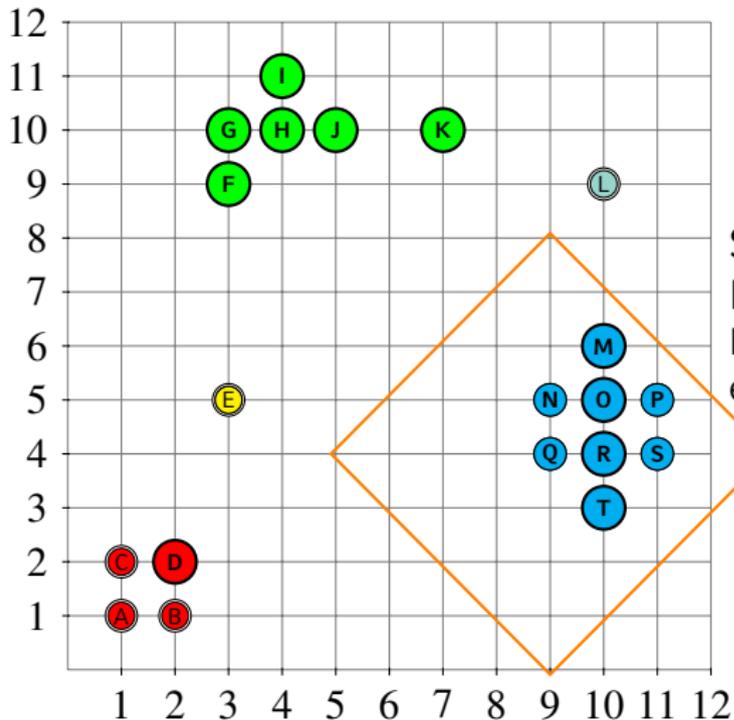
$$\epsilon = 4.1$$

$$\text{minPts} = 5$$

Seed list:

NPQS

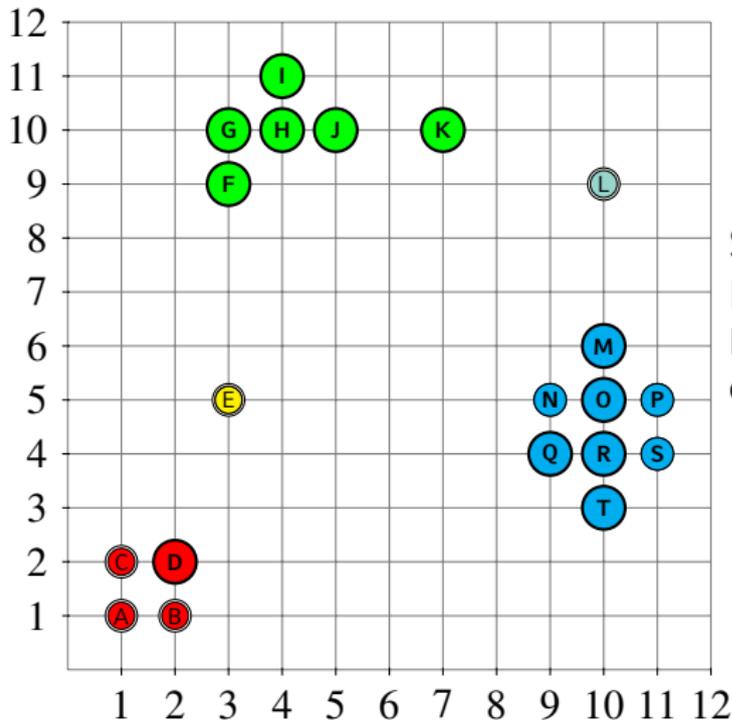
E und L nicht
eindeutig!

 $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

NPS

E und L nicht
eindeutig!



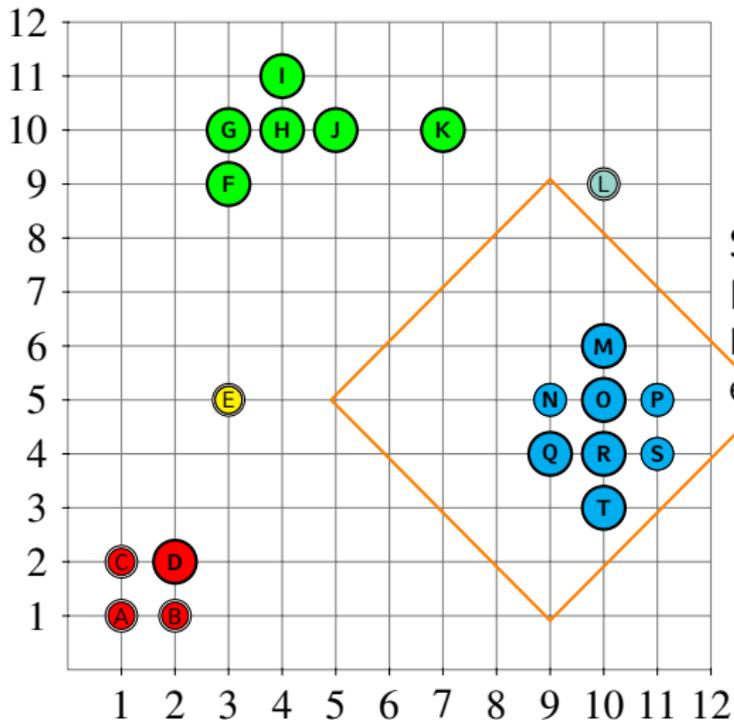
$$\epsilon = 4.1$$

$$\text{minPts} = 5$$

Seed list:

NPS

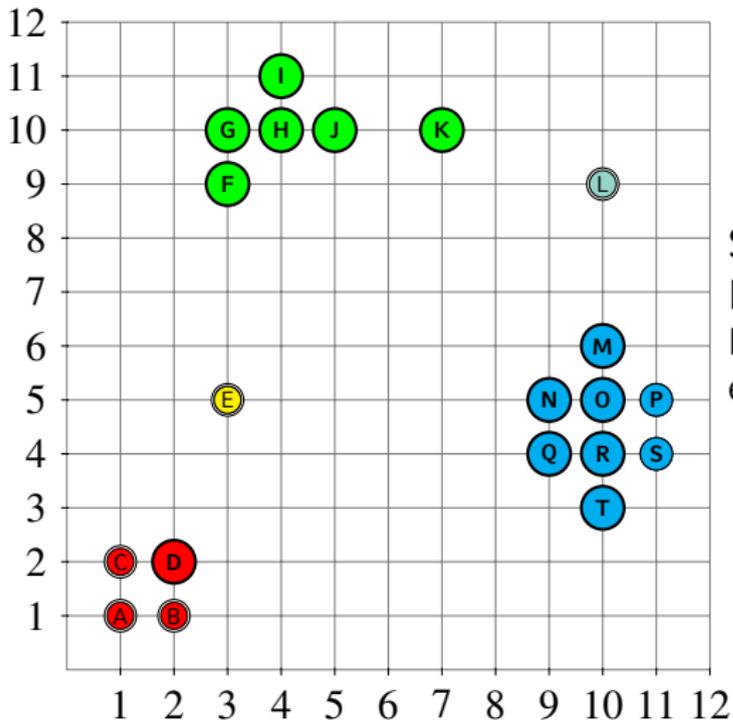
E und L nicht
eindeutig!

$\epsilon = 1.1$
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 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

PS

E und L nicht
eindeutig!



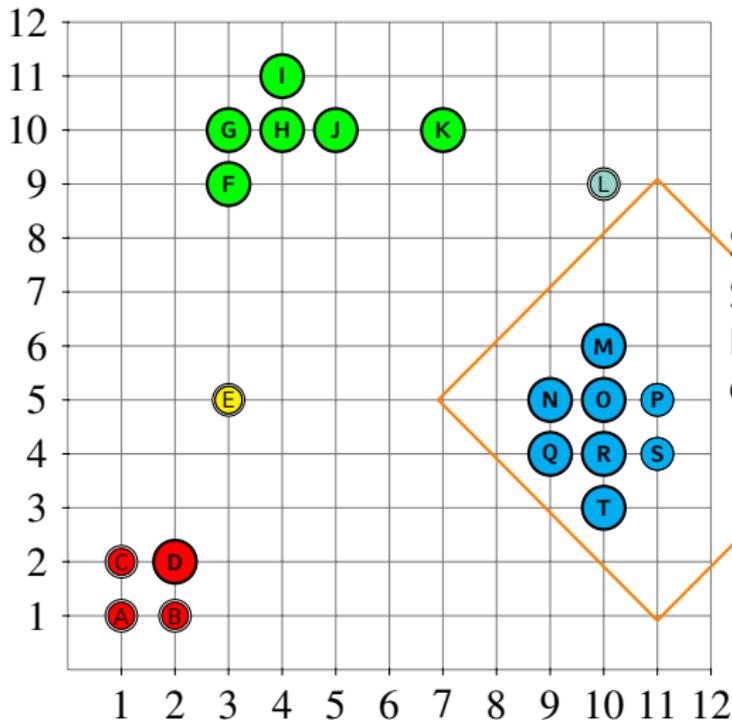
$$\epsilon = 4.1$$

$$\text{minPts} = 5$$

Seed list:

PS

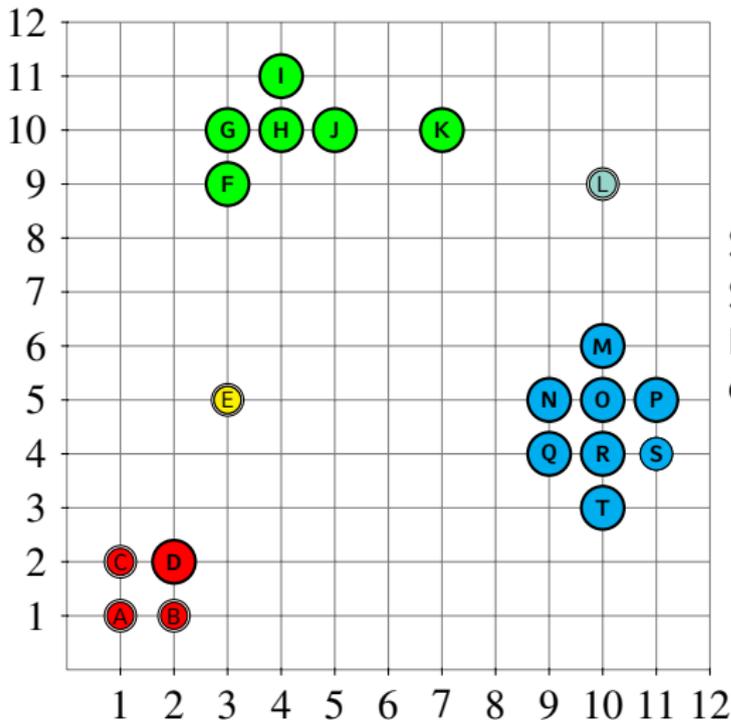
E und L
nicht
eindeutig!

 $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

S

E und L nicht
eindeutig!



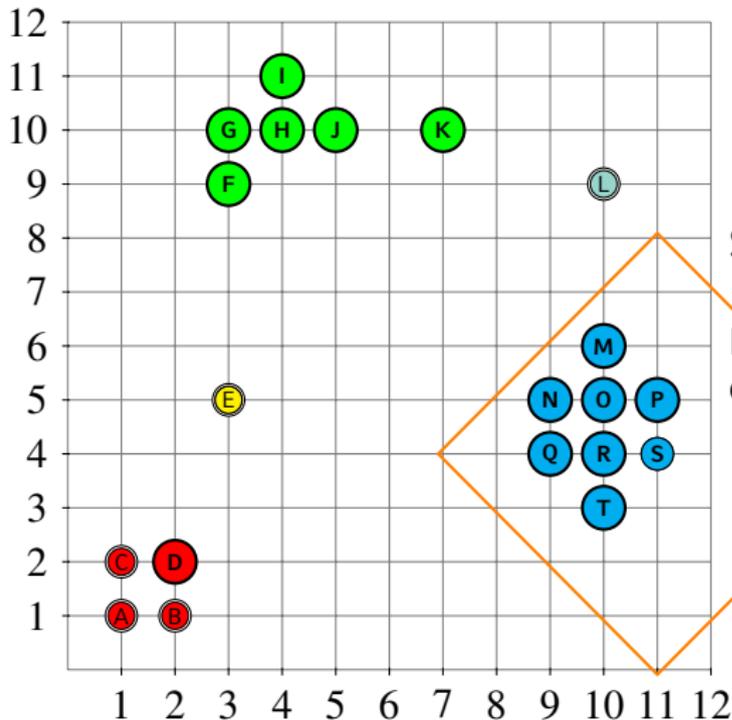
$\epsilon = 4.1$

$\text{minPts} = 5$

Seed list:

S

E und L nicht
eindeutig!

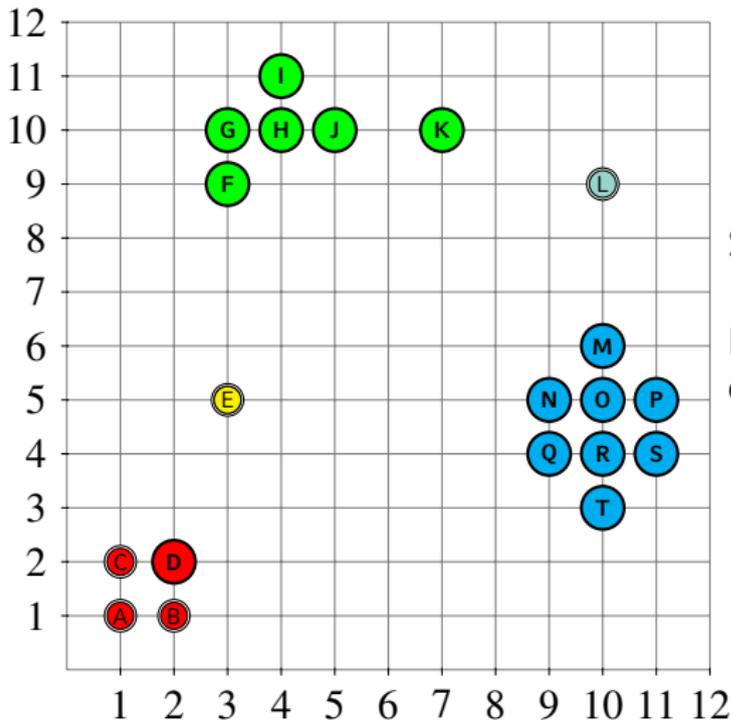


$\epsilon = 4.1$

$minPts = 5$

Seed list:

E und L nicht
eindeutig!

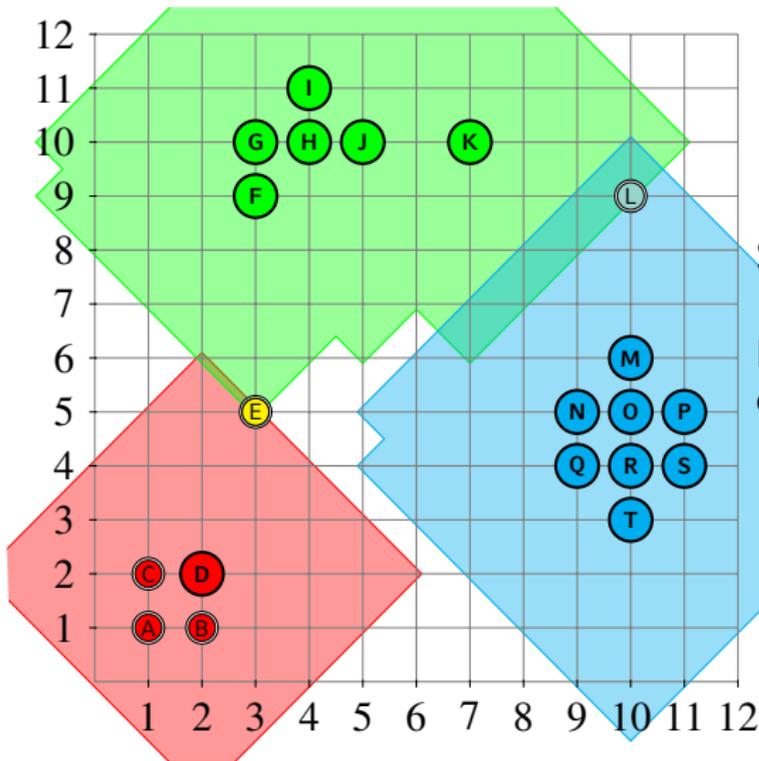


$\epsilon = 4.1$

$\text{minPts} = 5$

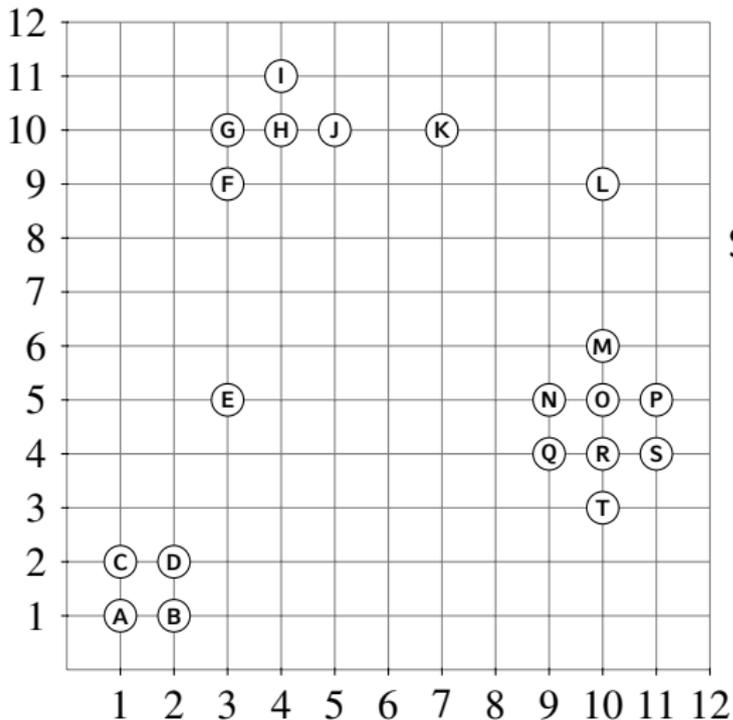
Seed list:

E und L nicht
eindeutig!

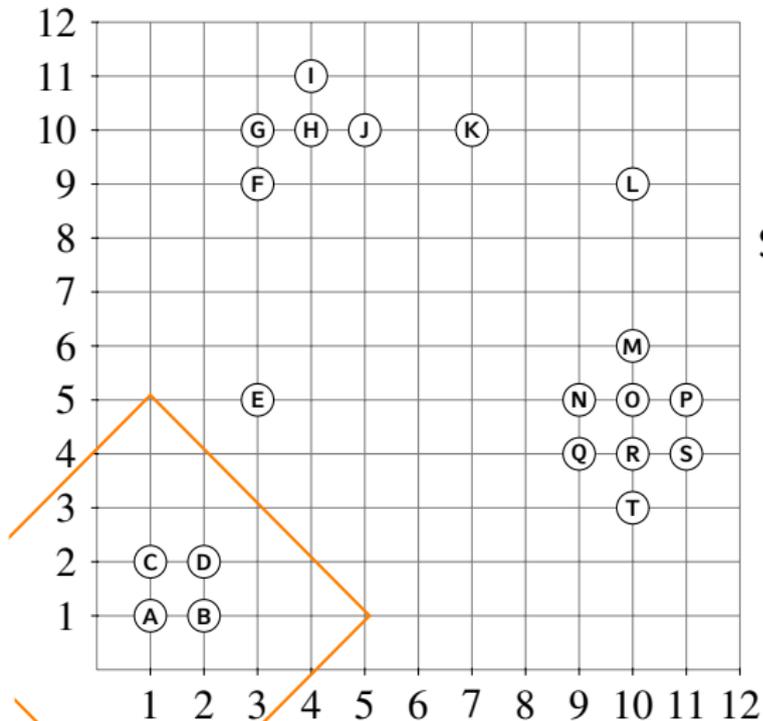
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 $\text{minPts} = 4$ $\epsilon = 4.1$
 $\text{minPts} = 5$ $\epsilon = 4.1$
 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 5$

Seed list:

E und L nicht
eindeutig!

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
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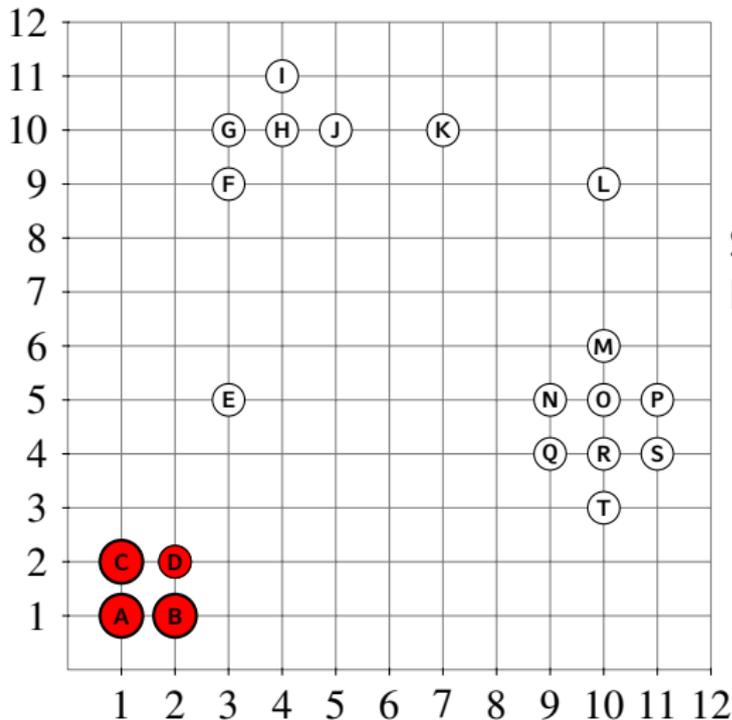
Seeds:



$\epsilon = 4.1$

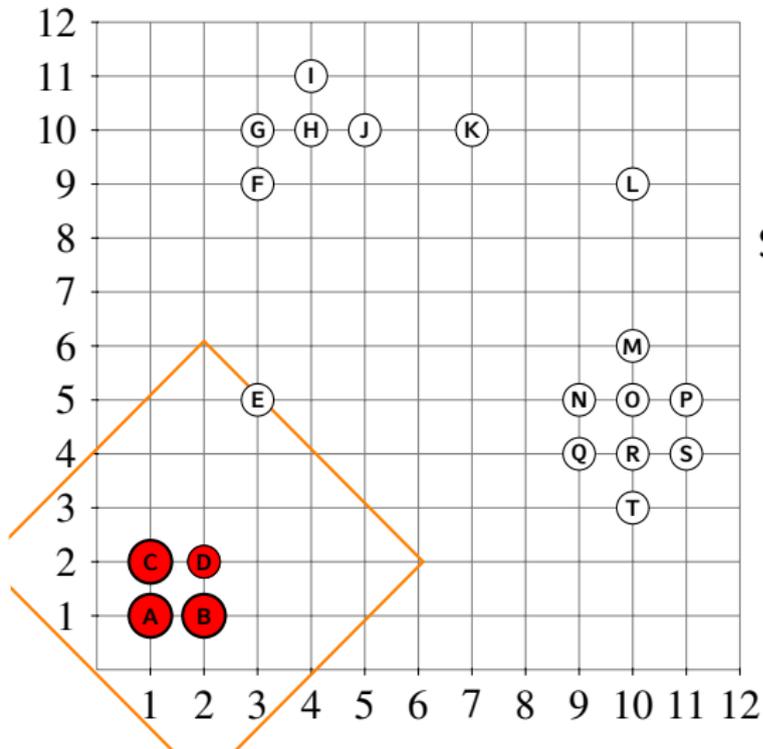
$\text{minPts} = 4$

Seeds:

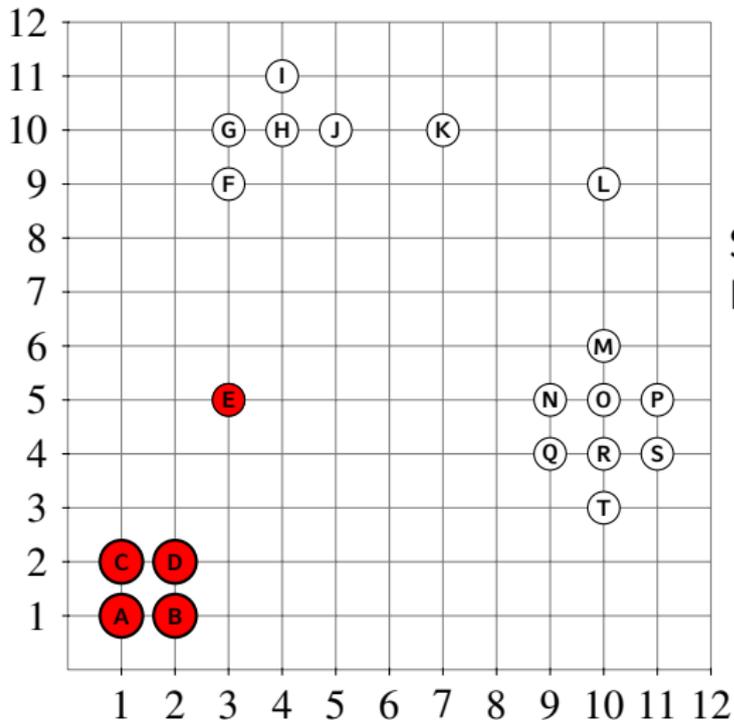
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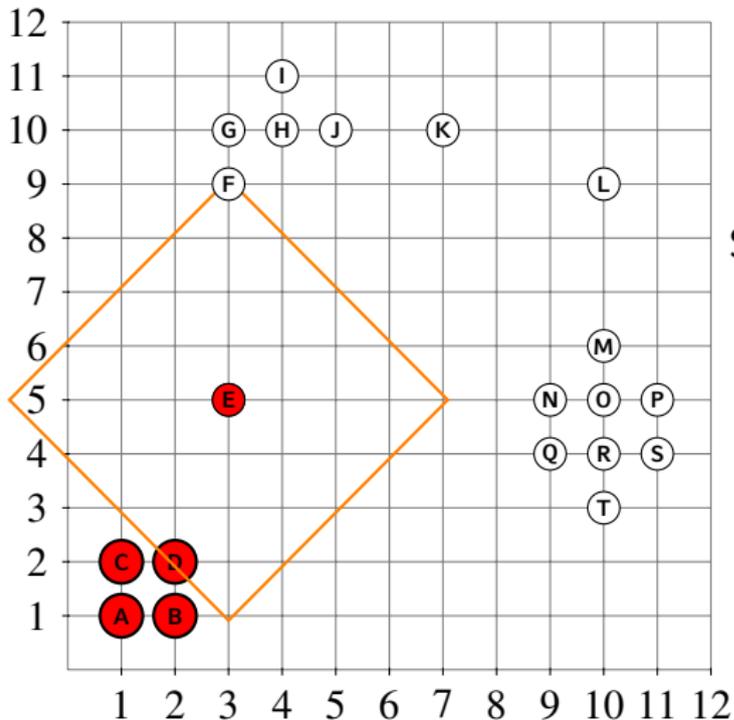
Seeds:

D

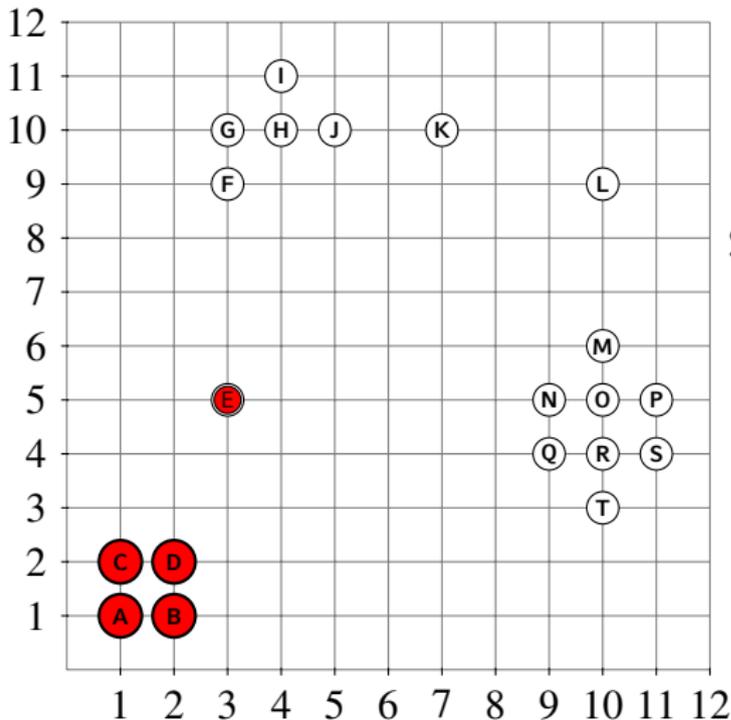
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Seeds:

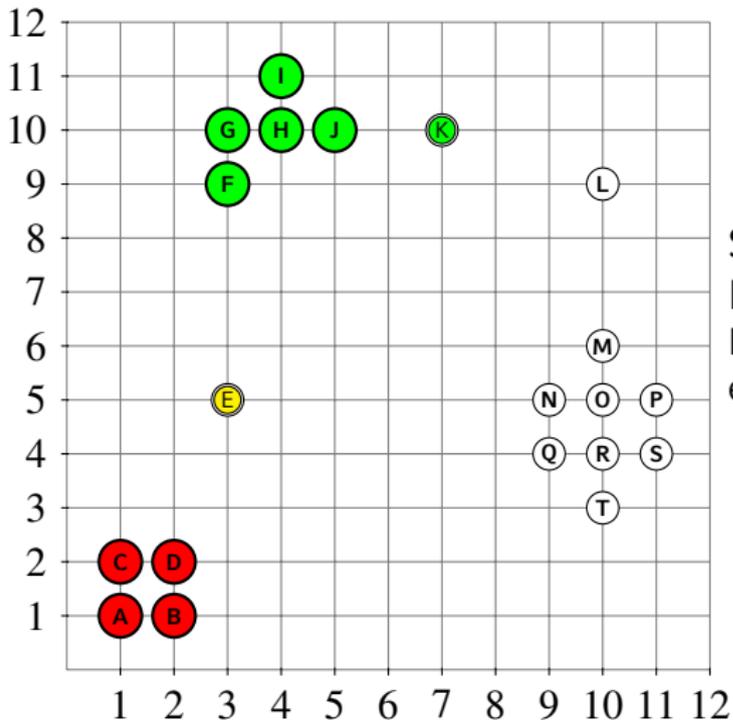


$\epsilon = 1.1$
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 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 4$

Seeds:

$\epsilon = 1.1$
 $\text{minPts} = 2$ $\epsilon = 1.1$
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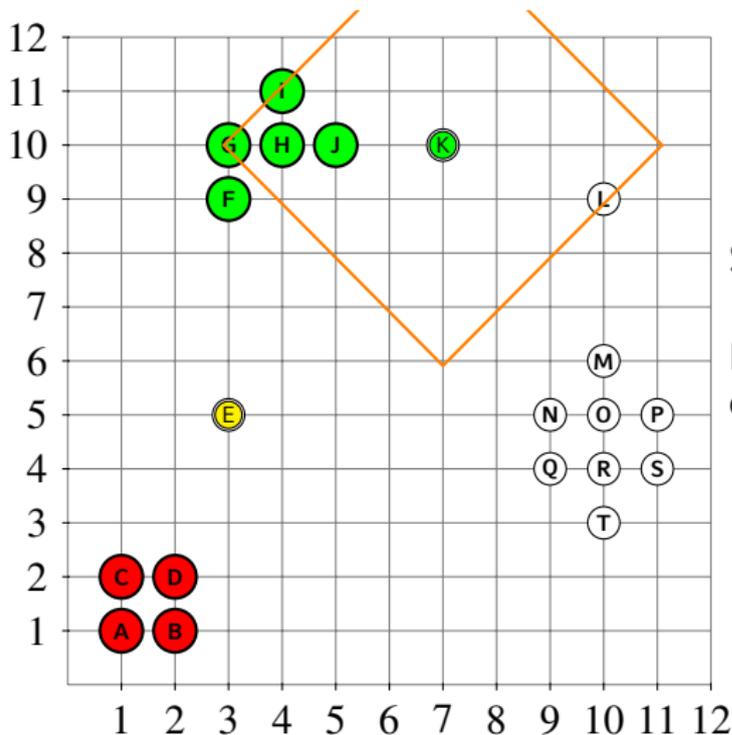
Seeds:

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 $\text{minPts} = 3$ $\epsilon = 1.1$
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 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 4$

Seeds:

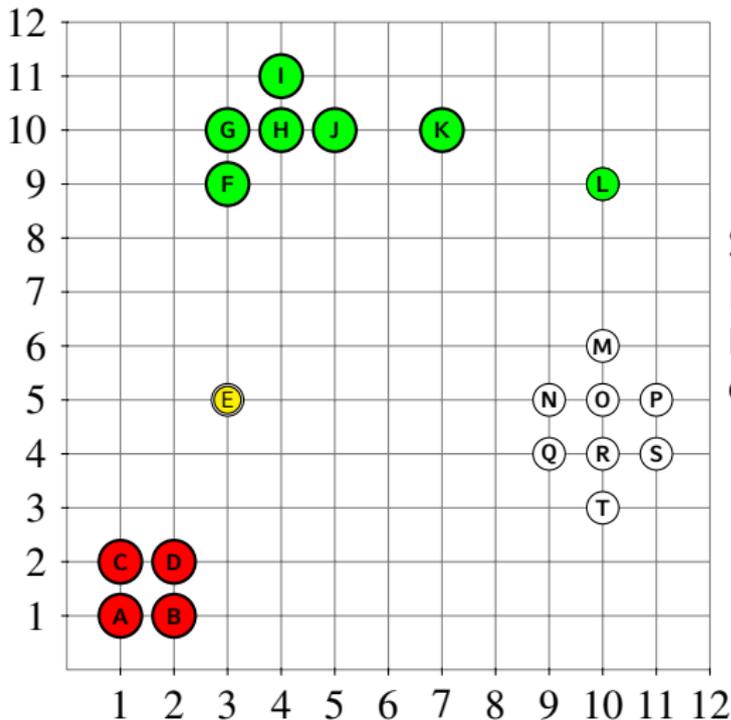
K

E nicht
eindeutig!

$\epsilon = 1.1$
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 $\text{minPts} = 3$ $\epsilon = 1.1$
 $\text{minPts} = 4$ $\epsilon = 2.1$
 $\text{minPts} = 4$ $\epsilon = 4.1$
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 $\text{minPts} = 4$  $\epsilon = 4.1$ $\text{minPts} = 4$

Seeds:

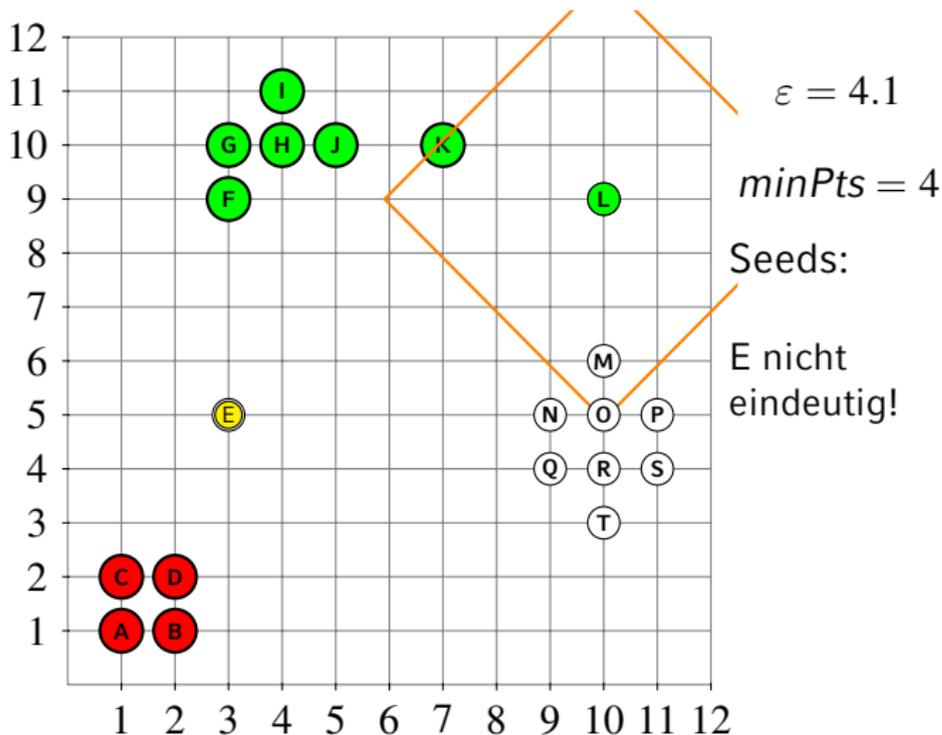
E nicht
eindeutig!

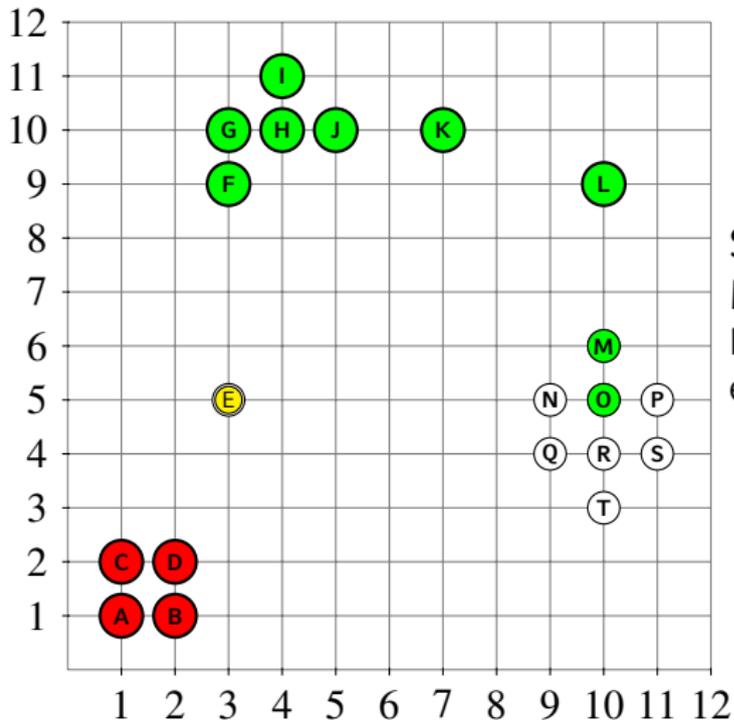
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 $\text{minPts} = 5$ $\epsilon = 4.1$
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Seeds:

L

E nicht
eindeutig!

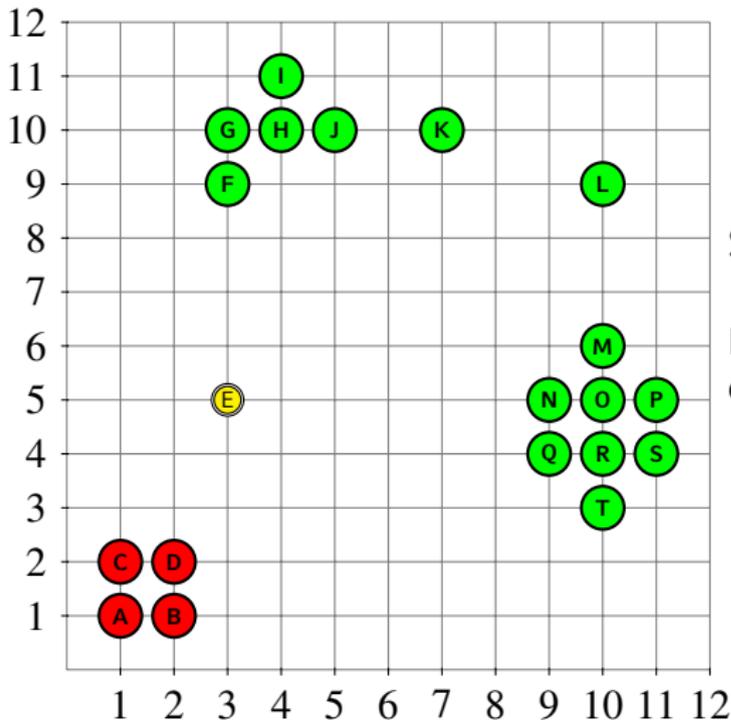
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 $\text{minPts} = 4$ $\epsilon = 4.1$
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$\epsilon = 1.1$
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Seeds:

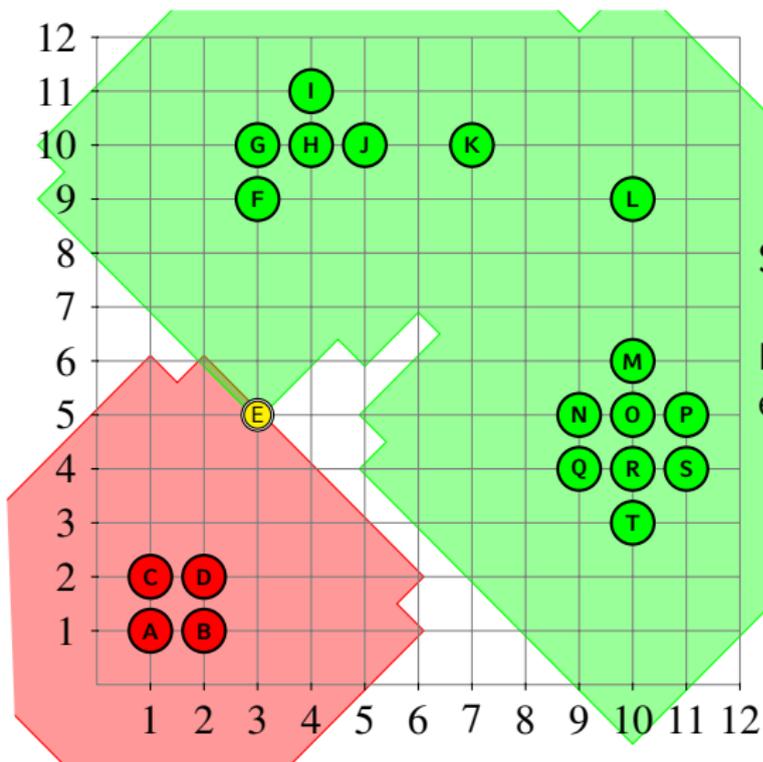
MO

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eindeutig!

$\epsilon = 1.1$
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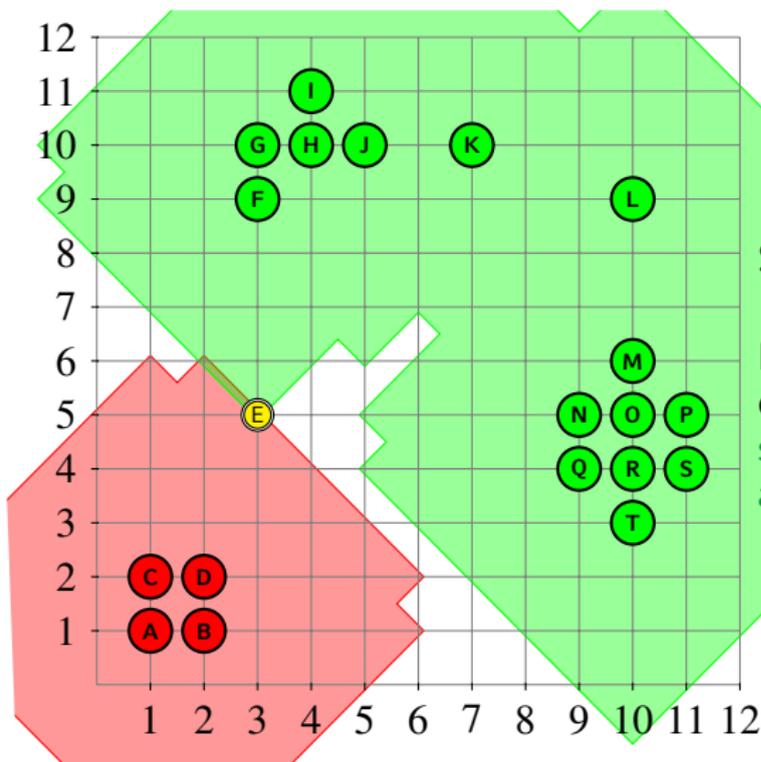
Seeds:

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$\epsilon = 1.1$
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Seeds:

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$\epsilon = 1.1$
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Seeds:

E nicht
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single-link
artiger Effekt