FAKULTÄT FÜR MATHEMATIK, INFORMATIK UND STATISTIK INSTITUT FÜR INFORMATIK

LEHRSTUHL FÜR DATENBANKSYSTEME UND DATA MINING

Lecture Notes for Deep Learning and Artificial Intelligence Winter Term 2018/2019

Sequential Decision Problems and autonomous Agents

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What is Artificial Intelligence?

Thinking Humanly: "The exciting new effort to make computers think .. machines with minds, in the full and literal sense"(Haugeland 1985) "[The automation of] activities that we associate with human thinking, activities such as decision making, problem solving, learning.."(Bellman 1978)

Acting Humanly: "The art of creating machines that perform functions that require intelligence when performed by people. "(Kurzweil, 1990) "The study of how to make computers do things at which, at the moment, people are better."(Rich and Knight 1991) Thinking Rationally: "The study of mental faculties through the use of computational models"(Charniak and McDermot 1985) "The study of the computations that make it possible to perceive, reason, and act."(Winston 1992)

Acting Rationally: "Computational Intelligence is the study of the design of intelligent agents."(Poole et al., 1998) "Al.. Is concerned with intelligent behavior in artefacts. "(Nilsson,

behavior in 1998)

From S.Russel, P. Norwig: Artificial Intelligence: A modern Approach, Pearson(2016)

AI & Machine/Deep Learning

so far we talked about Machine/Deep Learning:

- learns from data (observations)
- predicts future states
- interprets data
- transforms data
- •

machine learning is a core ingredient of modern AI:

- does not require exact knowledge of the mechanisms
- can handle "populations" which might be similar but vary
- can handle uncertain and unknown information

If we want to imitate human minds, we have to allow for individualism.

but there is more to Artificial Intelligence:

- make better decision: What is knowledge without using it?
- make machines act in an intelligent way: solve complex tasks with machines (chat bots, AI for games, ..)
- incorporate abstract knowledge and known physics:
 - not everything can be learned from observation
 - Global warming can be predicted based on physics but by observing 10.000 planets for 1000 years.
 - Humans conclude, abstract and transfer knowledge
 => Why learns something from data, I already know?
 => A child needs to 1 image to learn a new object
- Artificial general intelligence (AGI): build a "mind" that can solve various tasks and learns from all of them:
 - Specific Als heavily adapt to new tasks
 - Specific Als have to retrain on lots of data
 - => AGIs would learn different tasks and transfer what is applicable

AI and Decision Making

What is behaviour?

The reaction of a subject or an object to its environment?

- passive: a stone falls to the ground
- active: a mosquito flies into the light bulb

What makes behaviour intelligent?

- act like a human
- pursue a certain goal

=> Decide on an action to improve on a goal.

Prediction and Decision Making

How to make decisions to reach a goal?

- What do you know about the current situation ?
- What are your options ?
- Which option is the best?

Problems:

- Parts of your current situation might be unknown or not modeled
- Considering all options is often not possible
- Considering all possible impacts of choosing an option is often not possible.
- Your goal might not be reachable by one decision

Why is this connected to Machine learning?

Uncertain impacts :

- We do not really know what happens if we do something
- How does the environment react?
- How well do we perform the selected action?

Uncertain costs and rewards:

- We do not know if and when an action pays off.
- We cannot exactly predict uncertain factors like waiting times, prices, joy, congestions,..

Uncertain situation:

- We only got some input about our situation.
 e.g. sensor data, player view,..
- We might misinterpret a situation.

Sequential Decision Making

Machine learning can help to reduce these uncertainties by making good decision.

But: Can it do more?

- Observe humans or other intelligent agents and imitate their behaviour
- Observe behaviour and learn the outcomes and long term rewards of decisions
- \Rightarrow Directly learn the best action in any situation

This is the domain of Reinforcement Learning and training autonomous agents.

Applications Sequential Decision Making

- Al for Games:
 - Competitive agents: Alpha Go, Atari Games, Chess,..
 - Realistic opponents: football simulations,
- Controlling Robots and Systems
 - Autonomous Cars
 - Drones
 - Industrial Robots
 - Power stations
- Communicate with people
 - Chatbots for Technical Support
 - Ordering Assistants (e.g. reservations)
 - Internet advertisement
- Build intelligent assistant systems
 - planning trips and routs
 - optimize processes
 - manage financial portfolio

Reinforcement Leaning for board games

- games are classical domain of AI because opponent behaves not just nondeterministic but antagonistic
- progress on games like chess, backgammon, Poker.
- for a long time Go was considered the biggest challenge due to its enormous branching factor
- In Jan 2016: Deepmind challenged Grand Maste Lee Sedol with a program called Alpha Go and won.
- Alpha Go is a combination of reinforcement learning and Deep learning techniques which was trained on a huge database of Go matches.
- In 2017 the same time proposed Alpha Go Zero: Learns any board Game based on the rules only by playing against version of itself. Alpha Go Zero already outperformd prevision version of Alpha Go



3 hours

AlphaGo Zero plays like a human beginner, forgoing long term strategy to focus on greedily capturing as many stones as possible.

19 hours AlphaGo Zero has learnt the f

AlphaGo Zero has learnt the fundamentals of more advanced Go strategies such as life-and-death, influence and territory.



70 hours

AlphaGo Zero plays at super-human level. The game is disciplined and involves multiple challenges across the board.

Silver, D., Schrittwieser, J., Simonyan, K., Antonoglou, I., Huang, A., Guez, A., Hubert, T., Baker, L., Lai, M., Bolton, A., Chen, Y., Lillicrap, T., Hui, F., Sifre, L., van den Driessche, G., Graepel, T. & Hassabis, D. (2017). Mastering the game of Go without human knowledge. *Nature*, 550, 354--.

Games as Testbed for AGIs

Al is not build single purpose but receives images and general controls such as a human.

• DQN on Atari Games

https://deepmind.com/research/publications/playing-atarideep-reinforcement-learning/

• OpenAl Five (Dota2)

https://blog.openai.com/openai-five/

• RL for Starcraft II:

https://deepmind.com/blog/deepmind-and-blizzard-openstarcraft-ii-ai-research-environment/





https://techxplore.com/news/2016-11-deepmindboost-ai-unreal-agent.html



RL in Control and Robotics

 Control robots and drones



https://robohub.org/drones-that-drive/

Chatbots

For example: Google's assistent (https://www.youtube.com/watch?v=D5VN56jQMWM)

Modelfree and Modelbased Approaches

- Modelbased approaches a.k.a. planning
 - based on a complete model of the environment
 - computes rewards and actions within this models
 - optimizes policy based within this model
- Modelfree approaches
 - Assumes an interactive environment
 - Agent gets observations and selects actions
 - Environment process actions and sends new observation
 - The agents learns the best action based on the encountered interactions (episodes)

Prediction and Control

• Prediction:

Predicts how good an agents fares on a given problem.

⇒ Evaluate future behaviour

• Control:

Optimizes the action policy of an agent. => Optimize future behaviour

Agent and Environment

Environment



Deep Learning and Artificial Intelligence

Environment

Represents the world in which the agent is acting. (e.g. a game, a simulation or a robot)

- provides information about the state (e.g. images, sounds, game states)
- receives actions and applies them to alter its state

Properties of Environments

- partially / fully observable
- with known model/ model free
- deterministic / non-deterministic
- single vs. multi-agent
- competitive vs. collaborative
- static / dynamic / semi-dynamic
- discrete / continuous (states and/or actions)

Agents

Autonomous entity within the environment. types of agents:

• simple reflex agent

=> condition-action-rule
(example: If car-in-front-is-braking then initiate-braking.)

- model-based reflex agents (add internal state from history)
- goal-based agents (works towards a goal)
- utility-based agents (optimizes rewards/minimizes costs)
- learning agents (learns how to optimize rewards/costs)

Sequential Decision Making

- behavior is a sequence of actions
- sometimes immediate rewards must be sacrificed to acquire rewards in the future
 example: invest today to receive a pension in old age
- short-rewards might be very unlikely in many situations
 - example: score a goal from your own half in football
- => intelligent behavior needs to plan ahead

Agent and Environment



At each step t the environment:

- emits observation O_t
- emits scalar reward R_t
- receives and processes action A_t

At each step t the agent:

- selects action A_t
- receives observation O_t
- receives scalar reward R_t

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History and State

- What is the information we can base the decision on?
- History: Sequence of observations, action, rewards

 $H_t = O_1, R_1, A_1, O_2, O_2, O_2, \dots, A_{t-1}, O_t, R_t$

- all observable variables until t
- The history documents:
 - How the environment developed?
 - How the environment reacted to the last action?
 - Which action the agent selected at t given the history until t?
- State: Used to decide on the next decision.

formally: $S_t = f(H_t)$

(describes everything relevant to the decision)

Environment and Agent State



Environment state S_t^e :

- Complete status of e
- Observation/reward are derived from S^e_t
- S_t^e is usually invisible to the agent
- *S*^{*e*} *might contain irrelevant information*

Agent state S_t^a :

- Internal representation within agent a
- used for making the next decision
- S_t^a might be a function f(H_t)

A *Markov state* or *information state* contains all useful information from history.

Definition: A state St is Markov if and only if $P(S_{t+1}|S_t) = P(S_{t+1}|H_t)$

- everything to decide the future is contained in S_t
 => S_t is a sufficient statistic of the future
- the environment state S_t^e is Markov
- the history *H_t* is Markov

Observability of the Environment

- Full observability: $O_t = S_t^e = S_t^a$ the agent observes the complete environment state S_t^e = (fully observable) Markov Decision Process (MDP)
- Partially observability: $O_t \neq S_t^e$

= partially observable Markov decision process (POMDP) \Rightarrow agent must construct S_t^a from H_t

 \Rightarrow Beliefs of environment state:

$$S_t^a = (P(S_t^e = s_1), \dots, P(S_t^e = s_n))$$

example: robot with a camera (not exact location), poker player (only sees public cards), chat bot (does not know what the costumer wants from it)

Deterministic Sequential Planning

- Set of states $S = \{s_1, ..., s_n\}$
- Set of actions **A(s)** for each state *s* ∈ *S*
- Reward function R: R(s) (if negative = cost function)
- Transition function T: S×A => S: t(s,a) = s' (deterministic case !!)
- this implies:
 - episode = $s_1, a_1, r_1, s_2, a_2, r_2, s_3, a_3, r_3, s_3, \dots, s_l, a_l, r_l, s_{l+1}$
 - reward of the episode: $\sum_{i=1}^{l} \gamma^{i} r_{i}$ with $0 < \gamma \leq 1$ (γ =1: all rewards count the same, $\gamma < 1$: early rewards count more)
 - sometimes: process terminates when reaching a terminal state s^T or process end after k moves.
 - a strategy can be described by the actions in the episode which imply fixes states and rewards

Deterministic Sequential Planning

- Static, discrete, deterministic, known and fully observable environments:
 - S, A are discrete sets and known
 - t(s,a) has a deterministic state s'
 - Agent knows the current state
- **goal**: find a sequence of actions (path) that maximize the cumulated future rewards.

examples:

- routing from A to B on the map or find an exit
- riddles like the goat, wolf, cabbage transport problem

Example: Goat, Wolf, Cabbage

Task:

- You have a goat, a wolf and a cabbage you want to transport over a river on a small boat.
- The boat can only carry you an one item.
- If the wolf is alone with the goat, the wolf eats the goat.
- If the goat is alone with the cabbage the goat will eat the cabbage.

Which strategy can transport all three items over the river without losing one with a minimum amount of crossings?

Approach: A state models the boat, wolf, cabbage, goat as binary variable. (not all combinations are viable) Each crossing costs 1 time unit. The task is fulfilled when reaching the state (1,1,1,1) = all items are on the other side.

Example: Goat, Wolf, Cabbage



- (b,w,g,c)=(boat, wolf, goat, cabbage)
- invalid states: w=g≠b, g=c ≠b
- find the shortest path between (0,0,0,0) and (1,1,1,1)

Problem: When selecting an action, we do not know if it is on the shortest path.

Solution: Breadth-First search=first path arriving at (1,1,1,1) is optimal. (if costs per action vary, use Dijkstra's algorithm)

Nondeterministic Planning Problems

Problem: We might not know the outcome of an executed action

- the goat might not like the cabbage
- the wolf seems not to be hungry and leaves the goat be
- the boat can sink on each trip and I might drown
- => transitions lead to uncertain future states
- \Rightarrow t(s,a) is a stochastic function T: P(s'|s,a) for all s,s' \in S, a \in A

implications:

- we do not know the future state after performing action *a*.
- the reward R(s)/cost C(s) gets stochastic
- when searching a terminal state, there might be no secure path leading us to the target (the boat can always sink).
- => We need an action for each situation, we might encounter and not just the ones on a single path to the goal.

Policies and Utilities

- in **dynamic**, discrete, **non-deterministic**, known and fully observable environments
- a **policy** π is a mapping defining for every state $s \in S$ an action $\pi(s) \in A(s)$ (agent knows what to do in any situation)
- **stochastic policies**: Sometimes it is beneficial to vary the action then $\pi(s)$ is a distribution function over A(s).
 - think of a game where strictly following a strategy makes you predictable.

What is the best policy for **Rock - Paper – Scissor** having an unknown opponent?

sometimes best policy involves trying out different things

Markov Process

Markov processes are memoryless random processes generating sequences of states:

- A Markov Process (or Markov Chain) is a tuple (S, P) :
 - S is a finite set of states
 - P is a state transition probability matrix

 $P_{s,\acute{s}} = \Pr[S_{t+1} = \acute{s}|S_t = s]$

- ⇒ shortened definition: start and terminal states can be modelled as ordinary states, but are often mentioned separately.
- ⇒ Markov chains describe state sequence under a particular policy

Markov Reward Process $\langle S, P, R, \gamma \rangle$:

- S is a finite set of states
- P is a state transition probability matrix

$$-P_{s,\acute{s}} = \Pr[S_{t+1} = \acute{s}|S_t = s]$$

- R is a reward function $R_s = E[R_t|S_t = s]$
- $-\gamma$ discount factor, $\gamma \in [0,1]$
- ⇒ MDP under a fixed policy π (model prediction) ⇒ allows to evaluate sequences of states: $\sum_{i=1}^{l} \gamma^{i} r_{i}$ with $0 < \gamma \leq 1$ (discounted reward)

A Markov Decision Process (S, A, P, R, γ) :

- S is a finite set of states
- A is a finite set of actions
- P is a state transition probability matrix

$$P_{s,\acute{s}} = \Pr[S_{t+1} = \acute{s}|S_t = s]$$

- R is a reward function $R_s = E[R_t|S_t = s]$
- $-\gamma$ discount factor, $\gamma \in [0,1]$
- ⇒ environment where all states are Markov
- \Rightarrow allows to evaluate the quality of all possible policy

simple example: grid world



states S and rewards R(S)





actions

transition function P(S'|S,a)



Finite and Infinite Horizon MDP

When does the process stop?

Finite horizon:

- process terminates after n steps
- γ =1 allowed => all future rewards/costs are weighted equally
- **but**: policies become non-stationary $\pi(s) \rightarrow \pi^t(s)$

Infinite horizon:

- process potentially goes on forever or until a terminal state is reached
- termination might depend on the policy (proper policy: eventually reaches goal at some future time)
- γ <1 usually required:
 - future rewards/costs are weighted less
 - rewards of infinite random walks converges to a fixed value
 - human behaviour favours immediate rewards
 - immediate rewards earn more interest in financial applications
- Ergodic Markov Processes optimize the average reward for $\gamma=1$

Partially Observable Markov Decision Process

A **Partially Observable Markov Decision Process (POMDP)** is a MDP with hidden states (c.f. Hidden Markov Model).

A **POMDP** is a tuple $(S, A, O, P, R, Z, \gamma)$:

- S is a finite set of states
- A is a finite set of actions
- O is a finite set of observations
- P is a state transition probability matrix

$$P_{s,\dot{s}} = \Pr[S_{t+1} = \dot{s}|S_t = s]$$

- R is a reward function $R_s = E[R_{t+1}|S_t = s]$
- Z is an observation function, $Z_{s'o}^a = P[O_{t+1} = o | S_{t+1} = s', A_t = a]$
- γ discount factor, $\gamma \in [0,1]$
- \Rightarrow we only observe o but not s
- \Rightarrow Z describes the likelihood of observation o when taking action a in state s'

Belief States

Given history $h_t = O_1, R_1, A_1, O_2, O_2, O_2, \dots, A_{t-1}, O_t, R_t$. A belief state b(h) is a probability distribution over states, conditioned on the history h:

 $b(h) = (P[S_t = s^1 | H_t = h_t], \dots, P[S_t = s^n | H_t = h_t])$

- \Rightarrow b(h) described the likelihood that we are in state sⁱ at time t given the history h_t .
- \Rightarrow H_t satisfies the Markov property and thus, b(h) satisfies it as well.
- \Rightarrow POMDP can be described by history or beliefstate trees
- \Rightarrow adds uncertainty about the state to the expectation

Further Variants of MDPs

- Countably infinite state and/or action spaces
 => can be handled similarly as ordinary MDPs
- Continuous state and/or action spaces
 => Closed form for linear quadratic model (LQR)
- Continuous time
 - Requires partial differential equations
 - Hamilton-Jacobi-Bellman (HJB) equation
 - Limiting case of Bellman equation (t->0)

Evaluating Policies

We can compute the (discounted) reward of an episode, but how can be compute the reward of following a policy.

=> is in a nondeterministic environment, we might observe a variety of different episodes following the policy π => reward uncertain

Estimate the expected reward following π :

- We define the utility/state-value function of state s following policy π as: $U^{\pi}(s_i) = E[\sum_{t=i}^{\infty} \gamma^t R(s_t) | s_i = s, \pi]$
- Correspondingly, we define the action-value function: $q_{\pi}(s, a) = E[\sum_{t=i}^{\infty} \gamma^{t} R(s_{t}) | s_{i} = s, A_{i} = a, \pi]$

=> How to compute $U^{\pi}(s_i)$ and $q_{\pi}(s, a)$?

Bellman's Equations

 What is the reward of following π? (prediction) Utility U^π(s): expected reward when following π in state s w.r.t. some 0 ≤ γ ≤ 1:

•
$$U^{\pi}(s) = E[\sum_{t=0}^{\infty} \gamma^t R(s_t) | s_0 = s, \pi]$$

•
$$U^{\pi}(s) = \gamma^{0}R(s) + E[\sum_{t=1}^{\infty} \gamma^{t}R(s_{t}) | s_{0} = s, \pi]$$

•
$$U^{\pi}(s) = R(s) + \gamma \sum_{s' \in S} P(s'|s, \pi) U^{\pi}(s')$$

(Bellmann Equation)

• What is the optimal policy π^* ? (control) Bellman Optimality Equation:

$$U^{\pi*}(s) = R(s) + \gamma \max_{a \in A} \sum_{s' \in S} P(s'|s, a) \ U^{\pi*}(s')$$

Policy Evaluation

 Policy evaluation is much simpler than solving the bellman equation (c.f. Markov Reward Process)

$$U^{\pi}(s) = R(s) + \gamma \sum_{s' \in S} P(s'|s, \pi) \ U^{\pi}(s')$$

- Note that the non-linear function "max" is not present
- We can solve this by standard algorithms for linear equations systems
- For large state spaces solving linear equation systems takes $(O(n^3))$
- In large state spaces a simplified Bellman update for k times can be more performant

$$U_{i+1}(s) \leftarrow R(s) + \gamma \sum_{s'} P(s'|s, \pi_i) U_i(s')$$

Finding optimal Policies: Policy Iteration

- We are looking for the optimal policy.
- The exact utility values are not relevant if one action is clearly the optimal.
- Idea:

Alternate between:

- **Policy evaluation**: given a policy, calculate the corresponding utility values
- **Policy improvement**: Calculate the policy given the utility values $\pi(s) = \underset{a \in A}{argmax} \sum_{s' \in S} P(s'|s, a) U^*(s')$

(greedy policy selection)

Policy Iteration

repeat

 $U \leftarrow \text{PolicyEvaluation}(\pi, U, mdp)$ unchanged? $\leftarrow true$ for each state s in S do if $\max_{a \in A} \sum_{s'} P(s'|s, a) U[s'] > \sum_{s'} P(s'|s, \pi) U[s']$ then $\pi[s] \leftarrow \arg_{a \in A} \sum_{s'} P(s'|s, a) U[s']$ unchanged? $\leftarrow false$

until unchanged? return π

Value Iteration

- if we use Bellman updates anyway, we can join both steps
- update Bellman optimality equation directly:

$$U^*(s) = R(s) + \gamma \operatorname{argmax}_{a \in A} \sum_{s' \in S} P(s'|s, a) \ U^*(s')$$

- Non-linear system of equations
- Use Dynamic Programming:
 - Compute utility values for each state by using the current utility estimate
 - Repeat until it converges to U*
 - convergence can be proofed by contraction

(c.f.: S.Russel, P. Norwig: Artificial Intelligence: A modern Approach, Pearson(2016), page 654 for the proof)

Deep Learning and Artificial Intelligence

Value Iteration

repeat

 $U \leftarrow U'$ $\delta \leftarrow 0$ for each state s in S do $U'[s] \leftarrow R(s) + \gamma \max_{a \in A} \sum_{s'} P(s'|s, a) U[s']$ if $|U'[s] - U[s]| > \delta$ then $\delta \leftarrow |U'[s] - U[s]|$ until $\delta < \frac{\epsilon(1-\gamma)}{\gamma}$ return U

Synchronous Dynamic Programming

- Algorithms are based on state-value function U(s)
- Policy Iteration (prediction & control):
 - iterates prediction (Bellman Expectation Equation) and evaluation (Greedy Policy Improvement)
- Value Iteration (control):
 - updates utility and policy based on Bellman Optimality Equation
- Complexity O(mn²) per iteration for m actions and n states (with Bellmann updates)

Dynamic Programming with asynchronous backups

- Dynamic Programming with synchronous backups => all states are backed up in each iteration
- Dynamic Programming with asynchronous backups
 - select state to backup in any order
 - for each selected state, the appropriate back up is applied
 - allows to backups some states more often then others
 - Guaranteed to converge if all states continue to be selected

Advantages:

- some state might be never visited under the optimal policy π $_*$
- Utility U(s) might take different times to converge for different states
- => asynchronous update can significantly speed up computation

Directions for Async. Dyn. Programmming

- In-place dynamic programming
- Prioritised sweeping
- Real-time dynamic programming

In-place Dynamic Programming

 Synchronous Value iteration needs 2 copies for the U(s) for all s ∈ S:

$$U_{new}[s] \leftarrow R(s) + \gamma \max_{a \in A} \sum_{s'} P(s'|s, a) U_{old}[s']$$

 \Rightarrow'_{new} is computed based on U'_{old}

• Idea: directly update U'_{new} after back up of one state. for all s in S:

$$\mathbf{U}[s] \leftarrow R(s) + \gamma \max_{a \in A} \sum_{s'} P(s'|s, a) \, U[s']$$

 \Rightarrow less memory

 \Rightarrow back ups are done on more recent versions of the value function

Prioritized Sweep

• **Bellman error**: Difference between right and left side of the Bellman equation.

$$max_{a \in A}\left(R(s) + \gamma \sum_{s'} P(s'|s, a) U[s']\right) - U'[s]$$

Idea: Update the state with the largest Bellman error first and update Bellman errors of affected states (those relying on updated U(s))

- \Rightarrow Requires to know the predecessors
- ⇒ algorithm uses priority queue on states and always updates the one with the largest Bellman error until convergence.

Real-time dynamic programming

idea: Not all states are relevant to an agent.

- \Rightarrow some states might not even be visited under a reasonable policy
- \Rightarrow use the experience of the agent to select visited states

In particular:

- select state s_t
- select action a_t leading to reward R_{t+1}
- Backup s_t with U(s_t) = $\max_{a \in A} (R^a(s_t) + \gamma \sum_{s'} P(s'|s, a) U[s'])$
- sample over the possible follow states s_{t+1} and proceed with the sampled state (different variant use different sample schemes)

Caution: Not applicable to all types of MDPs:

- requires a proper policy, a terminal state and assumes costs
- requires monotonic lower bounds on the utility

Performance Bottlenecks on MDPs

- size of state space [S] is often huge (for example exponential in descriptive variables)
- transitions are potential |S|²·|A|
- In all dynamic programming approaches so far we do full-widths backups:
 - \Rightarrow We consider all potential followup states no matter their likelihood
 - ⇒ Unlikely steps often do not influence the utility to a high degree due to having a small likelihood

Solution approaches:

- summarize states
- build models considering a continuous state description vector than a discrete state
- sample backups instead of computing full-width backups
- \Rightarrow utilities are expectations and can be estimated using sampling

Summary MDPs

- MDPs rely on a Markov model with assumptions about: states, actions, rewards, transition probabilities, etc.
- If all the information is available, computing the optimal policy does not require any samples or learning
- Transitions probabilities are usually not defined but have to be estimated based on observations.
- usually observations ≠ states
 - partially observable MDP, estimate belief states (c.f. HMM)
 - set of possible states and transitions is unknown
- If the agent does not know the model, we require methods learning from experience
 => model free approaches and reinforcement learning

Literature

- Lecture notes D. Silver: Introduction to Reinforcement Learning (http://www0.cs.ucl.ac.uk/staff/d.silver/web/Teaching.html)
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- R. S. Sutton, A. G. Barto: Reinforcement Learning: An Introduction (Adaptive Computation and Machine Learning), The MIT Press; Auflage: 2., 2018