Chapter 8: Graph Data

Part 1: Link Analysis & Page Rank

Based on Leskovec, Rajaraman, Ullman 2014: Mining of Massive Datasets

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Big Data Management and Analytics





• Exam on the 5th of February, 2016, 14.00 to 16.00

•If you wish to attend, please register!

http://uniworx.ifi.lmu.de/



Graph Data: Social Networks



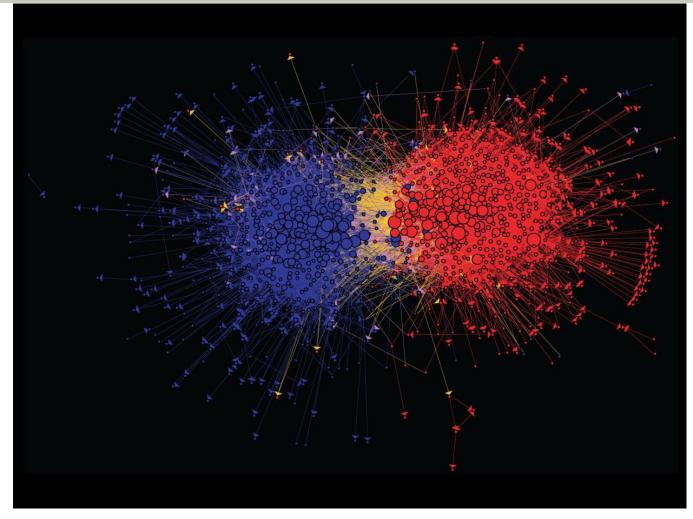


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Graph Data: Media Networks



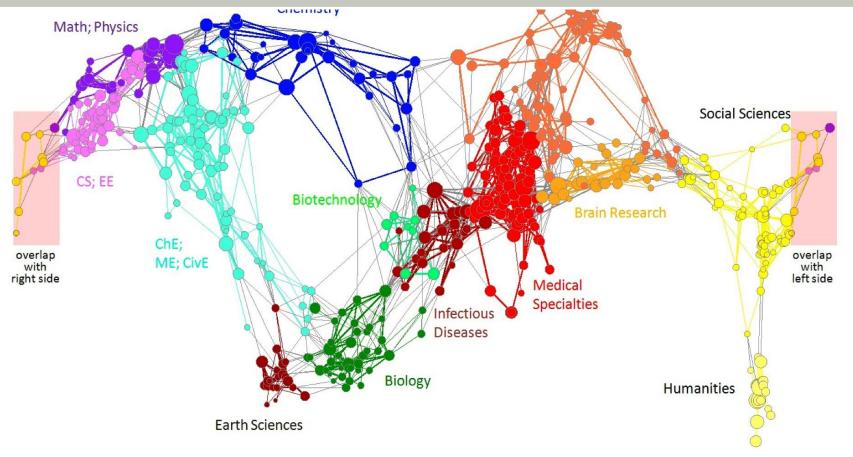


Connections between political blogs Polarization of the network [Adamic-Glance, 2005]



Graph Data: Information Networks





Citation Networks and Map of Science [Börner et al., 2012]



Graph Data: Technological Networks



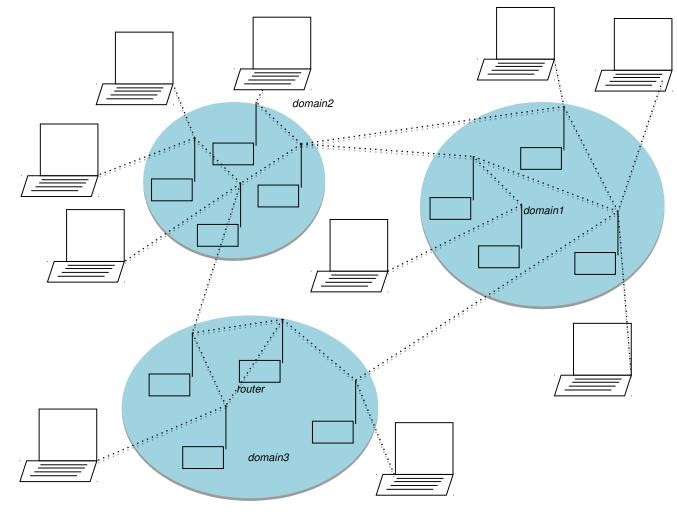


Road Network of Toulouse [Mathieu Leplatre]



Graph Data: Communication Networks





The Internet



Web as a Graph



Web as a directed graph:

- Nodes: Webpages
- Edges: Hyperlinks

LMU München Department of Computer Science

Database Systems Group Big Data Management & Analytics

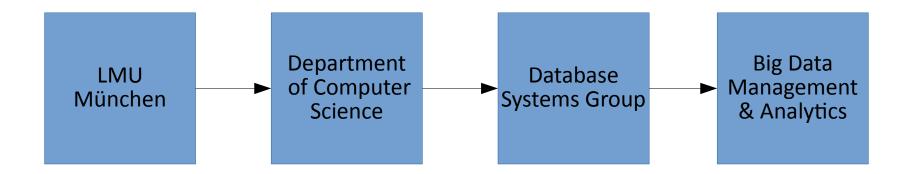


Web as a Graph



Web as a directed graph:

- Nodes: Webpages
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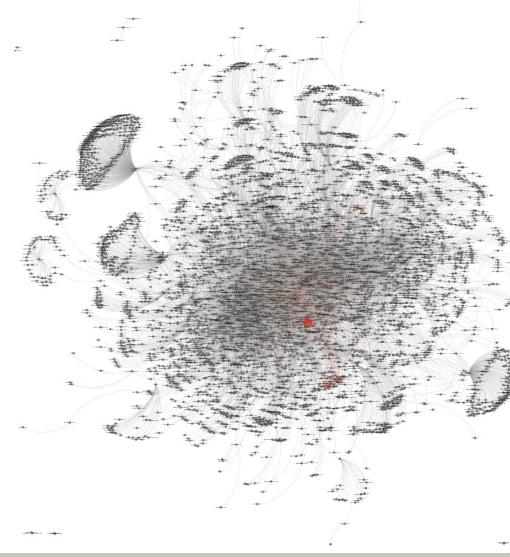




General Question



How to organise the web?



10



General Question



How to organise the web? **First try:** Human Curated Web Directories Yahoo, DMOZ, LookSmart YAHOO



Yahoo! Mail - Get your free e-mail account today!

Shopping - Yellow Pages - People Search - Maps - Travel Agent - Classifieds - Personals - Games - Chat Email - Calendar - Pager - My Yahoo! - Today's News - Sports - Weather - TV - Stock Quotes - more ...

News & Media

Arts & Humanities Literature, Photography ...

Business & Economy Companies, Finance, Jobs ...

Computers & Internet Internet, WWW, Software, Games

Education Universities, K-12, College Entrance.

Entertainment Cool Links, Movies, Humor, Music ...

Government Military, Politics, Law, Taxes ...

Health Medicine, Diseases, Drugs, Fitness ... **Recreation & Sports** Sports, Travel, Autos, Outdoors ...

Full Coverage, Newspapers, TV ...

Reference Libraries, Dictionaries, Quotations...

Regional Countries, Regions, US States..

Science Biology, Astronomy, Engineering ...

Society & Culture

Social Science Archaeology, Economics, Languages.

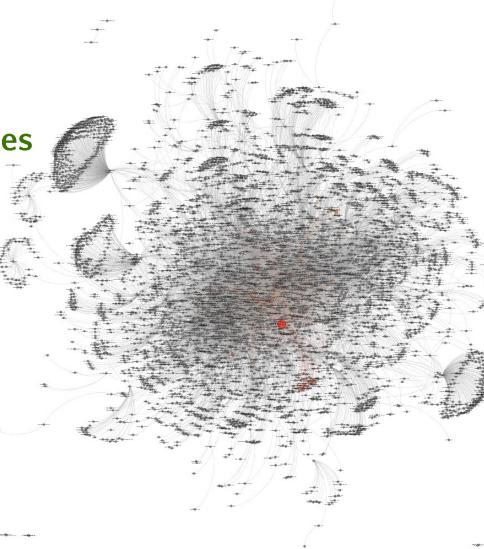
Y! Clubs - create your own People, Environment, Religion ...

In the News King Hussein of Jordan dies Online: Lewinsky video testimony

> NASA comet mission NBA season opens

Weekend's top movies

Inside Yahoo! Y! Personals - find a Valentine Shop for your Valentine





General Question

How to organise the web?



First try: Human Curated Web Directories Second try: Web Search But: Web is huge, full of untrusted documents, random things, web spam, etc.





1) Web contains many sources of information. → Who to trust?

Idea: Trustworthy pages may point to each other

2) What is the "best" answer to a certain query?→ How to rank results?

No single right answer.





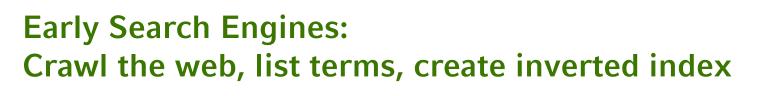
Early Search Engines: Crawl the web, list terms, create inverted index

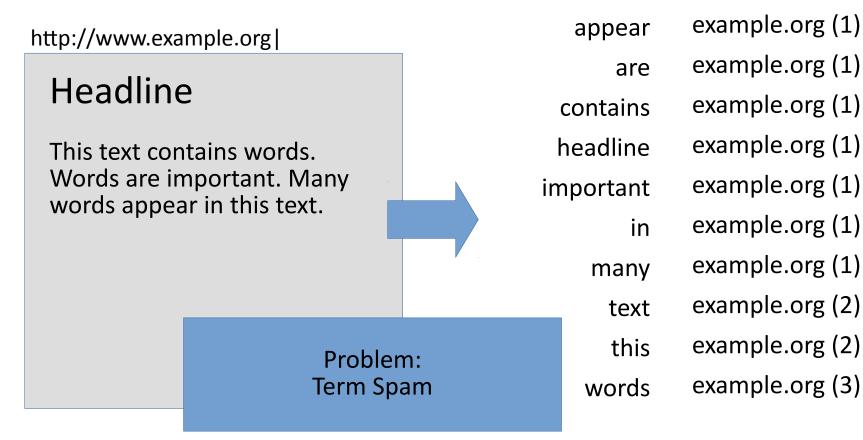
http://www.example.org|

Headline

This text contains words. Words are important. Many words appear in this text.













on Turkey.

the Union

President

Obama will

speech.



Not all web pages are equally "important"

VS.

www.nytimes.com (The New York Times)

The New Hork Times Tuesday, January 12, 2016 👘 Today's Paper 🔤 Video 😽 33*F | S. & P. 500 +0.28% -World U.S. Politics N.Y. Business Opinion Tech Science Health Sports Arts Style Food Travel Magazine T Magazine Real Estate ALL The Opinion Pages ELECTION 2016 Explosion Kills ARD D. KAHLENBERG Agony and Starvation in the Strong Unions, Strong Syrian War at Least 10 in Democracy Tourist District Weakening labor increases Aid convoys and inequality and instability. of Istanbul their supplies offer Brooks: The Brutalism of Ted Cruz only a respite What is By CEYLAN YEGINSU 9:34 AM ET needed is an end to the President Recep Tayyip Roller: Ads That Play to Racist Svrian war. Erdogan said a Syrian Fears suicide bomber was behind • Editorial: DuPont Kept Using a Toxic Chemical OP-ED CONTRIBUTOR the attack in the Istanbul The Other Refugee Crisis Room for Debate: How to Define Obama's Legacy district of Sultanahmet that killed 10 and wounded at How do we support The Stone: David Bowie's Vision of Love those who want to least 15 people, the latest in a series of terrorist assaults return to Syria? · Join us on Facebook » Iowans' Passion for Sanders Worries Clinton What the President Watching With voters mobbing Bernie Sanders at events in the state, Probably Won't Say 24m A medical panel has updated its mammogram guidelines but maintains that women with average risk can safely begin exposing a disparity in passion for the two Democrats. in Tonight's Address Hillary Clinton has gone on the attack # 493 Con screening at 50, a stance that has inspired much debate MoveOn Site Puts Its Backing Behind Sanders 22 minutes ago In his State of The New York Time · Chris Christie Makes Steady Rightward Shift on Guns China's Dalian Wanda Group said that it was buying Legendary Entertainment, one of Your Tuesday Briefing Hollywood's biggest movie production companies, for as much as \$3.5 billion By ADEEL HASSAN 9:50 AM E 1 3 offer reassurance on efforts Here's what you need to The New York Times against terrorism, but he is know to start your day. New York Today: A Sprinkle of Stardust 5:59 AM said to believe that the sense The fantasy sports websites FanDuel an of danger has been inflated. DraftKings will be allowed to operate in New York while they try to fend off a chall Obama's Gun Policies Are Popular, Polls Show 7:16 / from the state's attorney general. A Look Back at the First Lady's Allowing His Art to Deliver a Final Message Guests 5:15 AM ET Prosecutors in Florence, Italy, are investigating the death of an American woman who was found in her apartment over Mr. Bowie, who in his 50-year caree reimagined the worlds of pop music, art and the weekend the police said The Trials of ashion, told very few people about the cancer Alice Goffman that preceded his death on Sunday. · Bowie's Fashion Legacy Her first book, · Obituary: A Star Who Transcended Music and Art Dies at 69 "On the Run" about the lives Four Teenagers Are Charged in Brooklyn Rane Case

www.thetimesonline.com (The Times of Northwest Indiana, Munster, IN)



Big Data Management and Analytics





Not all web pages are equally "important"

<u>www.nytimes.com</u> vs. (The New York Times) www.thetimesonline.com (The Times of Northwest Indiana, Munster, IN)

in-links: ~13.600.000

in-links: 5.960

→ There is a large diversity in the web-graph node connectivity.
IDEA: rank pages by their link structure!





Idea: links as votes

Page is more important if it has more links

In-links? Out-links?





Idea: links as votes

Page is more important if it has more in-links

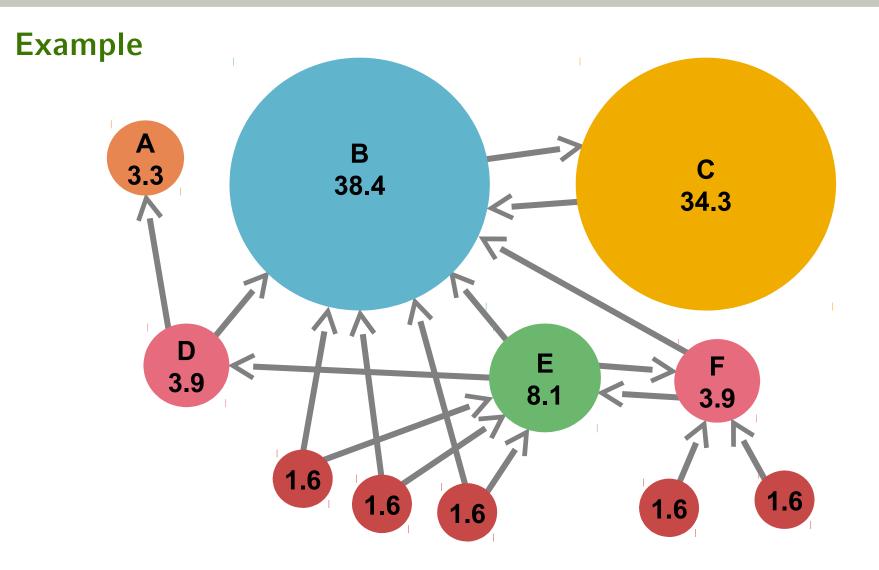
Think of in-links as votes.

Are all in-links equal? Links from important pages count more => Recursive Definition!



Page Rank: "Flow" Formulation



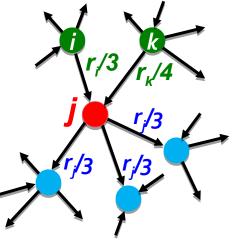






- Each link's vote is proportional to the importance of its source page
- If page j with importance r_j has n out-links, each link gets r_j / n votes
- Page j's own importance is the sum of the votes on its in-links

$$r_{j} = r_{i}/3 + r_{k}/4$$



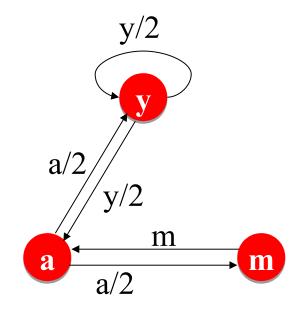




- •A "vote" from an important page is worth more
- •A page is more important if it is pointed to by other important pages

Define a "rank" r_j for page j (with d_j = out-degree of node i)

$$r_j = \sum_{i \to j} \frac{r_i}{\mathbf{d}_i}$$



"Flow" equations: $r_{y} = r_{y}/2 + r_{a}/2$ $r_{a} = r_{y}/2 + r_{m}$ $r_{m} = r_{a}/2$





•3 equations, 3 unknowns, no constants

- No unique solution
- All solutions equivalent modulo the scale factor

•Additional constraint forces uniqueness:

- $r_{y} + r_{a} + r_{m} = 1$
- Solution via Gaussian elimination $r_v = 2/5$, $r_a = 2/5$, $r_m = 1/5$
- Gaussian elimination method works for small examples, but we need a better method for large web-sized graphs

•We need a new formulation!





• Stochastic adjacency matrix M

- Let page i has d_i out-links
- If $i \rightarrow j$, then $M_{ji} = 1/d_{i'}$, else $M_{ji} = 0$
- M is a column stochastic matrix: columns sum to 1
- Rank vector r: vector with an entry per page
 - r_i is the importance score of page i
 - $\Sigma_{i} r_{i} = 1$

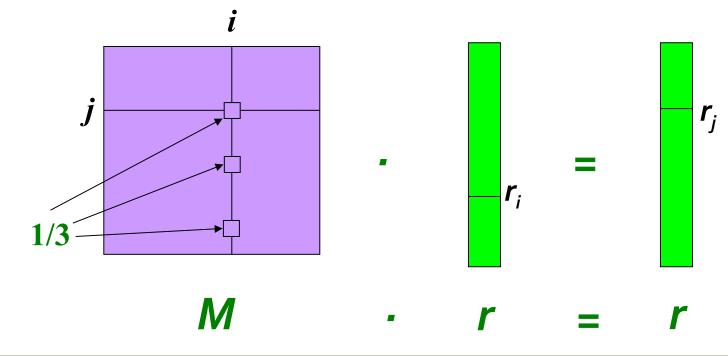
•The flow equations can be written

$$\mathbf{r} = \mathbf{M} \cdot \mathbf{r}$$





- Remember the flow equation: $r_j = \sum_{i \to j} \frac{r_i}{d_i}$
- Flow equation in matrix form: $M \cdot r = r$
 - Suppose page i links to 3 pages, including j:





• The flow equations can be written as $r = M \cdot r$

- So the rank vector r is an *eigenvector* of the stochastic web matrix M
 - In fact, its first or principal *eigenvector* with corresponding *eigenvalue* 1
 - Largest *eigenvalue* of *M* is 1 since *M* is column stochastic (with non-negative entries)
 - We know *r* is unit length and each column of *M* sums to 1, so *M* · *r* ≤ 1

•We can now efficiently solve for *r*! Power Iteration



Note: x is an eigenvector with corresponding eigenvalue λ if:

 $Ax = \lambda x$





• Power Iteration is an eigenvalue algorithm

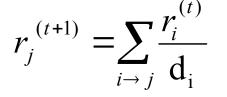
- Also known as Von Mises iteration
- Given a matrix A, P.I. returns a value λ and a nonzero vector v, such that $Av = \lambda v$
- •Will find only the dominant eigenvector (the vector corresponding to the largest eigenvalue)

$$\begin{aligned} \mathbf{r}^{(1)} &= \mathbf{M} \cdot \mathbf{r}^{(0)} \\ \mathbf{r}^{(2)} &= \mathbf{M} \cdot \mathbf{r}^{(1)} = \mathbf{M} (\mathbf{M} \cdot \mathbf{r}^{(0)}) = \mathbf{M}^2 \cdot \mathbf{r}^{(0)} \\ \mathbf{r}^{(3)} &= \mathbf{M} \cdot \mathbf{r}^{(2)} = \mathbf{M} (\mathbf{M}^2 \cdot \mathbf{r}^{(0)}) = \mathbf{M}^3 \cdot \mathbf{r}^{(0)} \end{aligned}$$





- Given a web graph with n nodes, where the nodes are pages and the edges are hyperlinks
- •Power iteration: a simple iterative scheme
 - Suppose there are N web pages
 - Initialize: $r^{(0)} = [1/N, ..., 1/N]^T$



- Iterate: $r^{(t+1)} = M \cdot r^{(t)}$
- Stop when: $|r^{(t+1)} r^{(t)}|_1 < \epsilon$

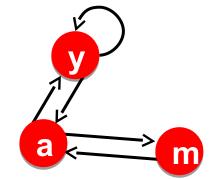


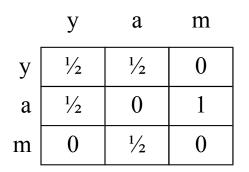
PageRank with Power Iteration



• Power Iteration:

- Set $r_i = 1/N$
- 1: $r'_{j} = \sum_{i \to j} r_{i} / d_{i}$
- 2: r = r'
- Goto 1





$$r_{y} = r_{y}/2 + r_{a}/2$$
$$r_{a} = r_{y}/2 + r_{m}$$
$$r_{m} = r_{a}/2$$



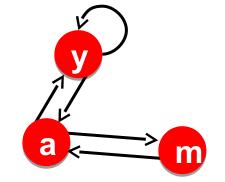
PageRank with Power Iteration

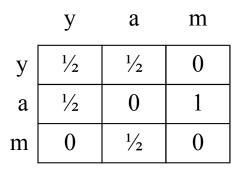


• Power Iteration:

- Set $r_i = 1/N$
- 1: $r'_{j} = \sum_{i \to j} r_{i} / d_{i}$
- 2: r = r'
- Goto 1

•Example:





$r_{y} = r_{y}^{2} + r_{a}^{2}$
$r_a = r_y/2 + r_m$
$r_{\rm m} = r_{\rm a}/2$

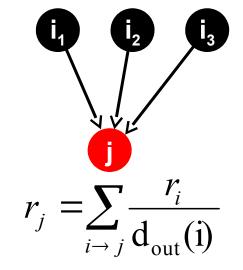
r _y		1/3	1/3	5/12	9/24		6/15
r _a	=	1/3	3/6	1/3	11/24	•••	6/15
r _m		1/3	1/6	3/12	1/6		3/15





Imagine a random web surfer:

- At any time t, surfer is on some page i
- At time *t* + 1, the surfer follows an out-link from *i* uniformly at random
- Ends up on page *j* linked from *i*
- Process repeats indefinitely



•Let:

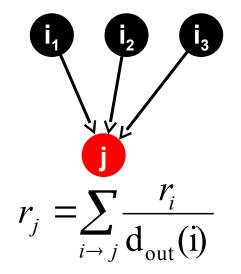
- *p(t)* ... vector whose ith coordinate is the probability that surfer is at page *i* at time *t*
- So, *p(t)* is a probability distribution over pages





•Where is surfer at time t + 1?

- Follows a link uniformly at random $p(t + 1) = M \cdot p(t)$
- Suppose the random walk reaches a state p (t + 1) = M · p (t) = p (t) then p (t) is stationary distribution of a random walk



- Our original rank vector r satisfies $r = M \cdot r$
 - So, r is a stationary distribution for a random walk





A central result from the theory of random walks (a.k.a. Markov processes):

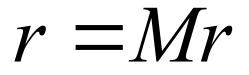
For graphs that satisfy **certain conditions**, the **stationary distribution is unique** and eventually will be reached no matter what the initial probability distribution at time t = 0.



PageRank in real life



 $r_j^{(t+1)} = \sum_{i \to j} \frac{r_i^{(r)}}{d_i}$



•Does this converge?

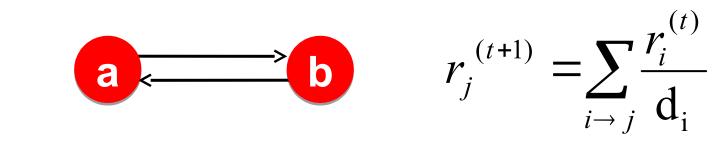
• Does it converge to what we want?

•Are results reasonable?

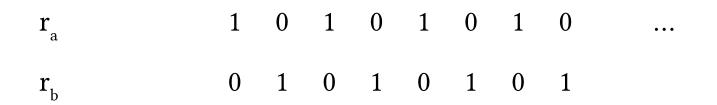


Does this converge?





• Example:



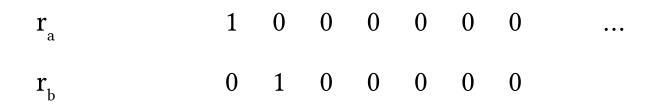


Does it converge to what we want?





• Example:



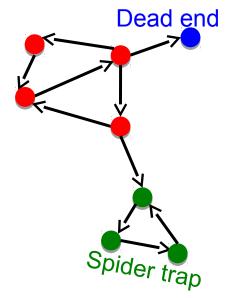


PageRank: Problems



2 Problems:

- Some pages are dead ends (have no out-links)
 - Random walk has "nowhere to go" to
 - Such pages cause "leak" of importance



Spider traps (all out-links are within a group)

- Random walk gets "stuck" in a trap
- Eventually spider trap absorbs all importance



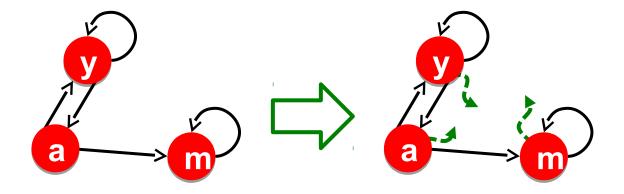


The Google solution for spider traps: *Teleports*

At each time step, the random surfer has two options:

- With probability ß, follow a link at random
- With probability 1 ß, jump to some random page
- Common values for ß range between 0.8 and 0.9

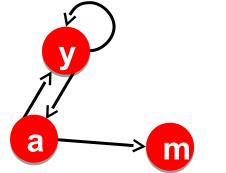
Surfer will teleport out of spider trap within a few time steps

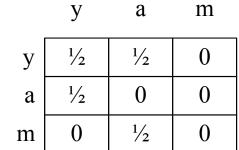






Dead ends cause the page importance to leak out, because the adjacency matrix is non-stochastic.





 $r_{y} = r_{y}/2 + r_{a}/2$ $r_{a} = r_{y}/2$ $r_{m} = r_{a}/2$

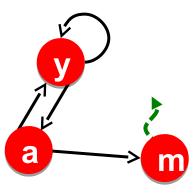


Dead Ends: Solution

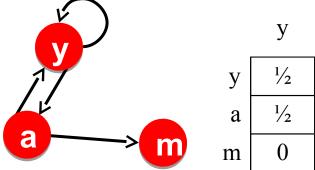


Dead ends cause the page importance to leak out, because the adjacency matrix is non-stochastic.

Solution: Always teleport! Adjust matrix accordingly:



	У	а	m
у	1/2	1/2	1/3
a	1/2	0	1/3
m	0	1/2	1/3



 $r_{y} = r_{y}/2 + r_{a}/2$ $r_{a} = r_{y}/2$ $r_{m} = r_{a}/2$





The final version of the Google PageRank: [Brin-Page 98]

$$r_j = \sum_{i \to j} \beta \ \frac{r_i}{d_i} + (1 - \beta) \frac{1}{N}$$

(This formulation assumes M has no dead ends.M can either be preprocessed to remove all dead ends or with explicit teleports to random links from dead ends.)



The Google Matrix



Google matrix A combines the adjacency matrix M with the random teleports by a factor ß.

(With ß = 0.8 for this example)

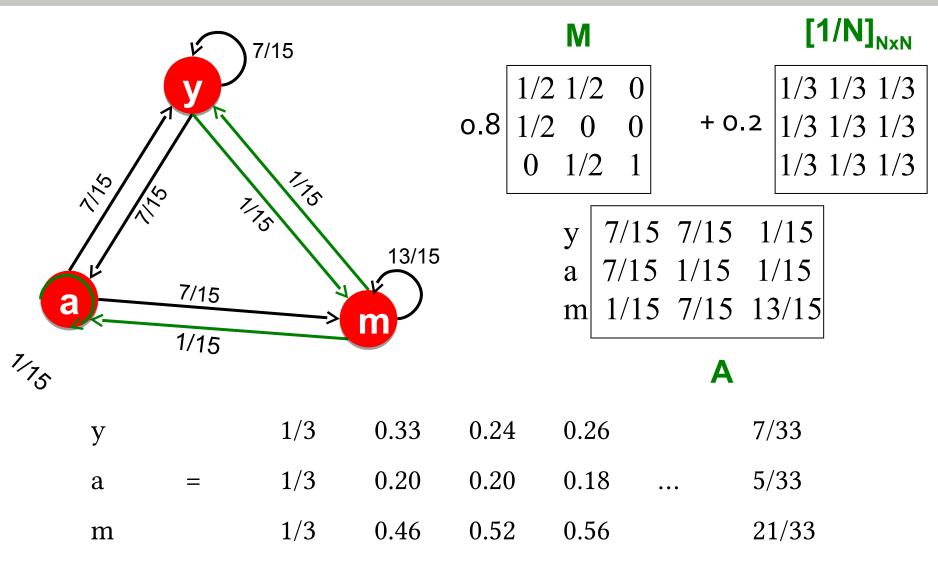


Α



The Google Matrix









•Measures generic popularity of a page

- Biased against topic-specific authorities
- Solution: Topic-specific PageRank

•Uses only one measure of importance

- Other models exist
- Solution: e.g., Hubs and Authorities

Susceptible to Link Spam

- Evolved from term spam (see: older search engines)
- Artificial link topographies created to boost page rank
- Solution: TrustRank





- Instead of generic popularity, can we measure popularity within a certain topic?
- Goal: evaluate web pages not only according to their popularity, but by how close they are to a particular topic, e.g., "sports" or "history"
- Allows search queries to be answered based on user interest
 - Example: Query "Trojan" may yield different results depending on whether user is interested in sports, history, computer security, ...





• Modification in random walk behaviour (teleports)

•Teleport has probability to go to:

- Standard PageRank: Any page with equal probability To avoid dead ends and spider-traps
- Topic-specific PageRank: A topic specific set of "relevant" pages (teleport set)

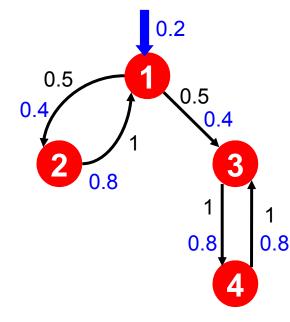
Idea: Bias the random walk

- When walker teleport, they pick a page from set S
- S contains only pages that are relevant to the topic, e.g., from Open Directory (DMOZ) pages for given topic
- For each teleport set S, we get a different vector r_s



Example: Topic-specific PageRank





Suppose *S* = {1}, *B* = 0.8

Node	Iteration						
	0	1	2	stable			
1	0.25	0.4	0.28	0.294			
2	0.25	0.1	0.16	0.118			
3	0.25	0.3	0.32	0.327			
4	0.25	0.2	0.24	0.261			

S={1}, β=0.90:
r=[0.17, 0.07, 0.40, 0.36]
S={1}, β=0.8:
r=[0.29, 0.11, 0.32, 0.26]
S={1}, β=0.70:
r=[0.39, 0.14, 0.27, 0.19]

S={1,2,3,4}, β=0.8:
r=[0.13, 0.10, 0.39, 0.36]
S={1,2,3}, β=0.8:
r=[0.17, 0.13, 0.38, 0.30]
S={1,2}, β=0.8:
r=[0.26, 0.20, 0.29, 0.23]
S={1}, β=0.8:
r=[0.29, 0.11, 0.32, 0.26]





• Create different PageRanks for different topics

• The 16 DMOZ top-level categories art, business, sports, ...

•Which topic ranking to use?

- User can pick from a menu
- Classify query into a topic
- Use context of query: e.g., query is launched from website about certain topic, or history of queries
- User context, e.g., bookmarks, ...



PageRank Summary



•"Normal" PageRank

- Teleports uniformly at random to any node

Topic-specific PageRank, also known as Personalized PageRank

- Teleports to a topic specific set of pages
- Nodes can have different landing probabilities
 S = [0.1, 0.0, 0.2, 0.0, 0.0, 0.0, 0.5, 0.0, 0.2, 0.0]

Random walk with restarts





•Spamming:

Any deliberate action with the intent to boost a web page's position in search engine results incommensurate with page's actual relevance

•Spam:

Query results that are the result of spamming

→ very broad definition

•Approximately 10% – 15% of web pages are spam





- Early spamming techniques flooded web pages with unfitting words to exploit search engines
 - Example: Web page for T-Shirts includes the word "movie" over and over again
 - "Term spam"
- •As Google became more dominant, spam farms tried to target PageRank to a single page by placing many contextual links on other pages
 - "Link Spam" or "Google Bomb"



2003 George W. Bush Google Bomb



0 1	Web	Images	Groups	News	Froogle	Local	mo	re »
Google	misera	miserable failure				Search		Advanced Search Preferences
0								

Web

Results 1 - 10 of about 969,000 for miserable failure. (0.06 seconds)

Biography of President George W. Bush

Biography of the president from the official White House web site. www.whitehouse.gov/president/gwbbio.html - 29k - Cached - Similar pages Past Presidents - Kids Only - Current News - President More results from www.whitehouse.gov »

Welcome to MichaelMoore.com!

Official site of the gadfly of corporations, creator of the film Roger and Me and the television show The Awful Truth. Includes mailing list, message board, ... www.michaelmoore.com/ - 35k - Sep 1, 2005 - Cached - Similar pages

BBC NEWS | Americas | 'Miserable failure' links to Bush

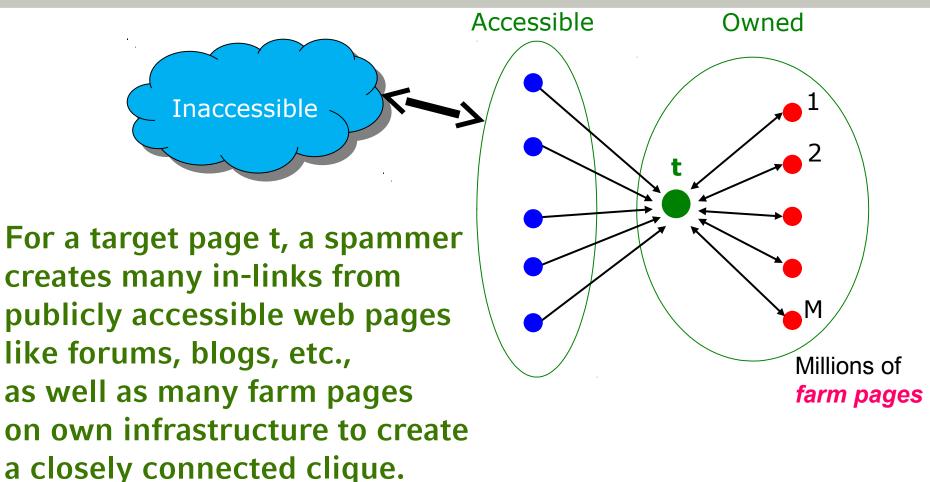
Web users manipulate a popular search engine so an unflattering description leads to the president's page. news.bbc.co.uk/2/hi/americas/3298443.stm - 31k - Cached - Similar pages

Google's (and Inktomi's) Miserable Failure

A search for **miserable failure** on Google brings up the official George W. Bush biography from the US White House web site. Dismissed by Google as not a ... searchenginewatch.com/sereport/article.php/3296101 - 45k - Sep 1, 2005 - <u>Cached</u> - <u>Similar pages</u>









Combating Spam



Combating Term Spam:

- Analyze text using statistical methods
- Similar to email spam filtering
- Detecting duplicate pages

Combating Link Spam:

- Detection and blacklisting of structures that look like spam farms
- Leads to another war: hiding and detecting
- TrustRank = topic-specific PageRank with teleport to a set of trusted pages, e.g., .edu domains or similar





•Alternative model for TrustRank: Trust Propagation

Initial seed set of trusted pages (evaluated by hand)

Set trust tp of each trusted page p to 1

• For each out-link from p, a portion of the trust is passed on to target page q

Trust is additive

• Trust of q is sum of all trust conferred by its in-links

•If trust is below a threshold, page is flagged as spam





• Exam on the 5th of February, 2016, 14.00 to 16.00

•If you wish to attend, please register!

http://uniworx.ifi.lmu.de/