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Abstract. A fundamental task in artificial intelligence and computer vision is to build machines that can behave like a human in recognizing a broad range of visual concepts. This paper aims to investigate and develop intelligent systems for learning the concept of female facial beauty and producing human-like predictors. Artists and social scientists have long been fascinated by the notion of facial beauty, but study by computer scientists has only begun in the last few years. Our work is notably different from and goes beyond previous works in several aspects: 1) we focus on *fully-automatic* learning approaches that do not require costly manual annotation of landmark facial features but simply take the raw pixels as inputs; 2) our study is based on a collection of data that is an order of magnitude larger than that of any previous study; 3) we imposed no restrictions in terms of pose, lighting, background, expression, age, and ethnicity on the face images used for training and testing. These factors significantly increased the difficulty of the learning task. We show that a biologically-inspired model with multiple layers of trainable feature extractors can produce results that are much more human-like than the previously used eigenface approach. Finally, we develop a novel visualization method to interpret the learned model and revealed the existence of several beautiful features that go beyond the current averageness and symmetry hypotheses.

1 Introduction

The notion of beauty has been an ill defined abstract concept for most of human history. Serious discussion of beauty has traditionally been the purview of artists and philosophers. It was not until the latter half of the twentieth century that the concept of facial beauty was explored by social scientists [1] and not until very recently that it was studied by computer scientists [2]. In this paper we explore a method of both quantifying and predicting female facial beauty using a hierarchical feed-forward model and discuss the relationship between our method and existing methods.

 $^{^{\}star}$ Work was performed while all authors were at NEC Labs America.

The social science approach to this problem can be characterized by the search for easily measurable and semantically meaningful features that are correlated with a human perception of beauty. In 1991, Alley and Cunningham showed that averaging many aligned face images together produced an attractive face, but that many attractive faces were not at all average [3]. In 1994 Grammer and Thornhill showed that facial symmetry can be related to facial attractiveness [4]. Since that time, the need for more complex feature representations has shifted research in this area to computer scientists.

Most computer science approaches to this problem can be described as geometric or landmark feature methods. A landmark feature is a manually selected point on a human face that usually has some semantic meaning such as right corner of mouth or center of left eye. The distances between these points and the ratios between these distances are then extracted and used for classification using some machine learning algorithm. While there are some methods of extracting this information automatically [5] most previous work relies on a very accurate set of dense manual labels, which are not currently available. Furthermore most previous methods are evaluated on relatively small datasets with different evaluation and ground truth methodologies. In 2001 Aarabi et al. built a classification system based on 8 landmark ratios and evaluated the method on a dataset of 80 images rated on a scale of 1-4 [2]. In 2005 Eisenthal *et al.* assembled an ensemble of features that included landmark distances and ratios, an indicator of facial symmetry, skin smoothness, hair color, and the coefficients of an eigenface decomposition [6]. Their method was evaluated on two datasets of 92 images each with ratings 1-7. Kagian et al. later improved upon their method using an improved feature selection method [7].

Most recently Guo and Sim have explored the related problem of automatic makeup application [8], which uses an example to transfer a style of makeup to a new face.

While all of the above methods produce respectable results for their respective data, they share a common set of flaws. Their datasets are very small and usually restricted to a very small and meticulously prepared subset of the population (*e.g.* uniform ethnicity, age, expression, pose and/or lighting conditions). The images are studio-quality photos taken by professional photographers. As another limitation, all these methods are not fully-automatic recognition systems, because they rely heavily on the accurate manual localization of landmark features and often ignore the image itself once they are collected.

We have attempted to solve the problem with fewer restrictions on the data and a ground truth rating methodology that produces an accurate ranking of the images in the data set. We have collected 2056 images of frontal female faces aged 18-40 with few restrictions on ethnicity, lighting, pose, or expression. Most of the face images are cropped from low-quality photos taken by cell-phone cameras. The data size is 20 times larger the that of any previous study. Some sorted examples can be found in figure 3, the ranking methodology is discussed in section 2. Because of the heavy cost of labeling landmark features on such a large data set, in this paper we solely focused on methodologies which do not require these features³. Furthermore, although landmark features and ratios appear to be correlated with facial attractiveness, it is yet unclear to what extent human brains really use these features to form their notion of facial beauty. In this paper we test the hypothesis if a biologically-inspired learning architecture can achieve a near human-level performance on this particular task using a large data set with few restrictions. The learning machine is an instance of the Hubel-Wiesel model [9] which simulates the structure and functionality of visual cortex systems, and consists of multiple layers of trainable feature extractors. In section 3 we discuss discuss the details of the approach to predict female facial attractiveness. In section 4.2 we present the experimental results. Interestingly, we develop a novel way to visualize and interpret the learned black-box model, which reveals some meaningful features highly relevant to beauty prediction and complementary to previous findings.

To summarize, we contribute to the field a method of quantifying and predicting female facial attractiveness using an automatically learned appearance model (as opposed to a manual geometric model). A more realistic dataset has been collected that is 20 times larger than any previously published work and has far fewer restrictions. To the best of our knowledge, it is the first work to test if a Hubel-Wiesel model can achieve a near human-level performance on the task of scoring female facial attractiveness. We also provide a novel method of interpreting the learned model and use it to present evidence for the existence of beautiful features that go beyond the current averageness and symmetry hypotheses. We believe that the work enriched the experiences of AI research toward building generic intelligent systems.

2 Dataset and Ground Truth

In order to make a credible attack on this problem we require a large dataset of high quality images labeled with a beauty score. As of the time of writing, no such data are publicly available. However there does exist a popular website HOTorNOT ⁴ with millions of images and billions of ratings. Users who submit their photo to this site waive their privacy expectations and agree to have their likeness criticized. Unfortunately the ratings that are associated with images in this dataset were collected from images of people as opposed to faces, and are not valid for the problem we are addressing. We have run face detection software on a subset of images from this website and produced a dataset of 2056 images and collected ratings of our own from 30 labelers.

2.1 Absolute vs. Pairwise Ratings

There are several kinds of ratings that can be collected for this task. The most popular are absolute ratings where a user is presented with a single image and

³ We also note that landmark feature methods fall outside the purview of computer vision as the original images may be discarded once the features are marked and ratings are collected.

 $^{^4}$ http://www.hotornot.com/

asked to give a score, typically between 1 and 10. Most previous work has used some version of absolute ratings usually presented in the form of a Likert scale [10] where the user is asked about the level of agreement with a statement. This form of rating requires many users to rate each image such that a distribution of ratings can be gathered and averaged to estimate the true score. This method is less than ideal because each user will have a different system of rating images and a user's rating of one image may be affected by the rating given to the previous image, among other things.

Another method used in [11] was to ask a user to sort a collection of images according to some criteria. This method is likely to give reliable ratings but it is challenging for users to sort a large dataset since this requires considering all the data at once.

The final method is to present a user with pair of images and ask which is more attractive. This method presents a user with a binary decision which we have found can be made more quickly than an absolute rating. In section 2.3 we show how to present an informative pair of images to a user in order to speed up the process of ranking the images in a dataset. This is the method that we have chosen to label our data.

2.2 Conversion to Global Absolute Score

Pairwise ratings are easy to collect, but in order to use them for building a scoring system we need to convert the ratings into an absolute score for each image. ⁵ To convert the scores from pairwise to absolute, we minimize a cost function defined such that as many of the pairwise preferences as possible are enforced and the scores lie within a specified range. Let $\mathbf{s} = \{s_1, s_2, \ldots, s_N\}$ be the set of all scores assigned to images 1 to N. We formulate the problem into minimizing the cost function:

$$J(\mathbf{s}) = \sum_{i=1}^{M} \phi(s_i^+ - s_i^-) + \lambda \mathbf{s}^T \mathbf{s}$$
(1)

where (s_i^+/s_i^-) denotes the current scores of the *i*th comparison and $\phi(d)$ is some cost function which penalizes images that have scores which disagree with one of M pairwise preferences and λ is a regularization constant that controls the range of final scores. We define $\phi(d)$ as an exponential cost function $\phi(d) = e^{-d}$. However this function can be any monotonically increasing cost function such as the hinge loss, which may be advisable in the presence of greater labeling noise. A gradient descent approach is then used to minimize this cost function. This iterative approach was chosen because as we receive new labels, we can quickly update the scores without resolving the entire problem. Our implementation is

⁵ One could alternatively train a model using image pairs and a siamese architecture such as in [12]. However a random cross validation split of the images would invalidate around half of the pairwise preferences.

built on a web server which updates the scores in real time as new labels are entered.

We note that in our study we hypothesize that in a large sense people agree on a consistent opinion on facial attractiveness, which is also the assumption by most of the previous work. Each individual's opinion can be varied due to factors like culture, race, and education. In this paper we focus on learning the common sense and leave further investigation on personal effects to future work.

2.3 Active learning

When our system is initialized, all images have a zero score and image pairs are presented to users at random. However as many comparisons are made and the scores begin to disperse, the efficacy of this strategy decays. The reason for this is due in part to labeling noise. If two images with very different scores are compared it is likely that the image with the higher score will be selected. If this is the case, we learn almost nothing from this comparison. However if the user accidentally clicks on the wrong image, this can have a very disruptive effect on the accuracy of the ranking.



Fig. 1. Simulation results for converting pairwise preferences to an absolute score.

For this reason we use a relevance feedback approach to selecting image pairs to present to the user. We first select an image at random with probability inversely proportional to the number of ratings r_i , it has received so far.

$$p(I_i) = \frac{(r_i + \epsilon)^{-1}}{\sum_{i=1}^{N} (r_i + \epsilon)^{-1}}$$
(2)

We then select the next image with probability that decays with the distance to first image score.

$$p(I_i|s_1) = \frac{\exp\left(-(s_1 - s_i)^2/\sigma^2\right)}{\sum_{i=1}^N \exp\left(-(s_1 - s_j)^2/\sigma^2\right)}$$
(3)

Where σ^2 is the current variance of **s**. This approach is similar to the tournament sort algorithm and has significantly reduced the number of pairwise preferences needed to achieve a desired correlation of 0.9 (15k vs. 20k). Figure 1 shows the results of a simulation similar in size to our dataset. In this simulation 15% of the preferences were marked incorrectly to reflect the inherent noise in collecting preference data.

3 Learning Methods

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Fig. 2. An overview of the organization of our **multiscale** model. The first convolution is only performed on the luminance channel. Downsampled versions of the original image are fed back into the model at lower levels. Arrows represent downsampling, lines represent convolution and the boxes represent downsampling with the max operator. Feature dimensions are listed on the left (height x width x channels).

Given a set of images and associated beauty scores, our task is to train a regression model that can predict those scores. We adopt a predictive function that models the relationship between an input image I and the output score s,

and learn the model in the following way

$$\min_{\mathbf{w},\theta} \sum_{i=1}^{N} (s_i - y_i)^2 + \lambda \mathbf{w}^T \mathbf{w}, \quad \text{s. t.} \quad y_i = \mathbf{w}^\top \Phi(I_i; \theta) + b \tag{4}$$

where I_i is the raw-pixel of the *i*-th image represented by size 128x128 in YCbCr colorspace, **w** is a *D*-dimensional weight vector, *b* is a scalar bias term, λ is a positive scalar fixed to be 0.01 in our experiments. As a main difference from the previous work, here we use $\Phi(\cdot)$ to directly operate on raw pixels *I* for extracting visual features, and its parameters θ are *automatically learned from data* with *no* manual efforts. In our study we investigated the following special cases of the model, whose differences are the definition of $\Phi(I; \theta)$:

- Eigenface Approach: The method has been used for facial beauty prediction by [6], perhaps the only attempt so far requiring no manual landmark features. The method is as follows. We first run singular value decomposition (SVD) on the input training data $[I_1, \ldots, I_N]$ to obtain its rank D decomposition $\mathbf{U} \mathbf{\Sigma} \mathbf{V}^{\top}$, and then set $\theta = \mathbf{U}$ as a set of linear filters to operate on images so that $\Phi(I_i; \theta) = \mathbf{U}^{\top} I_i$. We tried various D among $\{10, 20, 50, 100, 200\}$ and found that D = 100 gave the best performance.
- Single Layer Model: In contrast to Eigenface that uses global filters of receptive field 128×128 , this model consists of 48 local 9×9 linear filters, each followed by a non-linear logistic transformation. The filters convolute over the whole image and produce 48 feature maps, which were then down sampled by running max-operator within each non-overlapping 8×8 region and thus reduced to 48 smaller 15×15 feature maps. The results serve as the outputs of $\Phi(I_i; \theta)$.
- Two Layer Model: We further enrich the complexity of $\Phi(I_i; \theta)$ by adding one more layer of feature extraction. In more details, in the first layer the model employs separate 16 9 × 9 filters on the luminance channel, and 8 5 × 5 filters on a down-sampled chrominance channel; in the second layer, 24 5 × 5 filters are connected to the output of the previous layer, followed by max down-sampling by a factor of 4.
- Multiscale Model: The model is similar to the single-layer model, but with 3 additional convolution/downsampling layers. A diagram of this model can be found in figure 2. This model has 2974 tunable parameters⁶.

In each of our models, every element of each filters is a learnable parameter (*e.g.* if our first layer has 8 5x5 filters, then there will be 200 tunable parameters in that layer). As we can see, these models represent a family of architectures with gradually increased complexities: from linear to nonlinear, from single-layer to multi-layer, from global to local, and from course to fine feature extractions. In particular, the employed max operator makes the architecture more local- and

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 $^{^{6}}$ Note that this an order of magnitude less than the model trained for the task of face verification in $\left[12\right]$

partially scale-invariant, which is particularly useful in our case to handle the diversity of natural facial photos. The architectures can all be seen as a form of convolutional neural network [13] [12] that realize the well-known Hubel-Wiesel model [14] inspired by the structure and functionalities of the visual cortex.

These systems were trained using stochastic gradient descent with a quadratic loss function. Optimal performance on the test set was usually found within a few hundred iterations, models with fewer parameters tend to converge faster both in iterations and computation time. We have tested many models with varying detailed configurations, and found in general that the number and size of filters are not crucial but the number of layers are more important — $\Phi(I_i; \theta)$ containing 4 layers of feature extraction generally outperformed the counterparts with fewer layers.

4 Empirical Study

4.1 Prediction Results

A full and complete comparison with previous work would be challenging both to perform and interpret. Most of the previous methods that have been successful rely on many manually marked landmark features, the distances between them, the ratios between those distances, and other hand crafted features. Manually labeling every image in our dataset by hand would be very costly so we will only compare with methods which do not require landmark features. As of the time of publication, the only such method is the eigenface approach used in [6].

We compare the four learning methods described in Section 3 based on the 2056 female face images and the absolute scores computed from pair-wise comparisons. For each method, we investigate its performance on faces with and without face alignment. We perform alignment using the unsupervised method proposed in [15]. This approach is advantageous because it requires no manual annotation. In all the experiments, we fixed the training set to be 1028 randomly chosen images and used the remaining 1028 images for test.

Pearson's correlation coefficient is used to evaluate the alignment between the machine generated score and the human absolute score on the test data. Table 1 shows a comparison between the four methods – eigenface, single layer, two layer and multiscale models. We can see a significant improvement in the performance with alignment for the eigenface approach and a slight improvement for the hierarchal models. This discrepancy is likely due to the translation invariance that is introduced by the local filtering and down sampling with the max operator over multiple levels, as was first observed by [13]. Another observation is, with more layers being used, the performance improves. We note that eigenface produced a correlation score 0.40 in [6] on 92 studio quality photos of females with similar ages and the same ethnicity origins, but resulted very poor accuracy in our experiments. This shows that the large variability of our data significantly increased the difficulty of appearance-based approaches.

Though the Pearson's correlation provides a quantitative evaluation on how close the machine generated scores are to the human scores, it lacks of intuitive

Method	Correlation	Correlation
	w/o alignment	w/ alignment
Eigenface	0.134	0.180
Single Layer Model	0.403	0.417
Two Layer Model	0.405	0.438
Multiscale Model	0.425	0.458

 Table 1. Correlation score of different methods.

sense about this closeness. In figure 4 we show a scatter plot of the actual and predicted scores for the **multiscale** model on the aligned test images. This plot shows both the correlation found with our method and the variability in our data. One way to look at the results is that, if without knowing the labels of axes, it is quite difficult to tell which dimension is by human and which by machine. We highly suggest readers to try such a test⁷ on figure 4 with an enlarged display.

Figure 3 shows the top and bottom eight images according the humans and the machine. Note that at the ground truth for our training was generated with around 10^4 pairwise preferences, which is not sufficient to rank the data with complete accuracy. However, the notion of complete accuracy is something that can only be achieved for a single user, as no two people have the same exact preferences.

4.2 What Does the Model Learn?

With so much variability it is difficult to determine what features are being used for prediction. In this section we discuss a method of identifying these features to better understand the learned models. One of the classic criticisms of the hierarchical model and neural networks in general, is the *black box* problem. That is, what features are we using and why are they relevant? This is typically addressed by presenting the convolution filters and noting their similarity to edge detectors (*e.g.* gabor filters). This was interesting the first time it was presented, but by now everyone in the community knows that edges are important for almost every vision task. We attempt to address this issue using a logical extension to the backpropagation algorithm.

Backpropagation, the most fundamental tasks in training a neural network, is where the gradient of the final error function is propagated back through each layer in a network so that the gradient of each weight can be calculated w.r.t. the final error function. When a neural network is trained, the training input and associated labels are fixed, and the weights are iteratively optimized to reduce the error between the prediction and the true label.

We propose the *dual problem*. Given a trained neural network, fix the weights, set the gradient of the prediction to a fixed value and backpropagate the gradient all the way through the network to the input image. This gives the derivative

 $^{^{7}}$ Whether or not this constitutes a valid Turning test is left up to the reader.



Fig. 3. The top (a/b) and bottom (c/d) eight images from our dataset according to human ratings (a/c) and machine predictions (b/d).

of the image w.r.t. the concept the network was trained with. This information is useful for several reasons. Most importantly, it indicates the regions of the original image that are most relevant to the task at hand. Additionally, the sign of the gradient indicates whether increasing the value of a particular pixel will increase or decrease the network output, meaning we can perform a gradient descent optimization on the original image.

Semantic Gradient Descent A regularized cost function w.r.t. a desired score $(s^{(d)})$ and the corresponding gradient descent update can be written as:

$$J(I_t) = \phi(s_t - s^{(d)}) + \lambda \phi(I_t - I_0)$$
(5)

and

$$I_{t+1} = I_t - \omega \left(\frac{\partial I_t}{\partial s} + \lambda (I_t - I_0) \right)$$
(6)

In our implementation we use $\phi(x) = x^2$ and use different values of λ for the luminance and chrominance color channels.

The Derivative of Beauty The most pressing question is, *What does the derivative of beauty look like?* Figure 5 shows several example images and their respective gradients with respect to beauty for the multiscale model trained on



Fig. 4. A Scatter plot showing actual and predicted scores with the corresponding faces.



Fig. 5. Several faces (a) with their beauty derivative (b). These images are averaged over 10 gradient descent iterations and scaled in the colorspace for visibility.

aligned images. This clearly shows that the most important feature in this model is the darkness and color of the eyes.

The gradient descent approach can be used both to *beautify* and *beastify* the original image. If we vary the regularization parameters and change the sign of the derivative, we can visualize the image manifold induced by the optimization. Figure 6 shows how specific features are modified as the regularization is relaxed.

This shows most important features being used to predict beauty and concurs with some human observations about the data and beauty in general.

The first observation is that women often wear dark eye makeup to accentuate their eyes. This makeup often has a dark blue or purple tint. We can see this reflected on the extremes of figure 6 (c). In figure 6 (b), the eyes on the bottom are dark blue/purple tint while the eyes on the top are bright with a yellow/green tint.

The second observation is that large noses are generally not very attractive. If we again look at the extremes of figure 6 (c) we can see that the edges around the nose on the right have been smoothed, while the same edges on the left side have been accentuated.



Fig. 6. The manifold of beauty for two images. (a) From left (beast) to right (beauty) we can see how the regularization term (λ_Y/λ_C) controls the amount of modification. Specific features from (a): Eyes (b) and Noses (c).

The final observation is that a bright smile is attractive. Unfortunately the large amount of variation in facial expressions and mouth position in our training data leads to artifacts in these regions such as in the the extremes of figure 6. However when we apply these modifications to the average image in figure 7, we can see a change in the perceived expression.

Beautiful Features One of the early observations in the study of facial beauty was that averaged faces are attractive [3]. This is known as the averageness hypothesis. The average face from the dataset, presented in figure 7, has a score of 0.026. The scores returned by the proposed model are all zero mean, indicating that the average face is only of average attractiveness. This would seem to contradict the averageness hypothesis, however since the dataset presented here



Fig. 7. The average face image (a), beautified images (b) and beastified images (c). The x axis represents changes in the luminance channel, while the y axis represents changes in the chrominance channels.

was collected from a pool of user submitted photos, it does not represent a truly random sampling of female faces (*i.e.* it may have a positive bias).

As of the time of publication, averageness, symmetry, and face geometry are the only definable features that have been shown to be correlated with facial attractiveness. This paper presents evidence that many of the cosmetic products used by women to darken their eyes and hide lines and wrinkles are in fact attractive features.

5 Conclusion

We have presented a method of both quantifying and predicting female facial beauty using a hierarchical feed-forward model. Our method does not require landmark features which makes it complimentary to the traditional geometric approach [2] [16] [6] [7] [17] when the problem of accurately estimating landmark feature locations is solved. The system has been evaluated on a more realistic dataset that is an order of magnitude larger than any previously published results. It has been shown that in addition to achieving a statistically significant level of correlation with human ratings, the features extracted have semantic meaning. We believe that the work enriches the experience of AI research toward building generic intelligent systems. Our future work is to improve the prediction for this problem and to extend our work to cover the other half of the human population.

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